

DeepRob [Group 2] Lecture 3 by Harshavardhan, Raj Surya, Vaibhav NeRFs, Gaussian Splatting and Manipulation University of Minnesota





DR View Synthesis vs 3D Reconstruction

View Synthesis

Input: 3D Model and viewing direction

Output: Image









Point Cloud

Voxels

Mesh



Image Source: Antonie Toisoul, 3D Data Representations





Stores

- Occupancy
- Density
- Color
- Opacity

Pros

- Simplicity
- Uniform Resolution

Cons

- Memory
- Resolution
- Scalability









Image Credits: Prof. Shubham Tulsiani, CMU - Learning for 3D Vision Kajiya, J.T., Herzen, B.P.V.: Ray tracing volume densities. Computer Graphics (SIGGRAPH) (1984)





 $\sigma(x)$ = Volume Density, c = Color, T = Transmittance t = Distance along the ray, d = Direction of ray



Image Credits: Prof. Shubham Tulsiani, CMU - Learning for 3D Vision Ben Mildenhall, Pratul P. Srinivasan, Matthew Tancik, Jonathan T. Barron, Ravi Ramamoorthi, & Ren Ng. (2020). NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis.





Image Credits: Prof. Shubham Tulsiani, CMU - Learning for 3D Vision Ben Mildenhall, Pratul P. Srinivasan, Matthew Tancik, Jonathan T. Barron, Ravi Ramamoorthi, & Ren Ng. (2020). NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis.



$$\hat{C}(\mathbf{r}) = \sum_{i=1}^{N} T_i (1 - \exp(-\sigma_i \delta_i)) \mathbf{c}_i, \text{ where } T_i = \exp\left(-\sum_{j=1}^{i-1} \sigma_j \delta_j\right)$$

$$\delta_i = t_{i+1} - t_i$$

Algorithm

- Sample points (uniform/non-uniform) along the ray
- Compute C at each point/segment
- Sum up contributions across all segments







Algorithm

- Shoot a ray through every pixel
- Compute radiance (color)





- Memory usage -
- -
- Computational Cost Resolution Limitation -







QUESTIONS?







F = Multi Layer Perceptron

Maps 5D coordinate to volume density and directional emitted color

5 numbers in, 4 numbers out

 $(x,y,z,\theta,\phi) \longrightarrow F\theta \longrightarrow (R,G,B,\sigma)$









Image Source: Neural Radiance Fields (NeRFs): A Technical Exploration by Gaudenz Boesch









- 1. Modelling High Frequency Positional Encoding
- 2. Hierarchical Volume Sampling



Ground Truth



No Positional Encoding







Ground Truth



No Positional Encoding

Neural Networks are biased towards learning low frequency functions.

Ben Mildenhall, Pratul P. Srinivasan, Matthew Tancik, Jonathan T. Barron, Ravi Ramamoorthi, & Ren Ng. (2020). NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis.
 Rahaman, N., Baratin, A., Arpit, D., Dr¨axler, F., Lin, M., Hamprecht, F.A., Bengio, Y., Courville, A.C.: On the spectral bias of neural networks.
 In: ICML (2018)





Ground Truth



No Positional Encoding



With positional encoding

Map input into higher dimensional input.

$$\gamma(p) = (\sin(2^0\pi p), \cos(2^0\pi p), \cdots, \sin(2^{L-1}\pi p), \cos(2^{L-1}\pi p))$$

This function $\gamma(\cdot)$ is applied separately to each of the input variables.





Algorithm

- Perform uniform sampling (coarse sampling)
- Calculate PDF of each point
- Perform importance sampling using the PDF (fine sampling)









What is the expected behaviour of a well trained MLP in general?



Image Source: https://thecorrelation.in/overfitting-and-underfitting/





One Scene, One MLP

NO GENERALIZATION



Image Source: https://thecorrelation.in/overfitting-and-underfitting/



Dataset

- RGB Images, corresponding camera pose and intrinsics along with scene bounds.





Dataset

- RGB Images, corresponding camera pose and intrinsics along with scene bounds. Batch

- Sample camera rays (batch size = 4096) from set of all pixels





Dataset

- RGB Images, corresponding camera pose and intrinsics along with scene bounds. Batch

- Sample camera rays (batch size = 4096) from set of all pixels Algorithm

- Sample Nc (=64) coarse points.
- Perform ray marching. Use MLP to compute color and density at each point.
- Compute PDF and sample Nf (=128) fine points. Perform ray marching again.
- Compute loss and optimize (Optimizer = Adam).

$$\hat{C}(\mathbf{r}) = \sum_{i=1}^{N} T_i (1 - \exp(-\sigma_i \delta_i)) \mathbf{c}_i, \text{ where } T_i = \exp\left(-\sum_{j=1}^{i-1} \sigma_j \delta_j\right)$$
$$\mathcal{L} = \sum_{\mathbf{r} \in \mathcal{R}} \left[\left\| \hat{C}_c(\mathbf{r}) - C(\mathbf{r}) \right\|_2^2 + \left\| \hat{C}_f(\mathbf{r}) - C(\mathbf{r}) \right\|_2^2 \right] \overset{\mathrm{C}_c}{\underset{\mathsf{C}_f}{=} \text{ Radiance Calculated using coarse points}} \underset{\mathsf{C}_f = \text{ Radiance Calculated using fine points}}{\hat{C}_f = \text{ Radiance Calculated using fine points}} \right]$$





Need: Unbounded Scene

Method: Train two NeRF models, one for foreground, one for background



(a) NeRF++ prediction

(b) predicted foreground

 F_{θ}

(c) predicted background

G_θ



Kai Zhang, Gernot Riegler, Noah Snavely, & Vladlen Koltun (2020). NeRF++: Analyzing and Improving Neural Radiance Fields. arXiv:2010.07492.





$$(x,y,z,\theta,\phi) \longrightarrow F_{\theta} \longrightarrow (R,G,B,\sigma)$$

$$(x,y,z,\theta,\phi,1/r) \longrightarrow G_{\theta} \longrightarrow (R,G,B,\sigma)$$

Background NeRF uses normalised coordinates.



Kai Zhang, Gernot Riegler, Noah Snavely, & Vladlen Koltun (2020). NeRF++: Analyzing and Improving Neural Radiance Fields. arXiv:2010.07492.



- Instant NGP NVLabs
 <u>https://github.com/NVlabs/instant-ngp</u>
- NeRF Studio <u>https://docs.nerf.studio/</u>







Let's go back to some NeRF limitations

- We need more powerful GPUs to complete training
- They take a lot of time to complete training
- They are scene and view dependent





Image source - https://link.springer.com/article/10.1007/s11263-023-01829-3



Image Source https://www.nicehash.com/blog/post/nvidia-rtx-4090-s pecs-and-mining-hashrate



How would you address the limitations ?





What if we remove the neural network from NeRFs?

- How do we learn the 3D information ?
- Data structure for representation
- How to project from 3D to 2D in an efficient way?
- What makes training (optimization) faster ?
- How do we address view dependent effects and colors?





3D Gaussian Splatting



Reconstructed View

Individual Splats

A close up

Viewer -https://github.com/playcanvas/supersplat





3D Gaussian Splatting

- How do we learn the 3D information ?
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Point Clouds using SFM







COLMAP's incremental Structure-from-Motion pipeline.

Source : https://colmap.github.io/tutorial.html#structure-from-motion













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Point Clouds using SFM

Anisotropic Gaussians





- Anisotropic(Elliptical) gaussians are closed for affine transformations.
- A single elliptical gaussian splat can cover a large distance, thus influencing the set of pixels it covers

Parameters:

- Mean μ given by (x,y,z)
- Covariance Matrix Σ
- Opacity *a*
- Color from spherical harmonics (and rgb interchangeably)



Image Source https://towardsdatascience.com/a-comprehensive-overview-of-gaussian-splatting-e 7d570081362





3D -> 2D Gaussian projection.

• From the 2001 EWA Splatting paper, we can project to the image space as follows:

 $\Sigma'=JW\SigmaW^{T}J^{T}$

W - viewing transformation

- EWA paper also shows that upon removing the third row and column of Σ' , we should get a 2x2 covariance matrix with the same properties and structure
- Since covariances only have physical meaning when they are positive and semi definitie : Σ=RSS^TR^T



Image Source https://www.researchgate.net/figure/Ilustration-of-forward-splatting-using-EW A-Zwicker-et-al-2001_fig1_333717475


A more detailed overview of the Math in the previous slide

Alpha Compositing

The RGB value of each pixel is computed by α blending the gaussians from front-to-back. The rgb values of each pixel can be computed with:

$$C(u, v) = \sum_{i=1}^{N} \alpha_i c_i w_i$$
$$w_i = (1 - \sum_{j=0}^{i-1} \alpha_j w_j)$$
$$w_0 = 1$$
$$\alpha_i = o_i g_i(u, v)$$

Where c_i and o_i are the color and opacity of the i^{th} gaussian and $g_i(u, v)$ is the probability of the i^{th} gaussian at the pixel coordinates u, v.





Differentiable volumetric representation Unstructured and explicit to allow fast rendering



Why 3D anisotropic gaussians ? (Part 2)





Image Source - 3D Gaussian Splatting for Real-Time Radiance Field Rendering



3D Gaussian Splatting

- How do we learn the 3D information ? Point Clouds using SFM
- Data structure for representation
- How to project from 3D to 2D in an efficient way ?
 Anisotropic Gaussians
- What makes training (optimization) faster? Tile Rasterizer
- How do we address view dependent effects and colors?





3D Gaussian Splatting

- How do we learn the 3D information ?
- What is the data structure for representation?
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Point Clouds using SFM

Anisotropic Gaussians Tile Rasterizer







Chen, Guikun, and Wenguan Wang. "A Survey on 3D Gaussian Splatting." arXiv preprint arXiv:2401.03890 (2024).





- Gaussians are culled against the view frustum and each independent tile, only retaining 99% confidence rendering task
- Guard bands surrounding each tile is used to reject gaussians at extreme positions.





Differentiable Tile Rasterizer



$$\alpha'_n = \alpha_n \times \exp\left(-\frac{1}{2}(\boldsymbol{x}' - \boldsymbol{\mu}'_n)^\top \boldsymbol{\Sigma}_n^{\prime-1}(\boldsymbol{x}' - \boldsymbol{\mu}'_n)\right),$$

X represents the position of a pixel on the screen , α represents the learned opacity and C represents the color at each pixel and c represents the learnt color



 $C = \sum_{n=1}^{|\mathcal{N}|} c_n \alpha'_n \prod_{i=1}^{n-1} (1 - \alpha'_i),$

Chen, Guikun, and Wenguan Wang. "A Survey on 3D Gaussian Splatting." arXiv preprint arXiv:2401.03890 (2024).







Image Source - https://medium.com/@soyoungpark.psy/lets-crack-3d-gaussian-splatting-in-5mins-5777a7b735eb





Image Source - 3D Gaussian Splatting for Real-Time Radiance Field Rendering



DR Overall Optimization Algorithm

```
Algorithm 1 Optimization and Densification
w, h: width and height of the training images
  M \leftarrow \text{SfM Points}
                                                                  ▶ Positions
  S, C, A \leftarrow \text{InitAttributes}()
                                        ▶ Covariances, Colors, Opacities
  i \leftarrow 0
                                                           ▶ Iteration Count
  while not converged do
       V, \hat{I} \leftarrow \text{SampleTrainingView}()
                                                   \triangleright Camera V and Image
       I \leftarrow \text{Rasterize}(M, S, C, A, V)
                                                                      ▶ Alg. 2
       L \leftarrow Loss(I, \hat{I})
                                                                        ▶ Loss
       M, S, C, A \leftarrow \operatorname{Adam}(\nabla L)
                                                         ▶ Backprop & Step
       if IsRefinementIteration(i) then
                                                                                 Algorithm Source - 3D Gaussian Splatting for Real-Time
           for all Gaussians (\mu, \Sigma, c, \alpha) in (M, S, C, A) do
                                                                   ▶ Pruning Radiance Field Rendering
                if \alpha < \epsilon or IsTooLarge(\mu, \Sigma) then
                    RemoveGaussian()
                end if
                                                             ▶ Densification
               if \nabla_p L > \tau_p then
                    if ||S|| > \tau_S then
                                                    ▶ Over-reconstruction
                        SplitGaussian(\mu, \Sigma, c, \alpha)
                    else
                                                   ▶ Under-reconstruction
                        CloneGaussian(\mu, \Sigma, c, \alpha)
                    end if
               end if
           end for
       end if
       i \leftarrow i + 1
  end while
```





Algorithm 2 GPU software rasterization of 3D Gaussians

w, *h*: width and height of the image to rasterize

M, *S*: Gaussian means and covariances in world space

C, *A*: Gaussian colors and opacities

V: view configuration of current camera

```
function RASTERIZE(w, h, M, S, C, A, V)
    CullGaussian(p, V)
                                                      ▶ Frustum Culling
    M', S' \leftarrow \text{ScreenspaceGaussians}(M, S, V)
                                                             ▶ Transform
    T \leftarrow \text{CreateTiles}(w, h)
    L, K \leftarrow \text{DuplicateWithKeys}(M', T)
                                                      Indices and Keys
                                                          ▶ Globally Sort
    SortByKeys(K, L)
    R \leftarrow \text{IdentifyTileRanges}(T, K)
    I \leftarrow 0
                                                            Init Canvas
    for all Tiles t in I do
        for all Pixels i in t do
             r \leftarrow \text{GetTileRange}(R, t)
            I[i] \leftarrow \text{BlendInOrder}(i, L, r, K, M', S', C, A)
        end for
    end for
     return I
end function
```

Algorithm Source - 3D Gaussian Splatting for Real-Time Radiance Field Rendering





3D Gaussian Splatting

- How do we learn the 3D information ?
- What is the data structure for representation?
- How to project from 3D to 2D in an efficient way?
- What makes training (optimization) faster ?
- How do we address view dependent effects and colors? Spherical Harmonics

Point Clouds using SFM

Anisotropic Gaussians Tile Rasterizer







Image Source :https://www.physicsforums.com/threads/what-do-the-color-maps-in-spherical-harmonics-represent.805216/





How is SH calculated by the 3Dgs code ?

22		Spherical Harmonic Lighting					
Equation 10. Cartesian version of the first few real SH functions.		<i>m</i> = -2	m = -1	m = 0	m = 1	<i>m</i> = 2	
	l = 0			$\frac{1}{2}\sqrt{\frac{1}{\pi}}$			
	<i>l</i> = 1		$\frac{1}{2}\sqrt{\frac{3}{\pi}}\frac{y}{r}$	$\frac{1}{2}\sqrt{\frac{3}{\pi}}\frac{z}{r}$	$\frac{1}{2}\sqrt{\frac{3}{\pi}}\frac{x}{r}$		
	<i>l</i> = 2	$\frac{1}{2}\sqrt{\frac{15}{\pi}}\frac{yx}{r^2}$	$\frac{1}{2}\sqrt{\frac{15}{\pi}}\frac{yz}{r^2}$	$\frac{1}{4}\sqrt{\frac{5}{\pi}}\frac{2z^2 - x^2 - y^2}{r^2}$	$\frac{1}{2}\sqrt{\frac{15}{\pi}}\frac{zx}{r^2}$	$\frac{1}{2}\sqrt{\frac{15}{\pi}}\frac{x^2-y^2}{r^2}$	

where

$$r = \sqrt{x^2 + y^2 + z^2}$$
 (n.b. usually $r = 1$)

Source : Spherical Harmonic Lighting: The Gritty Details

The source code for computing color from SH can be found<u>here</u> and the general data structure for SH seems to be arrays after a brief overview of the code.



B Spherical Harmonics Comparisons



Oth Degree(Band)



1st Degree(Band)



Images generated using 0 band SH should have uniform light representation in all direction, as the number of SH bands increase, the ability to handle different lighting from different directions increases. The image on the right should be a bit sharper and more representative of the actual image.



3D Gaussian Splatting

- How do we learn the 3D information ? Point Clouds using SFM
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- What makes training (optimization) faster? Tile Rasterizer
- How do we address view dependent effects and colors? Spherical Harmonics





3D Gaussian Splatting

- How do we learn the 3D information?
- What is the data structure for representation?
- How to project from 3D to 2D in an efficient way?
- What makes training (optimization) faster?
 - Tile Rasterizer

How do we address view dependent effects and colors? Spherical Harmonics

Point Clouds using SFM

Anisotropic Gaussians







Image Source - 3D Gaussian Splatting for Real-Time Radiance Field Rendering





Optimization Methodologies

- Makes use of stochastic gradient descent for optimization
- Sigmoid activation function to constrain α between [0,1) and obtain smooth gradients
- Loss is defined by -

$$\mathcal{L} = (1 - \lambda)\mathcal{L}_1 + \lambda \mathcal{L}_{\text{D-SSIM}}$$





 3DGS is significantly faster than NeRFs for both training and rendering purposes, although the memory it uses might be a relatively high as show in the table.







- Sparse Point Cloud Dependency
- Static nature
- Floaters and other inherited artifacts





Progress and Developments in Gaussian Splatting Since the Seminal 2022 Paper

- Using sparse images
- Memory efficiency
- Photorealism(Raytracing)
- 3DGS with structured information
- Dynamic Scenes
- Moving away from colmap and many more





Where do I introduce NeRF and Gaussian Splatting tin Robotics?

How is NeRF and Gaussian Splatting used for manipulation tasks?







Mildenhall, B., Srinivasan, P. P., Tancik, M., Barron, J. T., Ramamoorthi, R., & Ng, R. (2021). Nerf: Representing scenes as neural radiance fields for view synthesis. *Communications of the ACM*, 65(1), 99-106.



- NeRF's and Gaussian Splats are able to get a better grasp of the scene's 3D information.
- Recent advancements in gaussian splatting have enabled semantic segmentation of individual objects in the 3D scene.
- The ability to retain structure hidden within the input information distinguishes both NeRF and Gaussian Splatting from traditional vision input processing techniques.
- A key real world problem that is being tackled right now with both NeRF and Gaussian Splatting is **overcoming the Sim2Real gap.**





NeRF in Robotics

Fig. 1. A taxonomy of NeRF in robotics.



Wang, G., Pan, L., Peng, S., Liu, S., Xu, C., Miao, Y., ... & Wang, H. (2024). NeRF in Robotics: A Survey. arXiv preprint arXiv:2405.01333.







Wang, G., Pan, L., Peng, S., Liu, S., Xu, C., Miao, Y., ... & Wang, H. (2024). NeRF in Robotics: A Survey. arXiv preprint arXiv:2405.01333.























Fig. 1. A taxonomy of NeRF in robotics.











Coming Up : NeRF2Real





Coming Up : NeRF2Real

NeRF2Real is framework developed by DeepMind to incorporate the advantages of NeRF in creating vision processing models for robust applications







Byravan, A., Humplik, J., Hasenclever, L., Brussee, A., Nori, F., Haarnoja, T., ... & Heess, N. (2023, May). Nerf2real: Sim2real transfer of vision-guided bipedal motion skills using neural radiance fields. In 2023 IEEE International Conference on Robotics and Automation (ICRA) (pp. 9362-9369). IEEE.





Fig. 2: Overview of our system for recreating a scene in a simulator. **A.** We collect a video of the scene using a generic phone. **B.** We use structure-from-motion software to label a subset of the video with camera poses. **C.** We train a NeRF on these labeled images. **D.** We render the scene from novel views using the calibrated intrinsics of the robot's head-mounted camera. **E.** We use the same NeRF to extract the scene geometry as a mesh. We coarsen the mesh and replace the floor with a flat primitive. **F.** We combine the simplified mesh with a model of a robot, and any other dynamic objects, in a physics simulator. See Fig. 3 for further details on this step.



Byravan, A., Humplik, J., Hasenclever, L., Brussee, A., Nori, F., Haarnoja, T., ... & Heess, N. (2023, May). Nerf2real: Sim2real transfer of vision-guided bipedal motion skills using neural radiance fields. In 2023 IEEE International Conference on Robotics and Automation (ICRA) (pp. 9362-9369). IEEE.




Fig. 4: The policy's network architecture.



Byravan, A., Humplik, J., Hasenclever, L., Brussee, A., Nori, F., Haarnoja, T., ... & Heess, N. (2023, May). Nerf2real: Sim2real transfer of vision-guided bipedal motion skills using neural radiance fields. In 2023 IEEE International Conference on Robotics and Automation (ICRA) (pp. 9362-9369). IEEE. Architecture is inspired from the paper referenced below Müller, T., Evans, A., Schied, C., & Keller, A. (2022). Instant neural graphics primitives with a multiresolution hash encoding. ACM transactions on graphics (TOG), 41(4), 1-15.





Fig. 3: Our MuJoCo simulation is created by combining: (1) the learnt static scene mesh (Section III-E), (2) the dynamic object meshes and (3) the learnt static scene NeRF rendering (Section III-D) on which (4) the Mujoco rendering of dynamic objects (a ball and robot's left arm in the camera image above) are overlaid. Other dynamic parameters (e.g. friction) are assumed known or measured.



Byravan, A., Humplik, J., Hasenclever, L., Brussee, A., Nori, F., Haarnoja, T., ... & Heess, N. (2023, May). Nerf2real: Sim2real transfer of vision-guided bipedal motion skills using neural radiance fields. In 2023 IEEE International Conference on Robotics and Automation (ICRA) (pp. 9362-9369). IEEE.

RL Training algorithm used is explained in the paper below

Osa, T., Hayashi, A., Deo, P., Morihira, N., & Yoshiike, T. (2023). Offline reinforcement learning with mixture of deterministic policies. Transactions on Machine Learning Research.



Coming Up : SplatSim





Coming Up : SplatSim

SplatSim is a very recent development, of bringing Gaussian Splatting of plain RGB Images to create high quality simulated renders to reduce the sim2Real gap in manipulation.





Gaussian Splatting in Robotics: Splat-Sim



Qureshi, M. N., Garg, S., Yandun, F., Held, D., Kantor, G., & Silwal, A. (2024). Splatsim: Zero-shot sim2real transfer of rgb manipulation policies using gaussian splatting. arXiv preprint arXiv:2409.10161.

R Gaussian Splatting in Robotics: Splat-Sim





3. Given our Splat Model, it is important to align the Gaussian Splat with the real world robot links. Please see the next slide to understand this process



Qureshi, M. N., Garg, S., Yandun, F., Held, D., Kantor, G., & Silwal, A. (2024). Splatsim: Zero-shot sim2real transfer of rgb manipulation policies using gaussian splatting. *arXiv preprint arXiv:2409.10161*.







Qureshi, M. N., Garg, S., Yandun, F., Held, D., Kantor, G., & Silwal, A. (2024). Splatsim: Zero-shot sim2real transfer of rgb manipulation policies using gaussian splatting. arXiv preprint arXiv:2409.10161.





Fig. 4: We use a KNN-based classifier for segmenting links for articulated objects like parallel jaw grippers. We train a KNN model with the ground truth point labeling from the URDF model of the end effector.



R Gaussian Splatting in Robotics: Splat-Sim







Qureshi, M. N., Garg, S., Yandun, F., Held, D., Kantor, G., & Silwal, A. (2024). Splatsim: Zero-shot sim2real transfer of rgb manipulation policies using gaussian splatting. *arXiv preprint arXiv:2409.10161*. Diffusion Policy Paper referenced is

Chi, C., Xu, Z., Feng, S., Cousineau, E., Du, Y., Burchfiel, B., ... & Song, S. (2023). Diffusion policy: Visuomotor policy learning via action diffusion. The International Journal of Robotics Research, 02783649241273668.



Next Lecture: Student Lecture 4 Deformable Object Manipulation





DeepRob [Group 2] Lecture 3 by Harshavardhan, Raj Surya, Vaibhav NeRFs, Gaussian Splatting and Manipulation University of Minnesota



