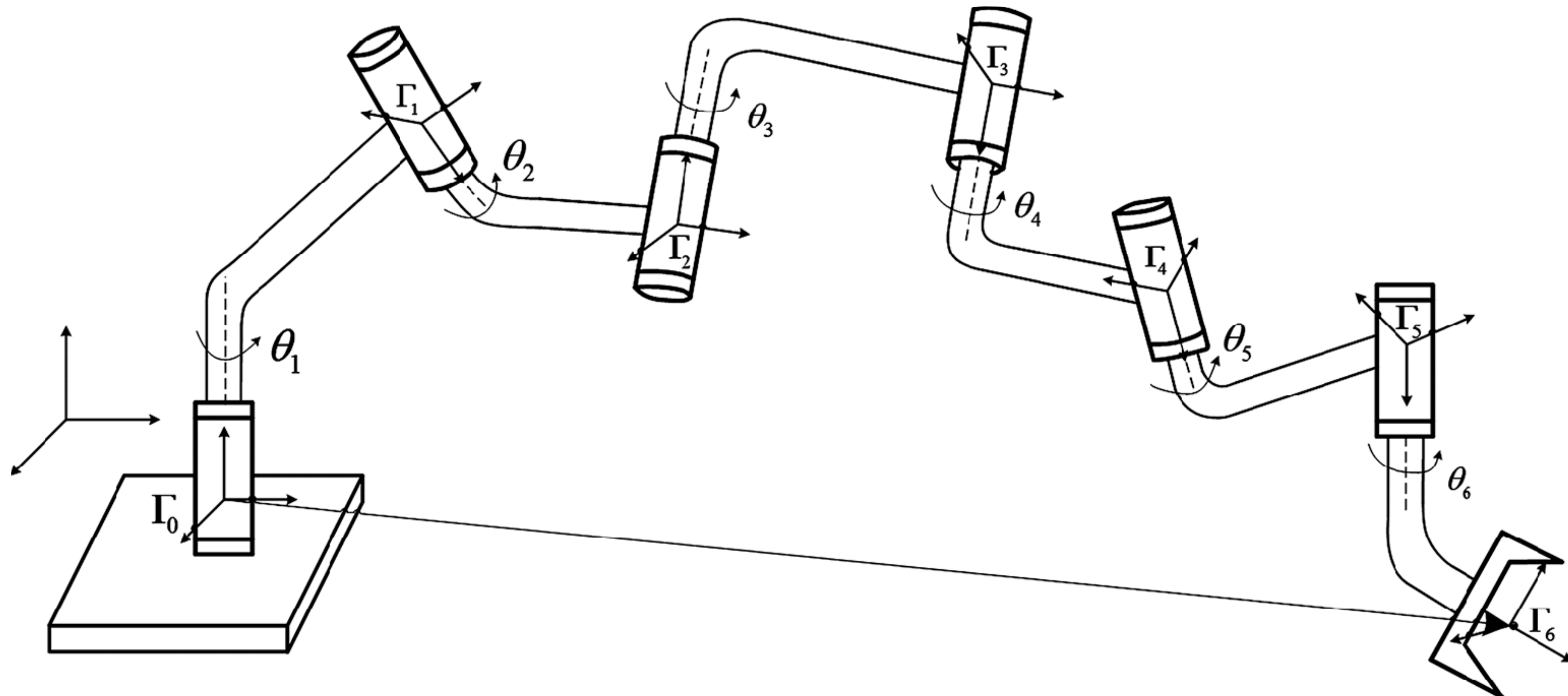


Lecture 06

Manipulation - I

Forward Kinematics & Decision Making



Course Logistics

- Project 2 was posted on 01/31 and will be due **on Wed 02/07.**
- Quiz 3 will be posted tomorrow at 6 pm and will be due on Wed noon.
- Project 3 will be released on 02/07 and will be due on 02/14.
- Note: 3 Late Day Tokens are for the entire semester for P1-P6.
 - If you used 1 late token for P1, then you have 2 more for P2-P6.
 - If you used all 3 late tokens for P1, then you have no more late tokens left.
 - After the late tokens and due date, you will have to ask Chahyon Ku (TA) to submit, so we can consider the late submission with 25% penalty per day.
 - Feel free to talk to Karthik during his OH if you have any questions about this.



FAQs on P2

What to do in kineval/kineval_robot_init_joints.js?

```
12 kineval.initRobotJoints = function initRobotJoints() {
13   // build kinematic hierarchy by looping over each joint in the robot
14   // (object fields can be index through array-style indices, object[field] = property)
15   // and insert threejs scene graph (each joint and link are directly connect to scene root)
16   // NOTE: kinematic hierarchy is maintained independently by this code, not threejs
17
18   var x,tempmat;
19
20   for (x in robot.joints) {
21
22     // give the joint its name as an id
23     robot.joints[x].name = x;
24
25     // initialize joint angle value and control input value
26     robot.joints[x].angle = 0;
27     robot.joints[x].control = 0;
28     robot.joints[x].servo = {};
29     //set appropriate servo gains for arm setpoint control
30     robot.joints[x].servo.p_gain = 0.1;
31     robot.joints[x].servo.p_desired = 0;
32     robot.joints[x].servo.d_gain = 0.01;
33   /* STENCIL START */
34   // STENCIL: complete kinematic hierarchy of robot for convenience.
35   // robot description only specifies parent and child links for joints.
36   // additionally specify parent and CHILDREN joints for each link
37
38
39
40
41
42
43
44
45   /* STENCIL END */
46
47   }
```

robots/robot_mr2.js given to you has this information

```
54 // specify and create data objects for the joints of the robot
55 robot.joints = {};
56
57 robot.joints.clavicle_right_yaw = {parent:"base", child:"clavicle_right"};
58 robot.joints.clavicle_right_yaw.origin = {xyz: [0.3,0.4,0.0], rpy:[-Math.PI/2,0,0]};
59 robot.joints.clavicle_right_yaw.axis = [0.0,0.0,-1.0];
60
61 robot.joints.shoulder_right_yaw = {parent:"clavicle_right", child:"shoulder_right"};
62 robot.joints.shoulder_right_yaw.origin = {xyz: [0.0,-0.15,0.85], rpy:[Math.PI/2,0,0]};
63 robot.joints.shoulder_right_yaw.axis = [0.0,0.707,0.707];
64
65 robot.joints.upperarm_right_pitch = {parent:"shoulder_right", child:"upperarm_right"};
66 robot.joints.upperarm_right_pitch.origin = {xyz: [0.0,0.0,0.7], rpy:[0,0,0]};
67 robot.joints.upperarm_right_pitch.axis = [0.0,1.0,0.0];
68
69 robot.joints.forearm_right_yaw = {parent:"upperarm_right", child:"forearm_right"};
70 robot.joints.forearm_right_yaw.origin = {xyz: [0.0,0.0,0.7], rpy:[0,0,0]};
71 robot.joints.forearm_right_yaw.axis = [1.0,0.0,0.0];
72
73 robot.joints.clavicle_left_roll = {parent:"base", child:"clavicle_left"};
74 robot.joints.clavicle_left_roll.origin = {xyz: [-0.3,0.4,0.0], rpy:[-Math.PI/2,0,0]};
75 robot.joints.clavicle_left_roll.axis = [0.0,0.0,1.0];
76
77 // specify name of endeffector frame
78 robot.endeffector = {};
79 robot.endeffector.frame = "forearm_right_yaw";
80 robot.endeffector.position = [[0],[0],[0.5],[1]]
81
```

So we are asking you to populate the

- child (joint if any) of every link
- parent (joint) of every link

FAQs on P2

How do I go about `kineval/kineval_forward_kinematics.js`?

1 Answer



Chahyon Ku **STAFF**
2 days ago



You only need functions from `kineval_matrix.js` at this point.

2

The suggested structure is:

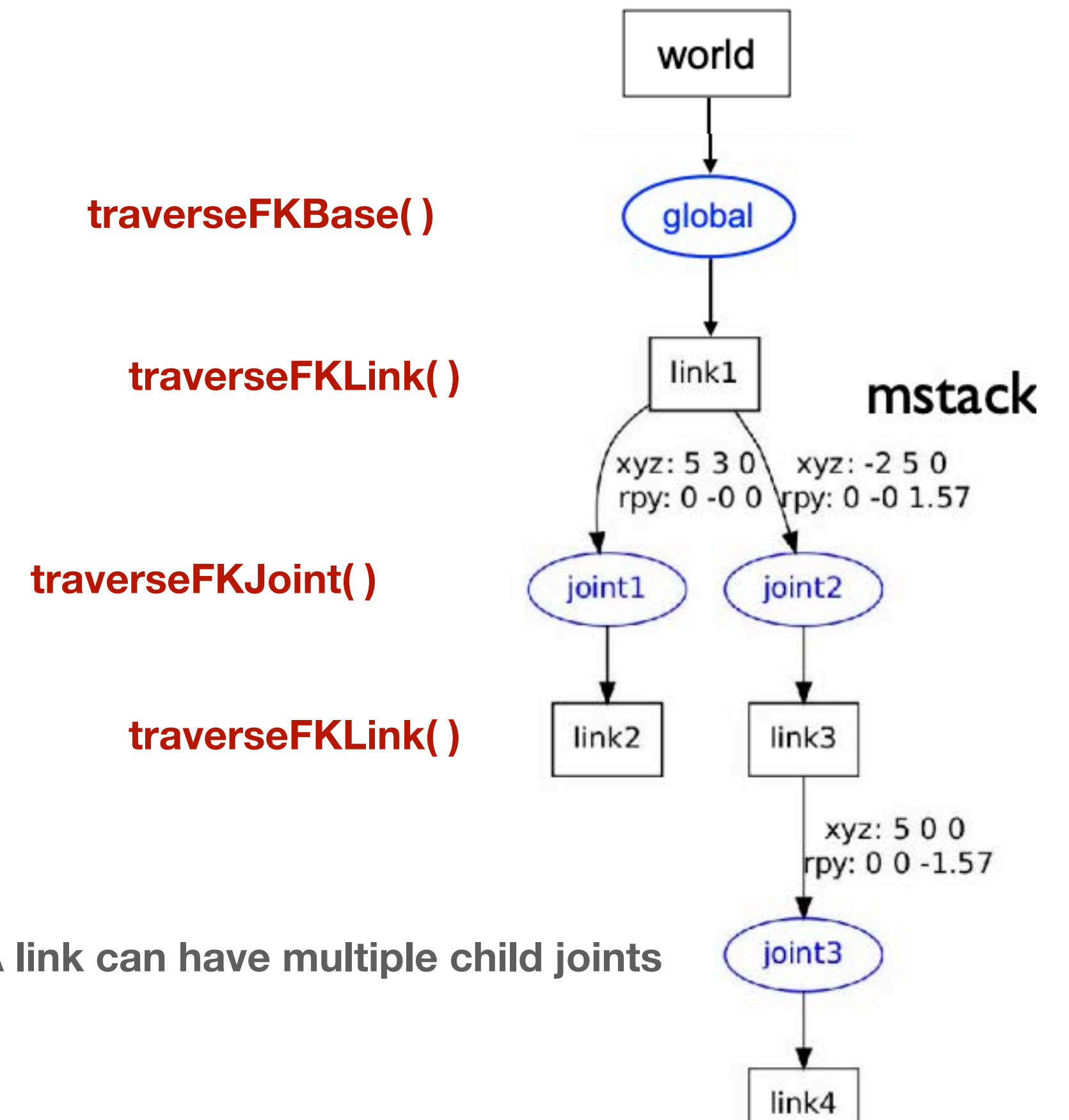


1. `kineval.robotForwardKinematics()` calls `kineval.buildFKTransforms()`
2. `kineval.buildFKTransforms()` calls `traverseFKBase()`
3. `traverseFKBase()` calls `traverseFKLink()`
4. `traverseFKLink()` calls `traverseFKJoint()`
5. `traverseFKJoint()` calls `traverseFKLink()`

, traversing the kinematic tree in depth-first order from root (base) to leaves (links with no children).

Feel free to make your question public as it doesn't include your code :)

Comment Edit Delete Unendorse ...



Note: A link can have multiple child joints

FAQs on P2

How do I go about other robots (fetch, sawyer, baxter, etc)?

Project Page Instructions:

- ROS uses a different default coordinate system than threejs, which needs to be taken into account in the FK computation for these three robots. ROS assumes that the Z, X, and Y axes correspond to the up, forward, and side directions, respectively. In contrast, threejs assumes that the Y, Z, and X axes correspond to the up, forward, and side directions. The variable `robot.links_geom_imported` will be set to true when geometries have been imported from ROS and set to false when geometries are defined completely within the robot description file. You will need to extend your FK implementation to compensate for the coordinate frame difference when this variable is set to true.
- You can test and debug your implementation by opening `home.html` with parameters attached to the back such as `?robot=robots/robot_mr2.js ?robot=robots/robot_crawler.js ?robot=robots/robot_urdf_example.js robots/fetch/fetch.urdf.js ?robot=robots/sawyer/sawyer.urdf.js ?robot=robots/baxter/baxter.urdf.js`. Your implementation should look like this:

Check for the variable `robot.links_geom_imported` in side your `traverseFKBase()`

Ed Discussion Project 2 Tips:

3. As ROS -> threejs changes the front/left/up direction of the axes, it directly affects only the transform of the base link and indirectly (through chained multiplication) affects all descendant joints and links. You should not change the order of multiplications and only apply the matrix on the base transform! The matrix for Y, Z, X (threejs) -> Z, X, Y (ROS) can be verified in the following way:

$$\begin{bmatrix} 0 \\ 1 \\ 0 \\ 1 \end{bmatrix} = R \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \end{bmatrix} = R \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} = R \begin{bmatrix} 0 \\ 1 \\ 0 \\ 1 \end{bmatrix}$$

Each representing Y -> Z, Z -> X, and X -> Y conversions.

If `robot.links_geom_imported` is true (For Fetch, Sawyer and Baxter), then multiple the Global Transform from robot base to the world, with additional one on the right that maps ROS to ThreeJs.

$$T_{robot_base}^{world} \longrightarrow T_{robot_base}^{world} T_{ROS}^{robot_base}$$



Please check Ed before coming to
the course staff in the OH!



Previously

Axis field specifies DOF axis of motion with respect to parent frame

Can we translate about an axis?

Can we rotate about an axis? Quaternions!

```

<robot name="test_robot">
  <link name="link1" />
  <link name="link2" />
  <link name="link3" />
  <link name="link4" />

  <joint name="joint1" type="continuous">
    <parent link="link1"/>
    <child link="link2"/>
    <origin xyz="5 3 0" rpy="0 0 0" />
    <axis xyz="0.9 0.15 0" />
  </joint>

  <joint name="joint2" type="continuous">
    <parent link="link1"/>
    <child link="link3"/>
    <origin xyz="-2 5 0" rpy="0 0 1.57" />
    <axis xyz="0.707 0.707 0" />
  </joint>

  <joint name="joint3" type="continuous">
    <parent link="link3"/>
    <child link="link4"/>
    <origin xyz="5 0 0" rpy="0 0 -1.57" />
    <axis xyz="0.707 -0.707 0" />
  </joint>
</robot>

```

```

// roll-pitch-yaw defined by ROS as corresponding to x-y-z
//http://wiki.ros.org/urdf/Tutorials/Creating%20your%20own%20urdf
robots/robot_urdf_example.js

// specify and create data objects for the joints of the robot
robot.joints = {};

robot.joints.joint1 = (parent:"link1", child:"link2");
robot.joints.joint1.origin = {xyz: [0.5,0.5,0], rpy:[0,0,0]};
robot.joints.joint1.axis = [-1.0,0.0,0]; // simpler axis

robot.joints.joint2 = (parent:"link1", child:"link3");
robot.joints.joint2.origin = {xyz: [-0.2,0.5,0], rpy:[0,0,0]};
robot.joints.joint2.axis = [-0.707,0.707,0];

robot.joints.joint3 = (parent:"link3", child:"link4");
robot.joints.joint3.origin = {xyz: [0.5,0,0], rpy:[0,0,0]};
robot.joints.joint3.axis = [0.707,-0.707,0];

```

joint specifies

- "parent" and "child" links
- Transform parameters for joint wrt. link frame
 - "xyz": T(x,y,z)
 - "rpy": R_x(roll), R_y(pitch), R_z(yaw)
- joint "axis" of motion for DOF
- "type" of joint motion for DOF state "angle"
 - "continuous" for rotation without limits
 - "revolute" for rotation within limits
 - "prismatic" for translation within limits

translation on unit joint axis u_1 scaled by joint state q_1

// transform of joint wrt. world
robot.joints["joint1"].xform = //this matrix

joint2 is revolute

rotation about unit joint axis u_2 by joint state q_2

// joint motor rotation axis
robot.joints["joint2"].axis = [0.707,0.0, 0.707]

Θ_2

Rotation by Quaternion

- Rotations are represented by unit quaternions
 - quaternion is point on 4D unit sphere geometrically
- Quaternion $q = (a, \mathbf{u}) = a + b\mathbf{i} + c\mathbf{j} + d\mathbf{k} = (\cos(\Theta/2), \mathbf{u} \sin(\Theta/2))$
 $= [\cos(\Theta/2), u_x \sin(\Theta/2), u_y \sin(\Theta/2), u_z \sin(\Theta/2)]$
- $\mathbf{u} = [u_x, u_y, u_z]$ is rotation axis, Θ rotation angle
- Rotating a 3D point \mathbf{p} by unit quaternion \mathbf{q} is performed by conjugation of \mathbf{v} by \mathbf{q}
 - $\mathbf{v}' = \mathbf{q}\mathbf{v}\mathbf{q}^{-1}$, where $\mathbf{q}^{-1} = a - \mathbf{u}$,
 - quaternion \mathbf{v} is constructed from point \mathbf{p} as $\mathbf{v} = 0 + \mathbf{p} = 0 + p_x\mathbf{i} + p_y\mathbf{j} + p_z\mathbf{k}$
 - rotated point $\mathbf{p}' = [\mathbf{v}'_x \mathbf{v}'_y \mathbf{v}'_z]$ is pulled from quaternion resulting from conjugation

- 1) form unit quaternion from axis and motor angle
 $q = [\cos(\Theta/2), u_x \sin(\Theta/2), u_y \sin(\Theta/2), u_z \sin(\Theta/2)]$
- 2) convert quaternion to rotation matrix
 - Inhomogeneous conversion to 3D rotation matrix of $q = [q_0 \ q_1 \ q_2 \ q_3]^T$

$$\begin{bmatrix} 1 - 2(q_2^2 + q_3^2) & 2(q_1q_2 - q_0q_3) & 2(q_0q_2 + q_1q_3) \\ 2(q_1q_2 + q_0q_3) & 1 - 2(q_1^2 + q_3^2) & 2(q_2q_3 - q_0q_1) \\ 2(q_1q_3 - q_0q_2) & 2(q_0q_1 + q_2q_3) & 1 - 2(q_1^2 + q_2^2) \end{bmatrix}$$
 - or equivalently, homogeneous conversion

$$\begin{bmatrix} q_0^2 + q_1^2 - q_2^2 - q_3^2 & 2(q_1q_2 - q_0q_3) & 2(q_0q_2 + q_1q_3) \\ 2(q_1q_2 + q_0q_3) & q_0^2 - q_1^2 + q_2^2 - q_3^2 & 2(q_2q_3 - q_0q_1) \\ 2(q_1q_3 - q_0q_2) & 2(q_0q_1 + q_2q_3) & q_0^2 - q_1^2 - q_2^2 + q_3^2 \end{bmatrix}$$
 - Rotation matrix to quaternion can also be performed

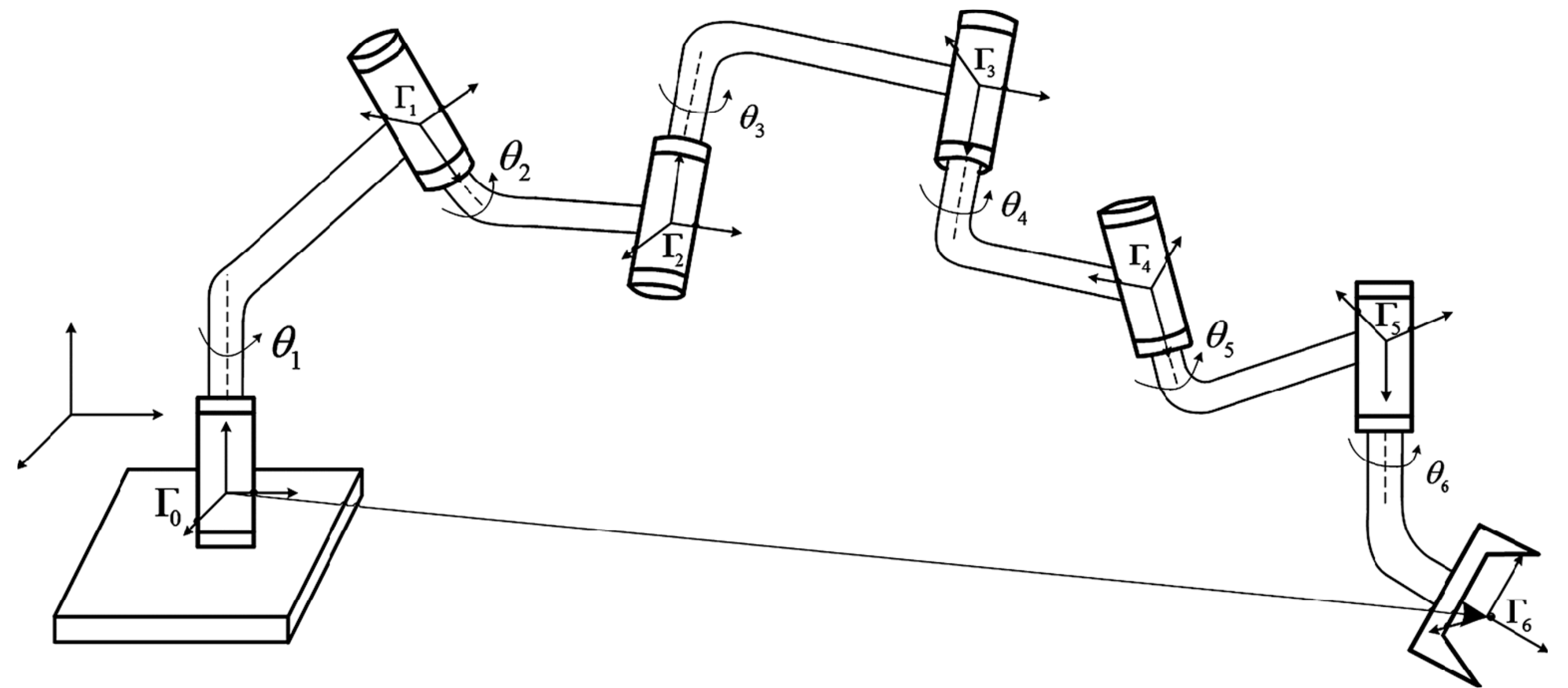
$D_{w_1} * R_{w_1} * D_{l_1}^3 * R_{l_1}^2 * R_{u_2}(q_2) * D_{l_2}^3 * R_{l_2}^2 * R_{u_3}(q_3)$

$D_{w_1} * R_{w_1}$

Robot Kinematics

Goal: Given the structure of a robot arm, compute

- **Forward kinematics:** infer the pose of the end-effector, given the state of each joint.
- **Inverse kinematics:** infer the joint states to reach a desired end-effector pose.



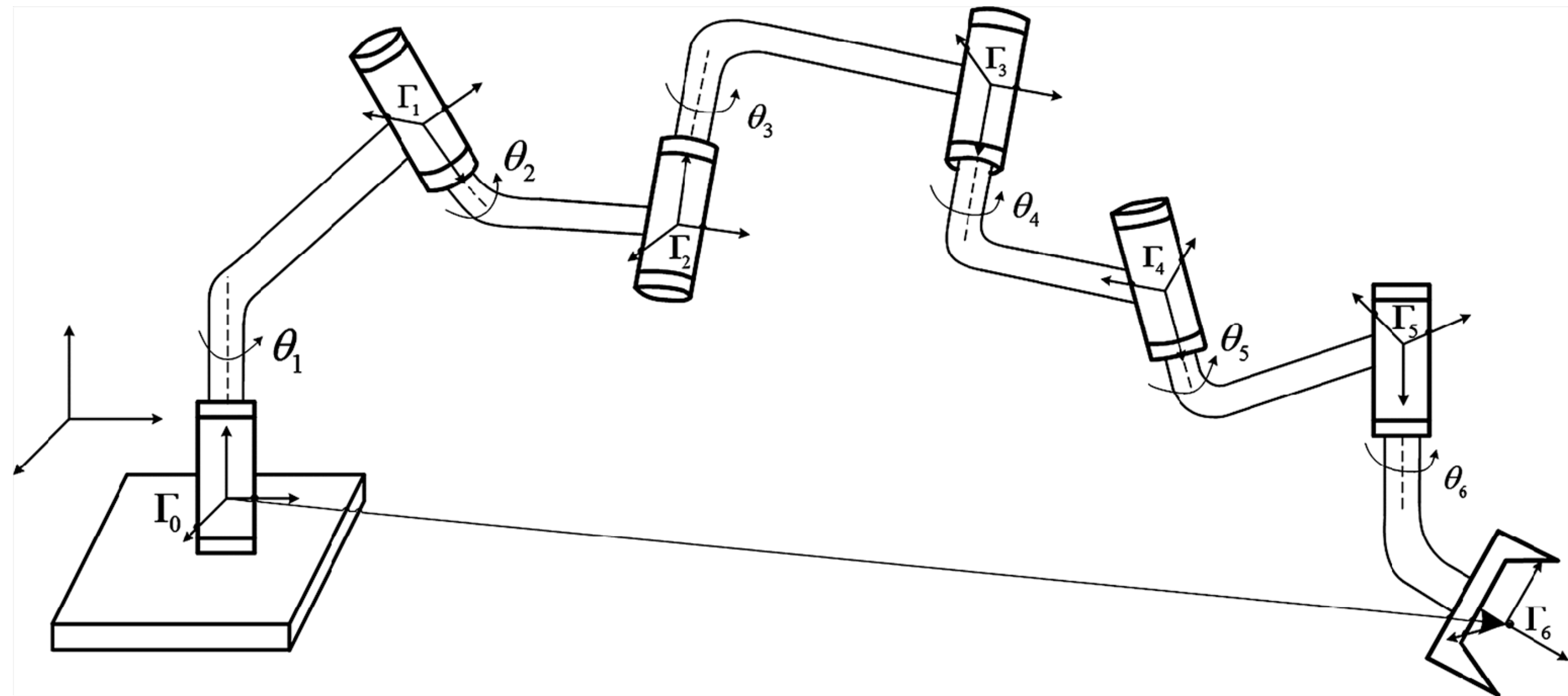
Robot Kinematics

– **Forward kinematics:** infer the pose of the end-effector, given the state of each joint.

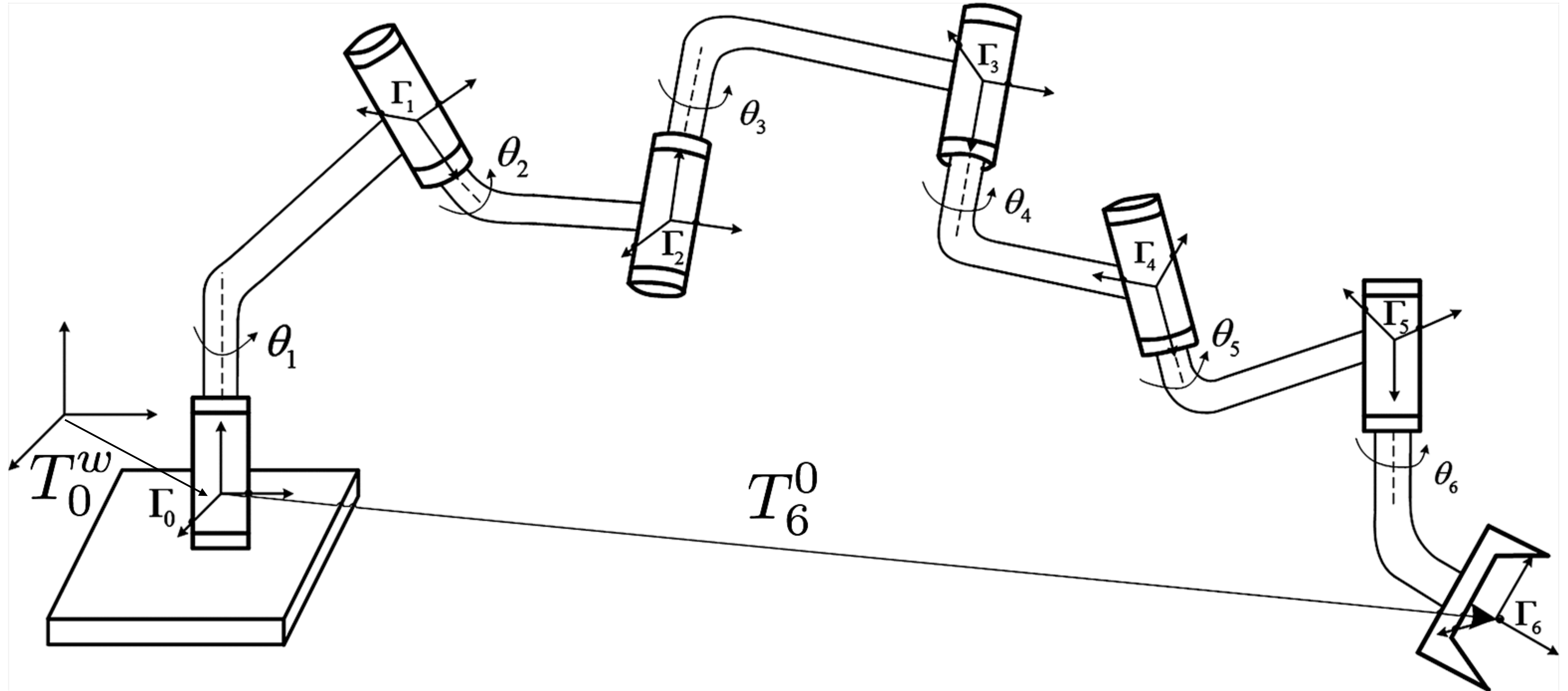
Infer: pose of each joint and link in a common world workspace

Assuming as given the:

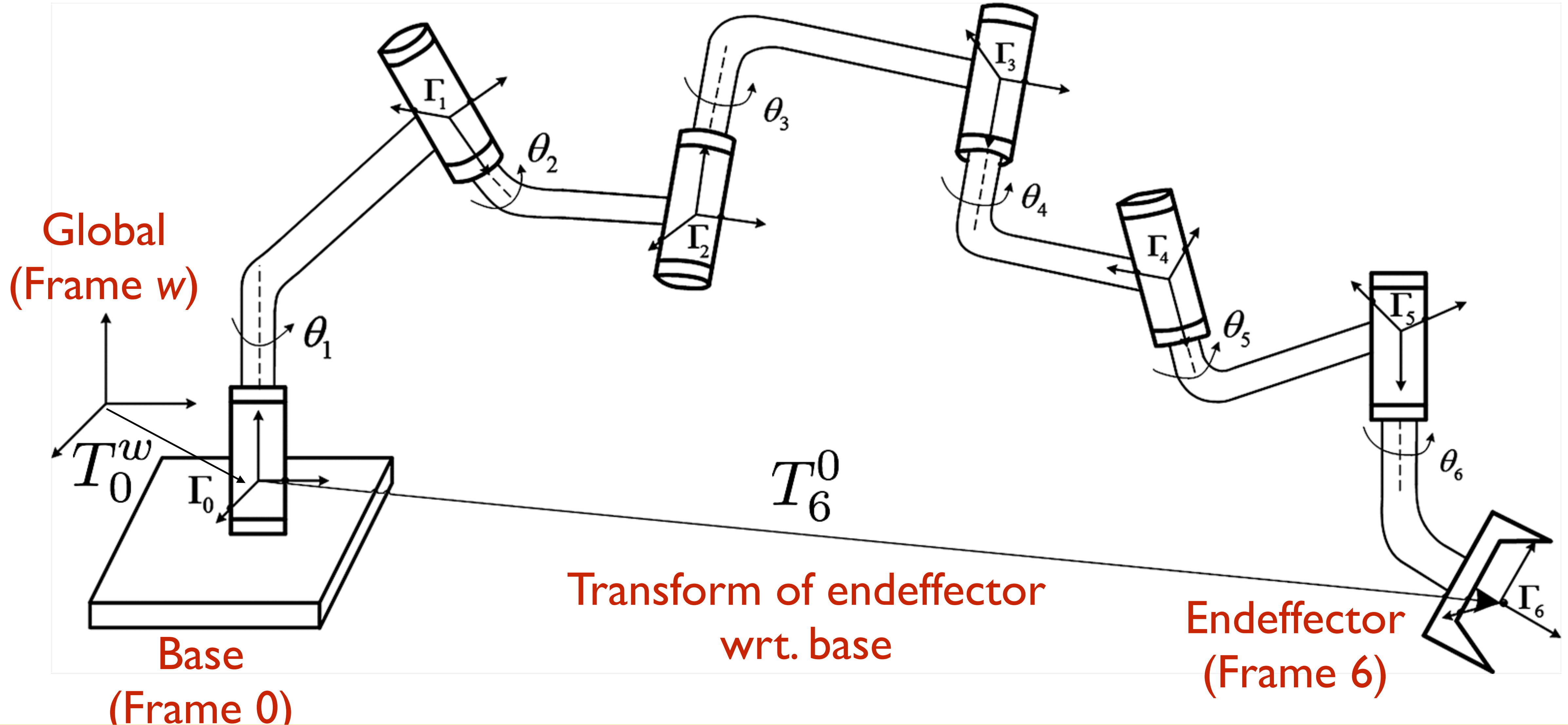
- robot's kinematic definition
- geometry of each link
- current state of all joints
 - zero configuration
 - add motor motion



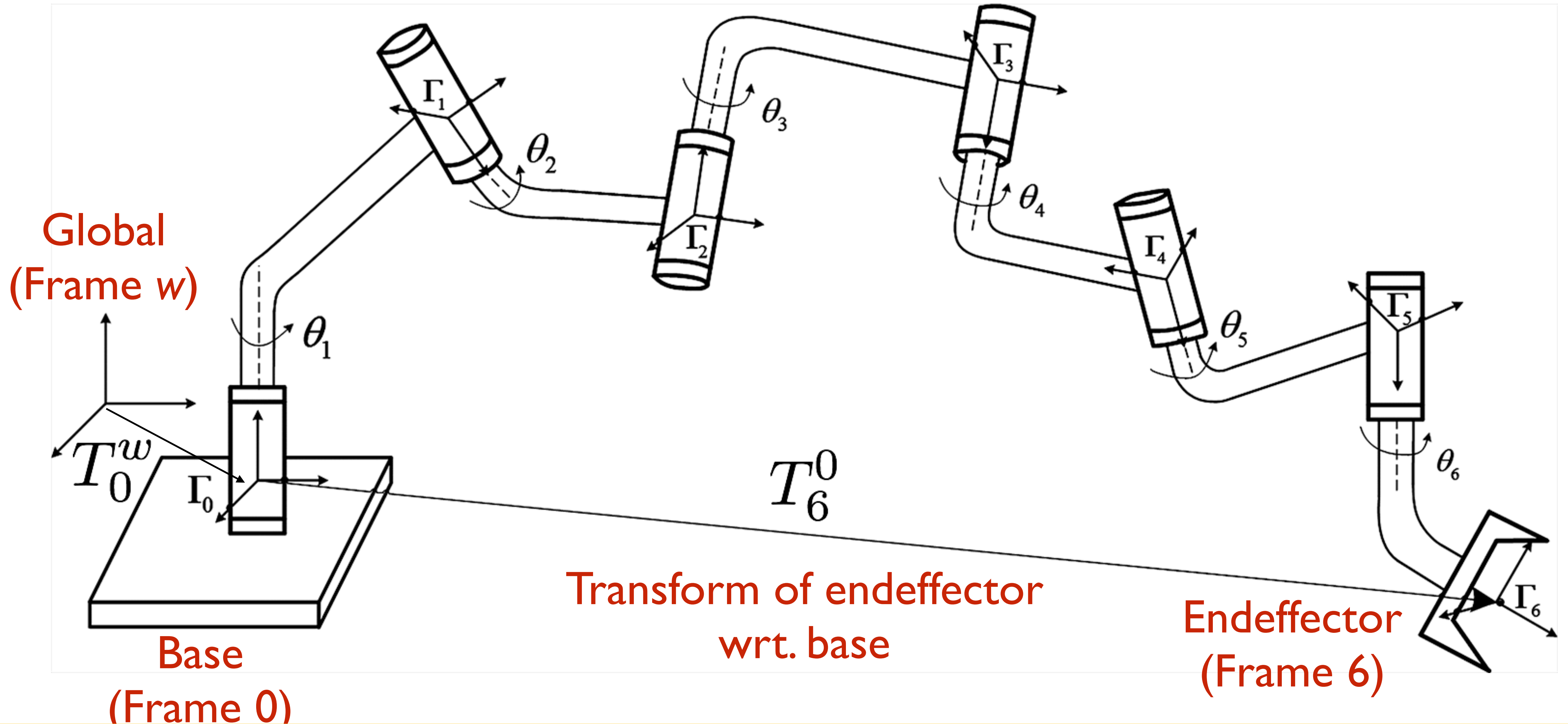
Forward kinematics: many-to-one mapping of robot configuration to reachable workspace endeffector poses



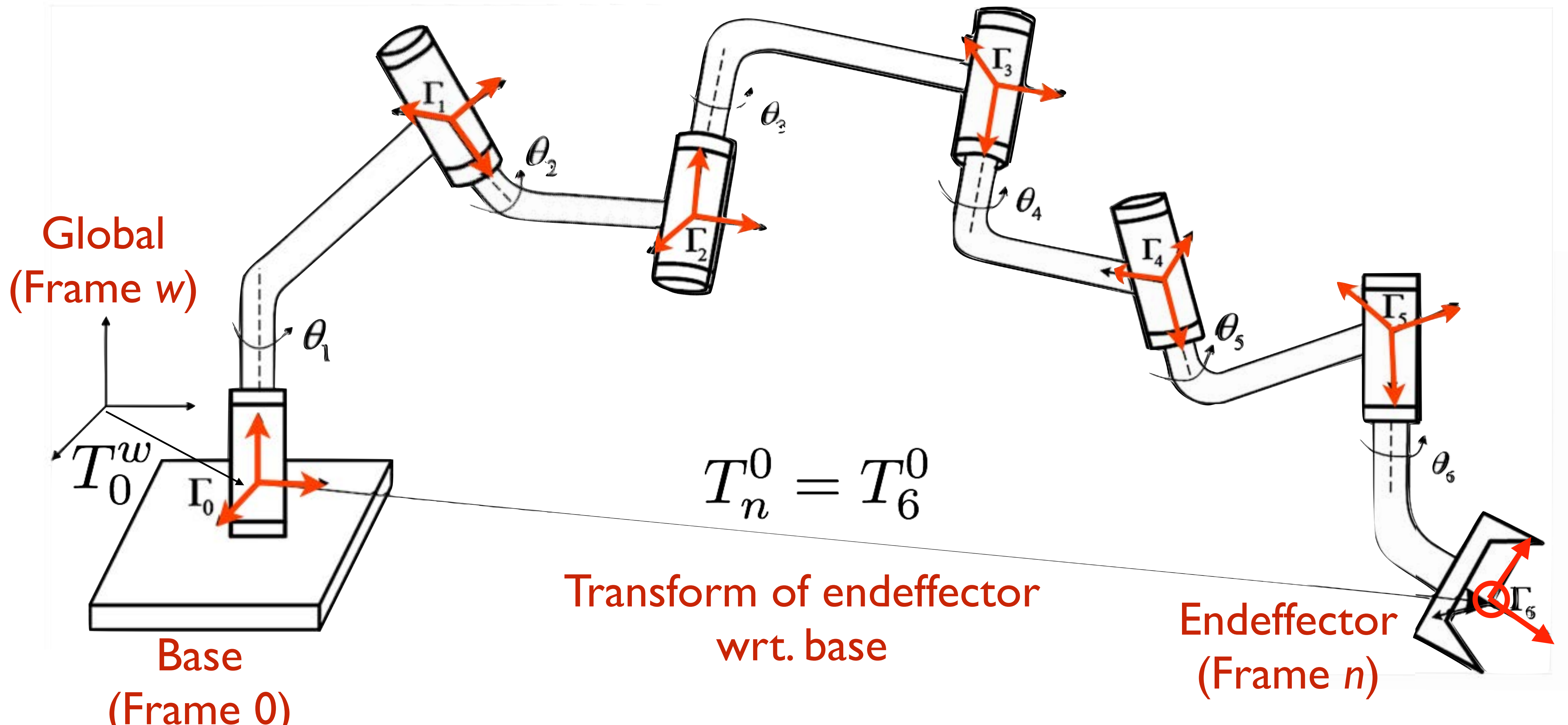
Forward kinematics: many-to-one mapping of robot configuration to reachable workspace endeffector poses



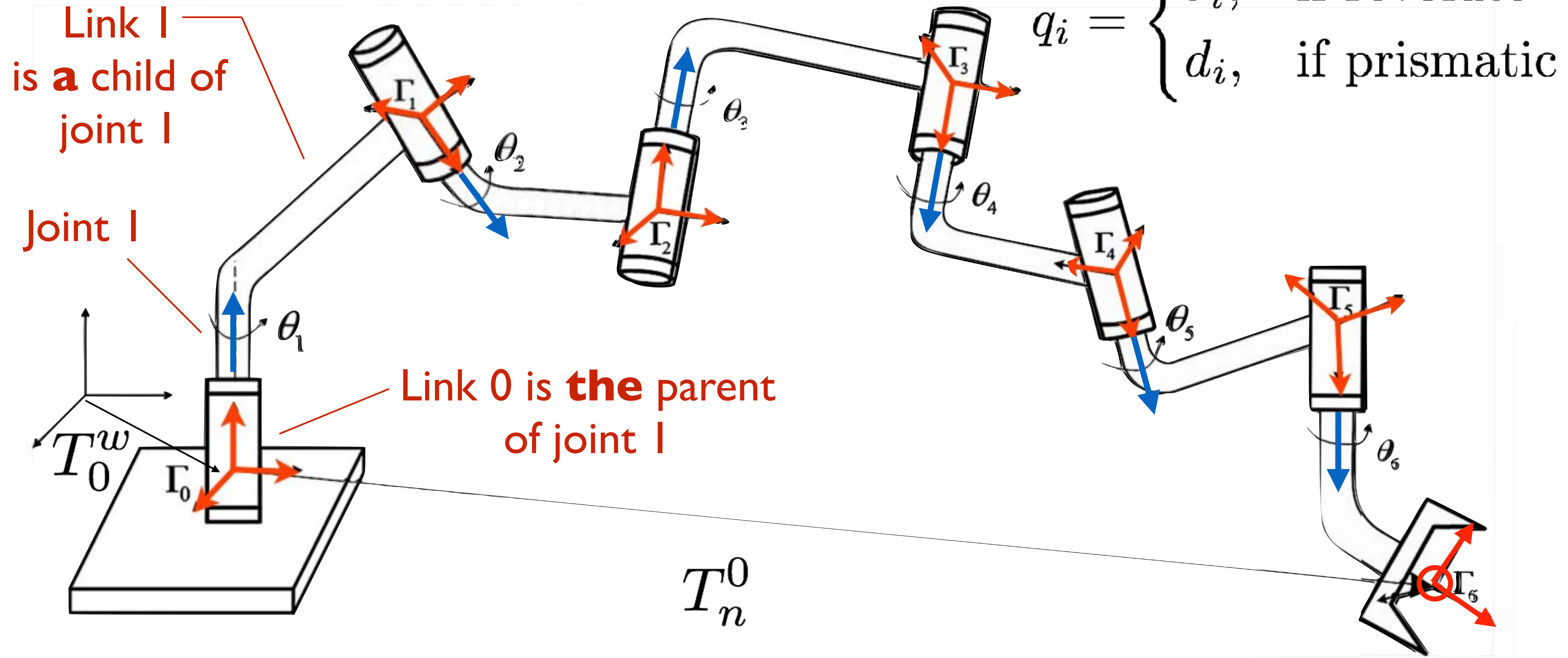
Workspace: 3D space defined in the global frame



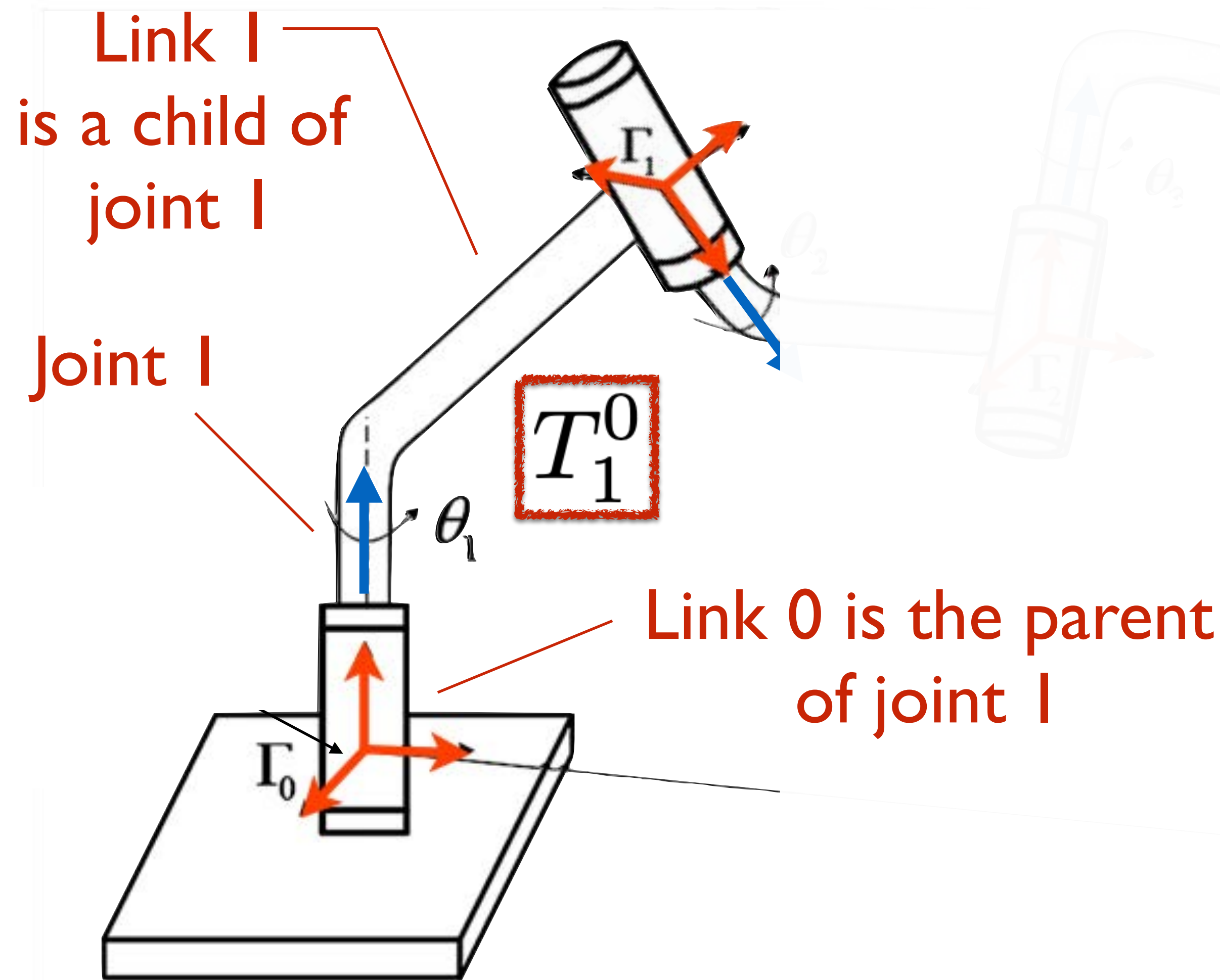
Kinematic chain: connects $N+1$ links together by N joints;
with a coordinate frame on each link



Joint (q_i): relates the motion of one link (the child link) wrt. another link (the parent)
 joint motion only affects the child link



Joint (q_i): relates the motion of one link (the child link) wrt. another link (the parent)
 joint motion only affects the child link, where its state



$$q_i = \begin{cases} \theta_i, & \text{if revolute} \\ d_i, & \text{if prismatic} \end{cases}$$

is used to express a 4-by-4 homogeneous transform $\mathbf{A}_i(q_i)$:

$$A_i = \begin{bmatrix} R_i^{i-1} & o^{i-1} \\ 0 & 1 \end{bmatrix}$$

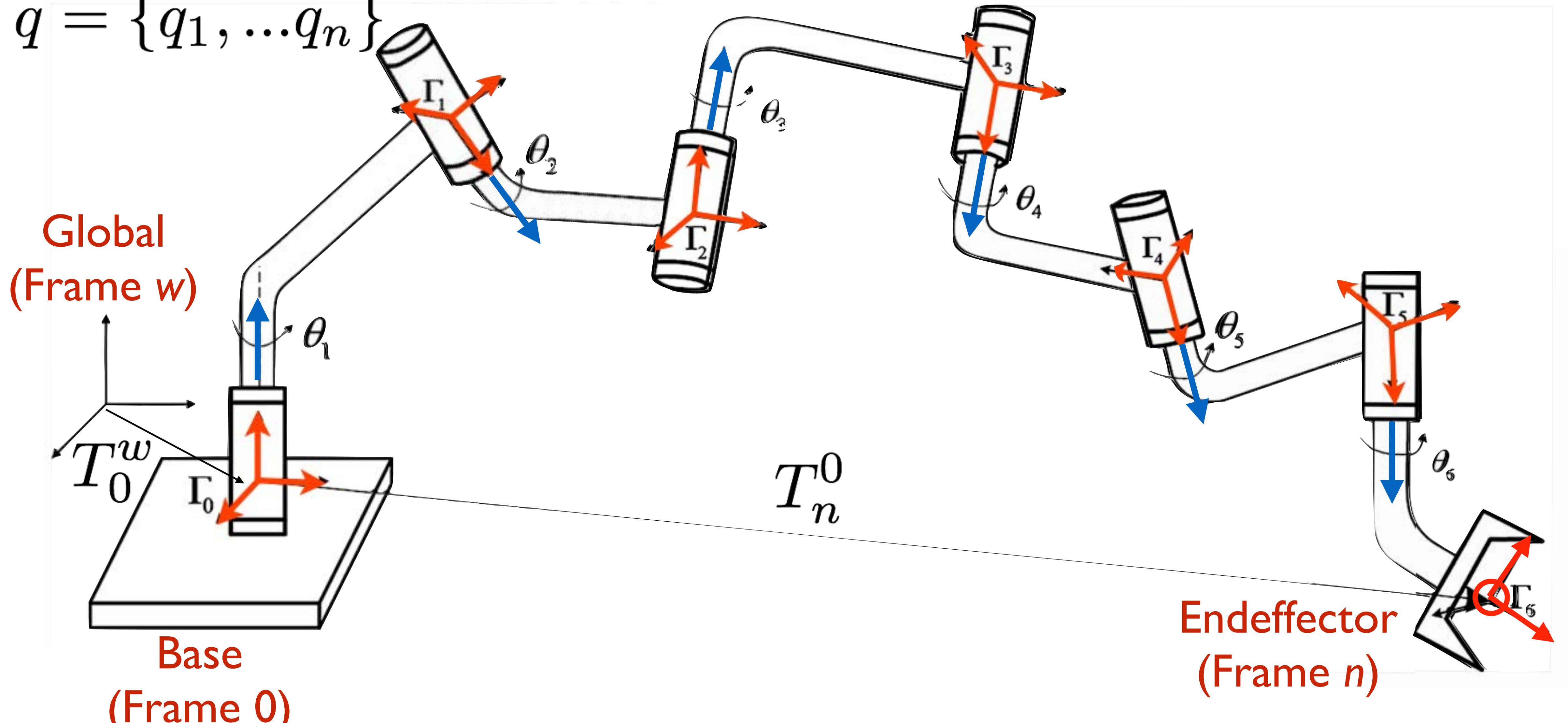
such that frames in a kinematic chain are related as by T_j^i :

$$T_j^i = \begin{cases} A_{i+1} A_{i+2} \dots A_{j-1} A_j & \text{if } i < j \\ I & \text{if } i = j \\ (T_j^i)^{-1} & \text{if } j > i \end{cases}$$

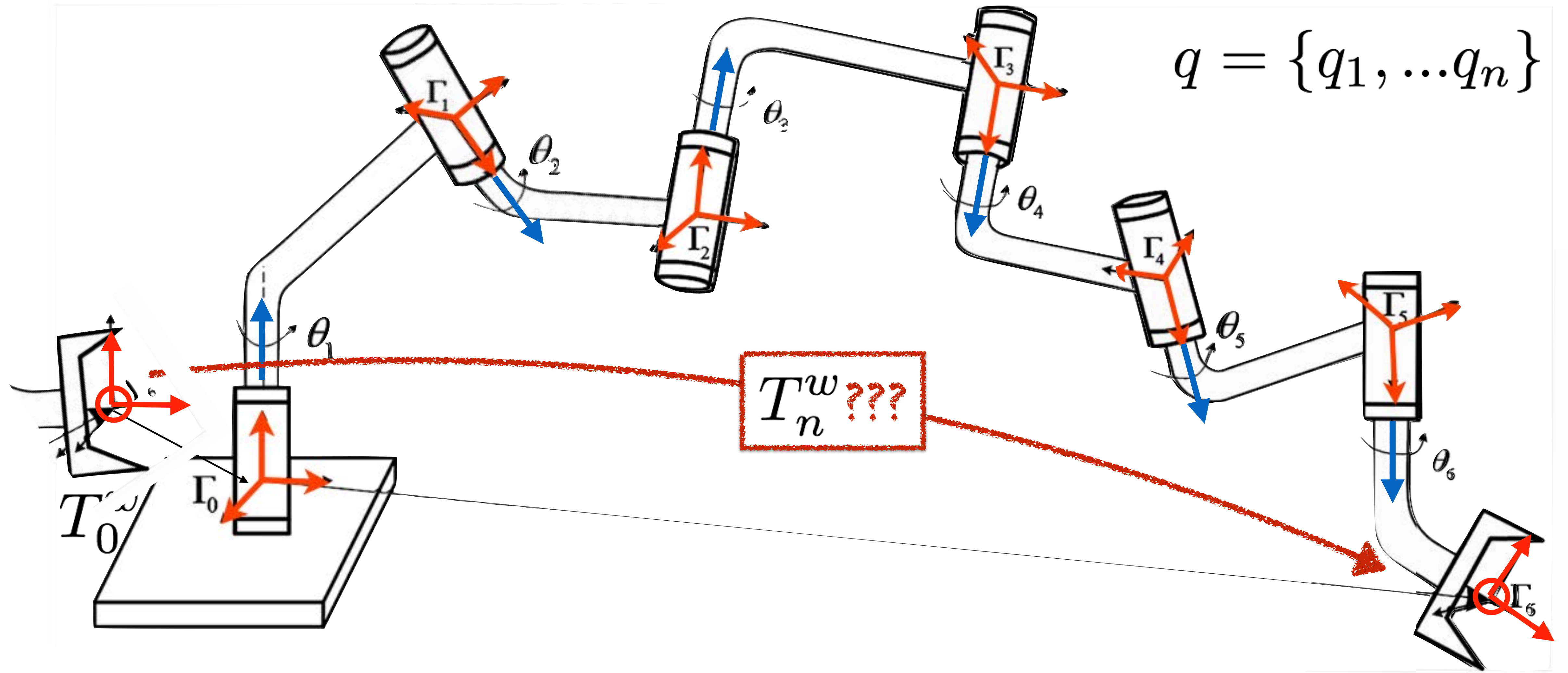
Configuration (q): is the state of all joints in the kinematic chain

Configuration space: the space of all possible configurations

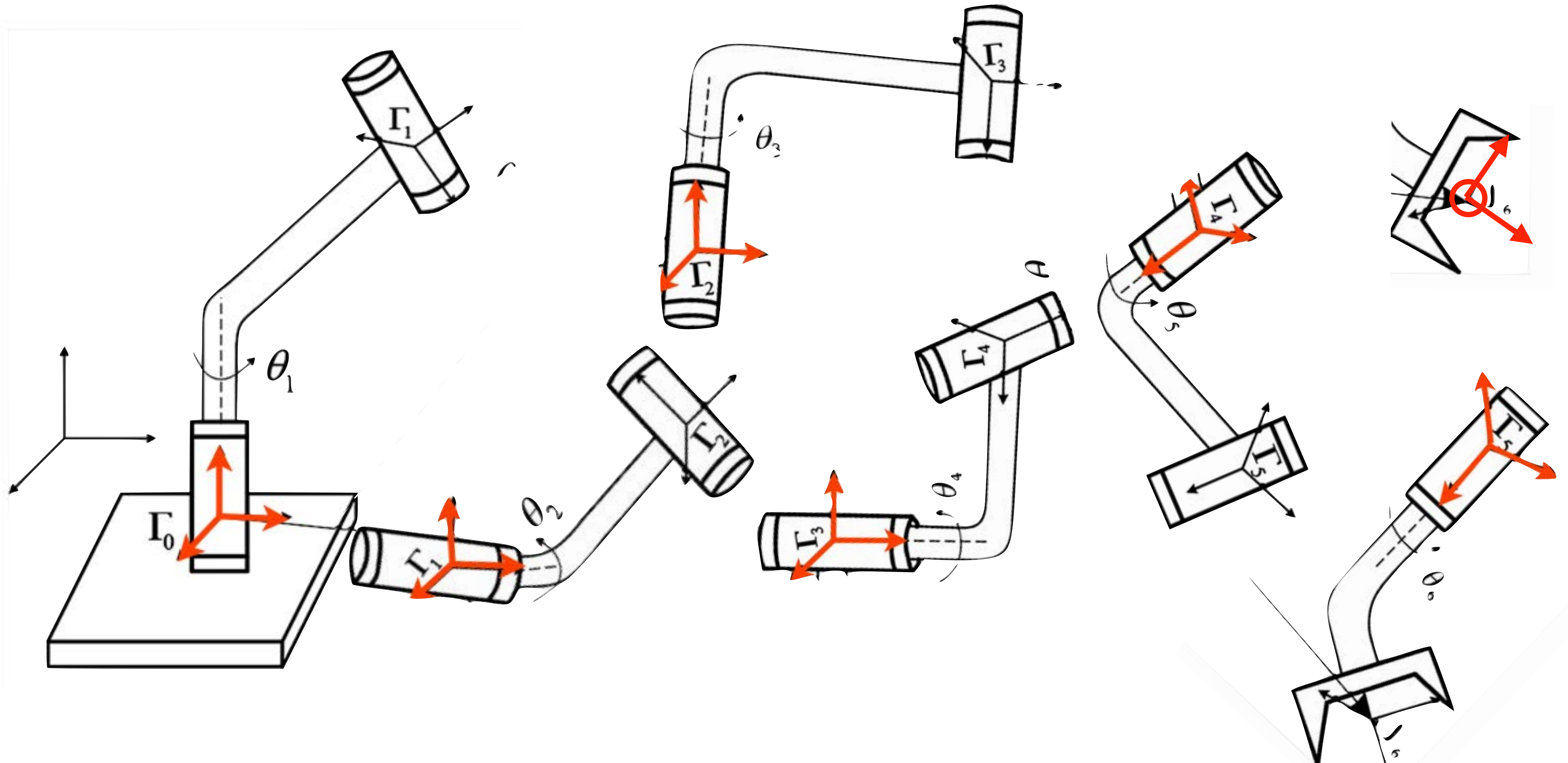
$$q = \{q_1, \dots, q_n\}$$



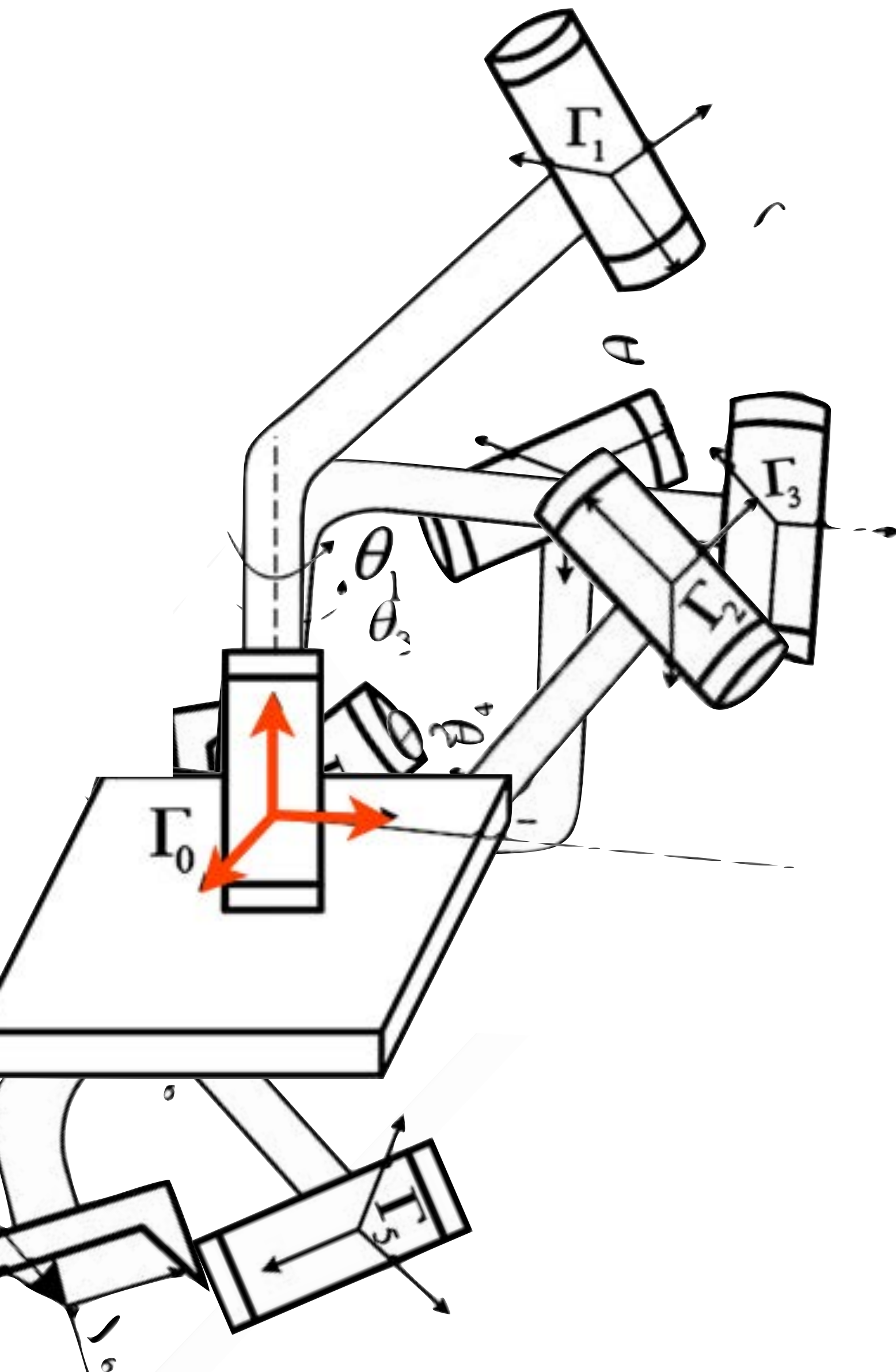
Forward kinematics restated: Given \mathbf{q} , find T_n^w ;
 T_n^w transforms endeffector into workspace



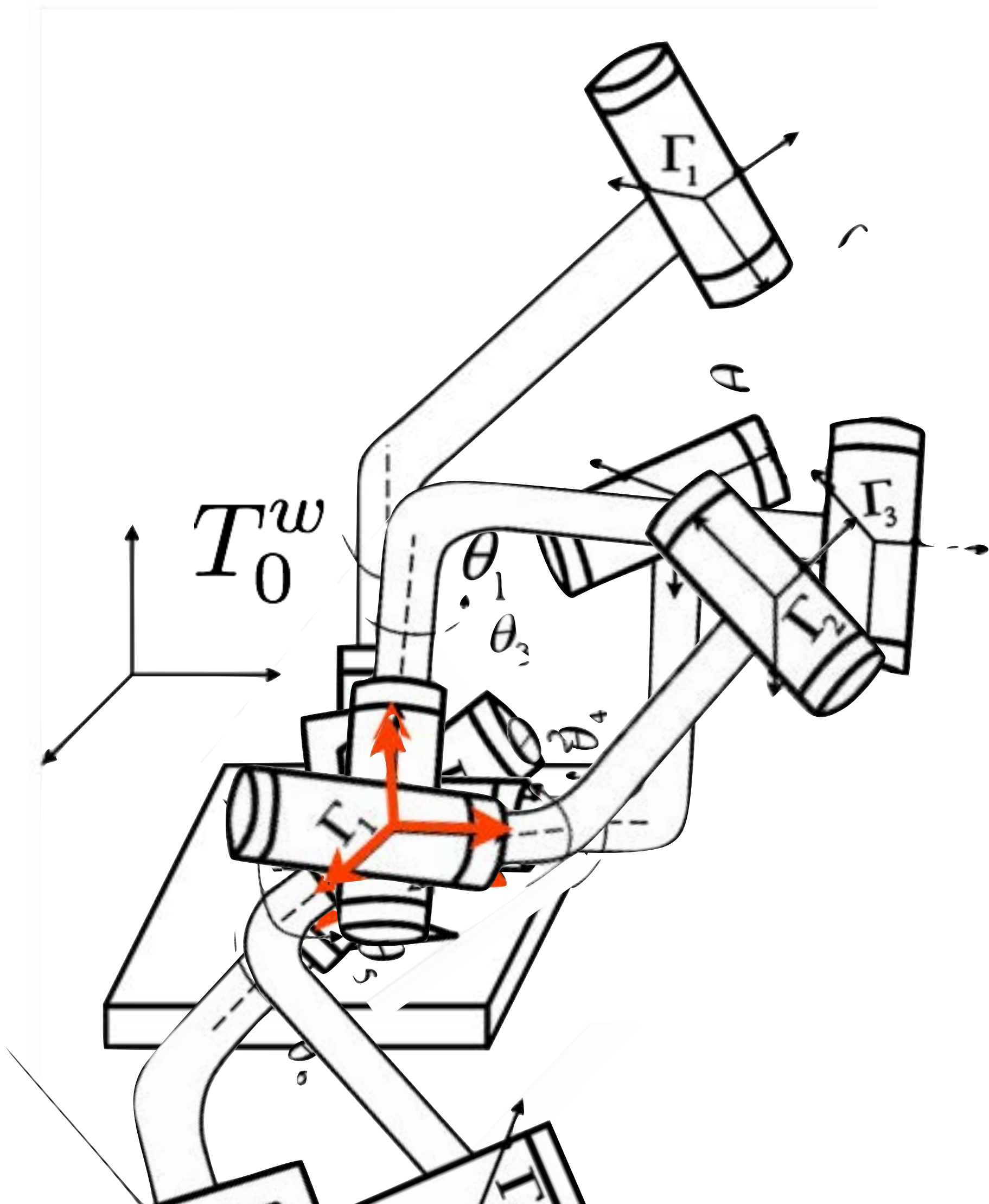
Problem: Every link considers itself to be the center of the universe.
How do we properly pose link with respect to each other?

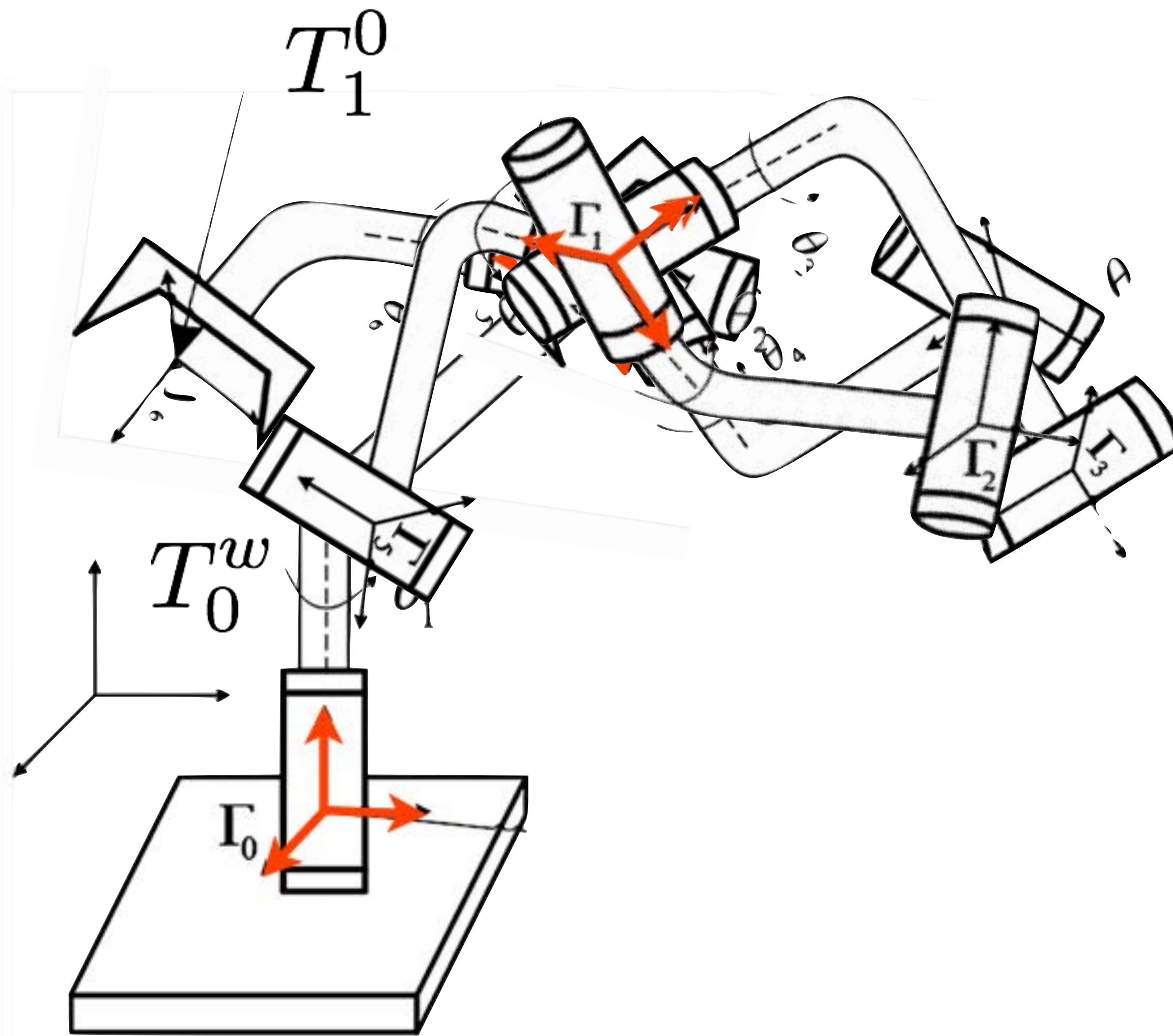


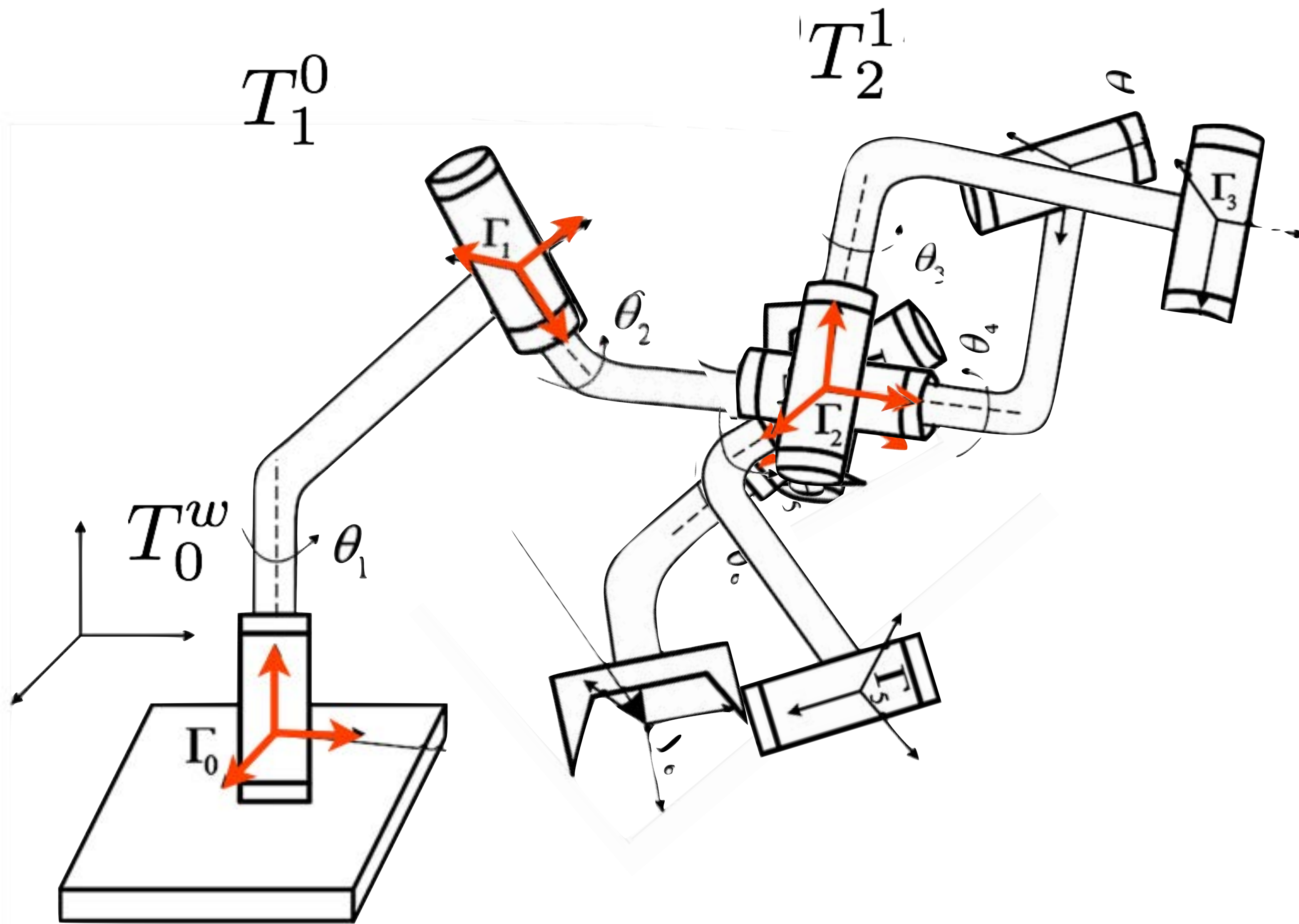
Approach: Consider all links to be aligned with the global origin ...

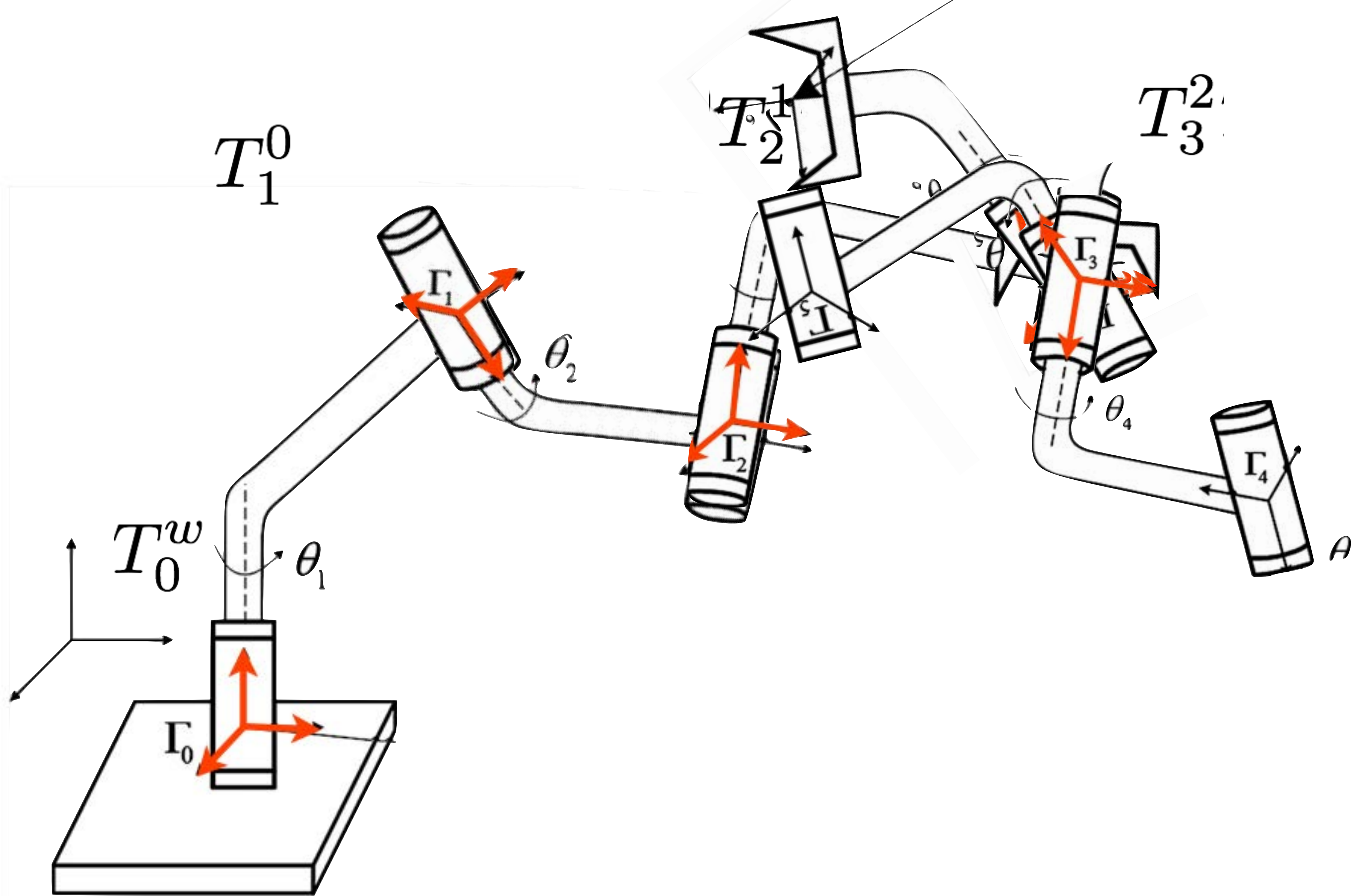


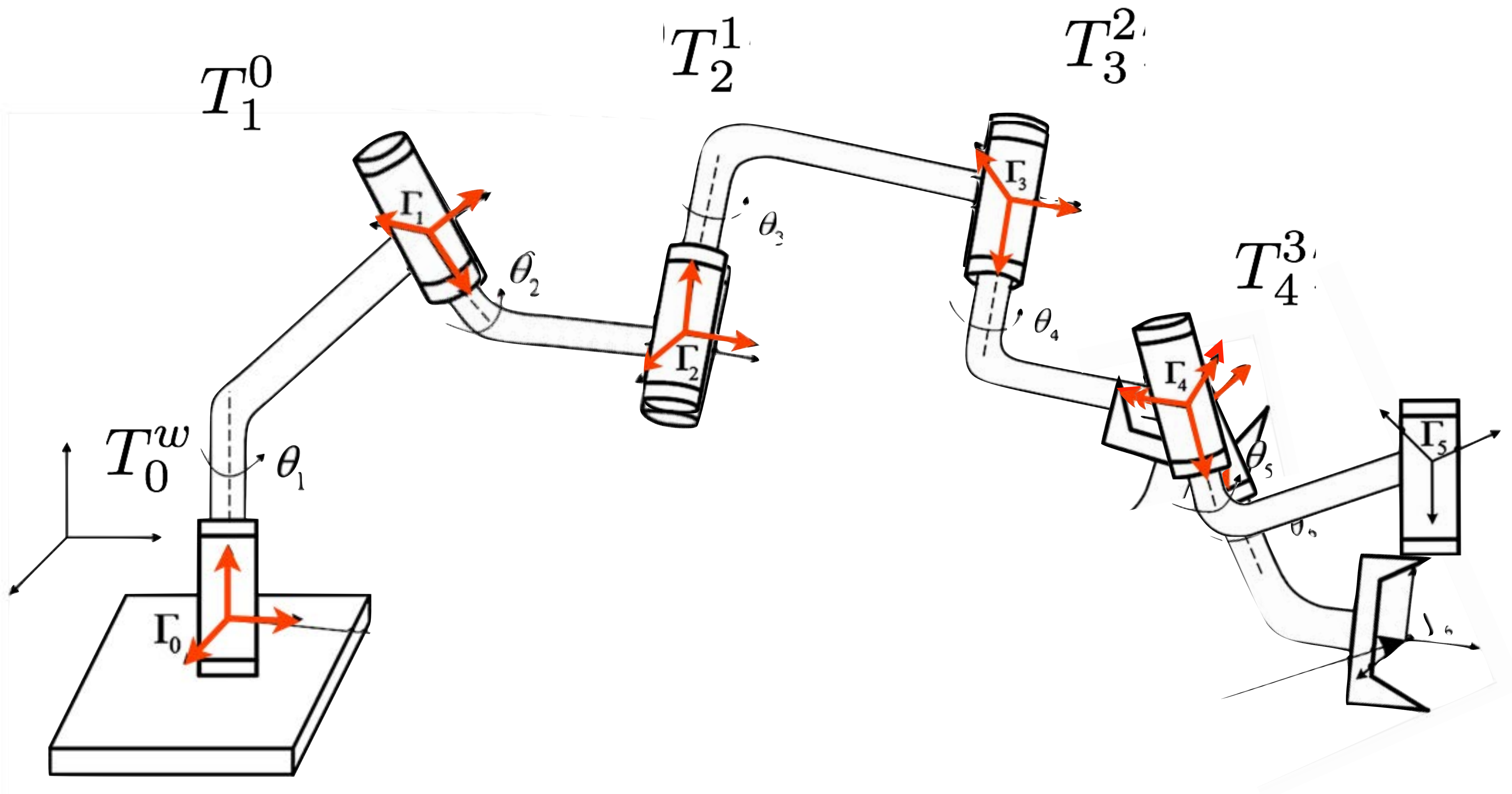
Approach: transform along kinematic chain bringing descendants along;
each transform will consist of a rotation and a translation

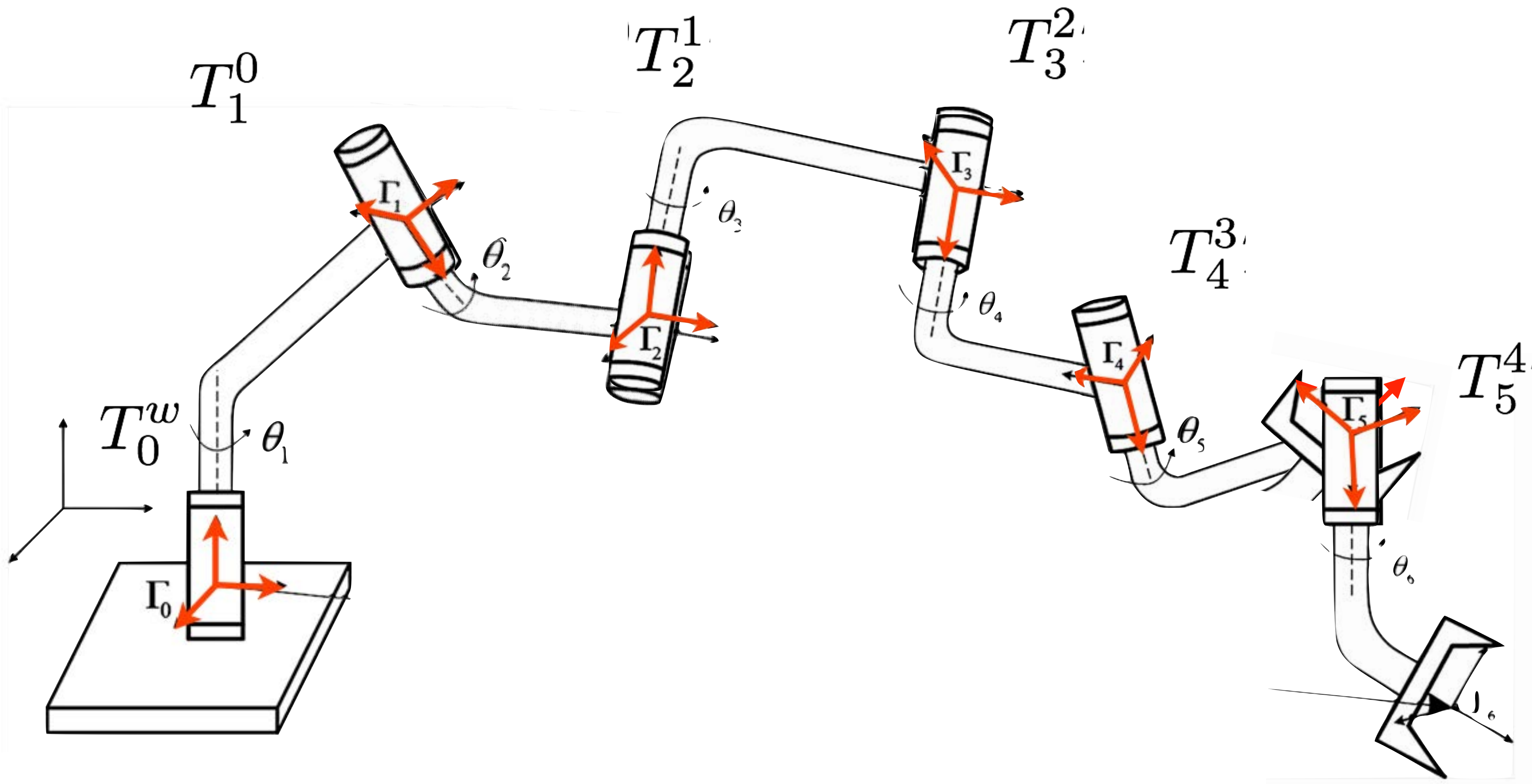


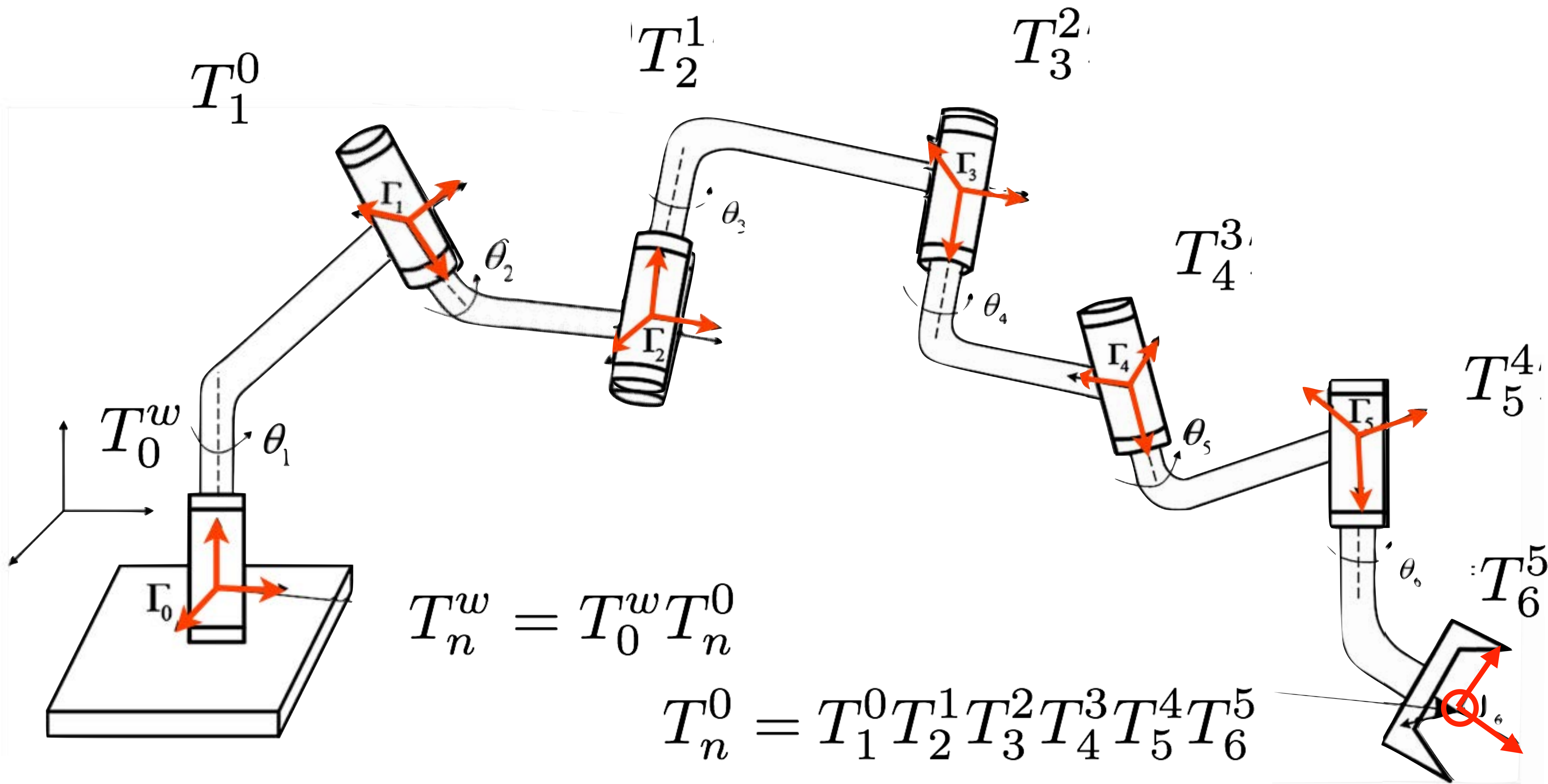




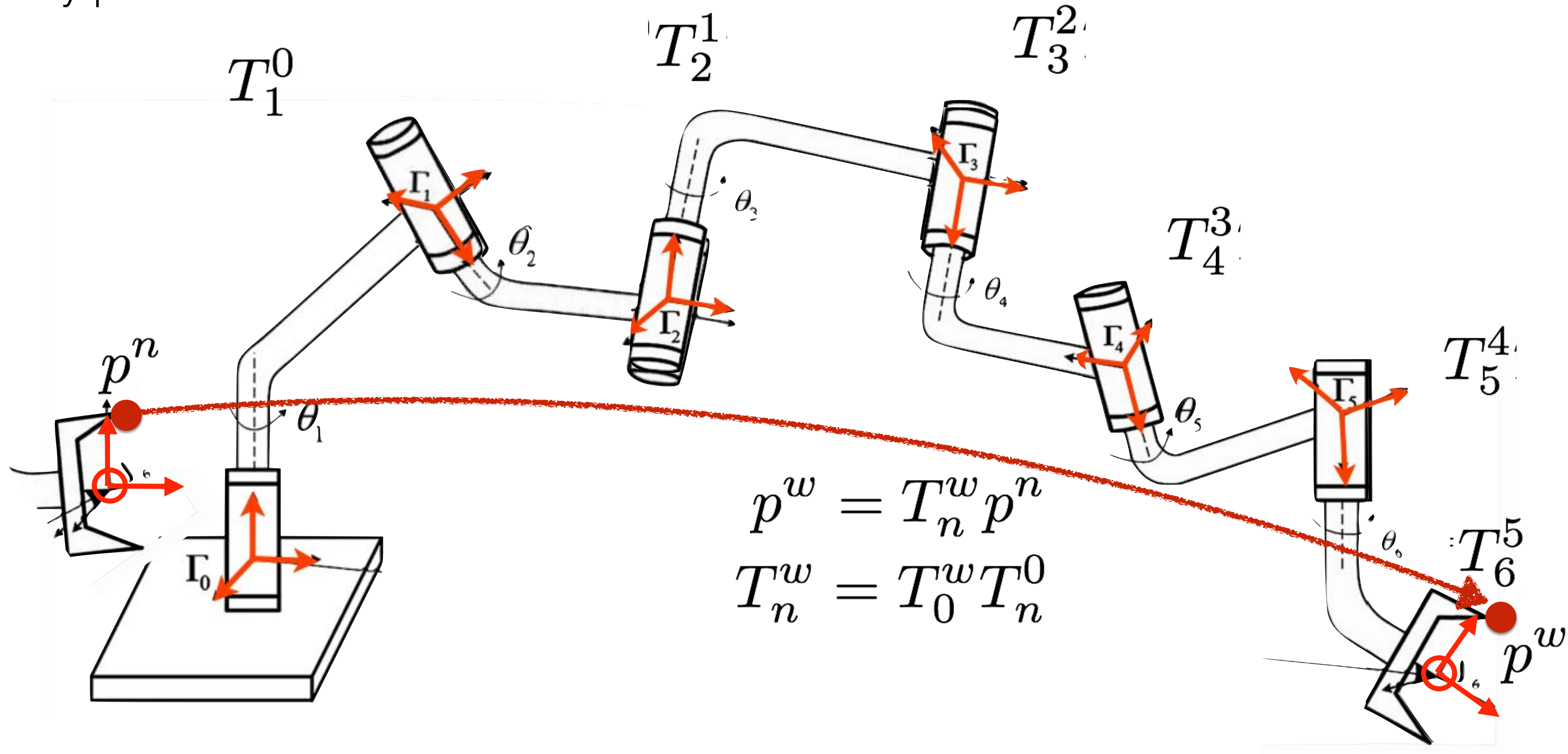




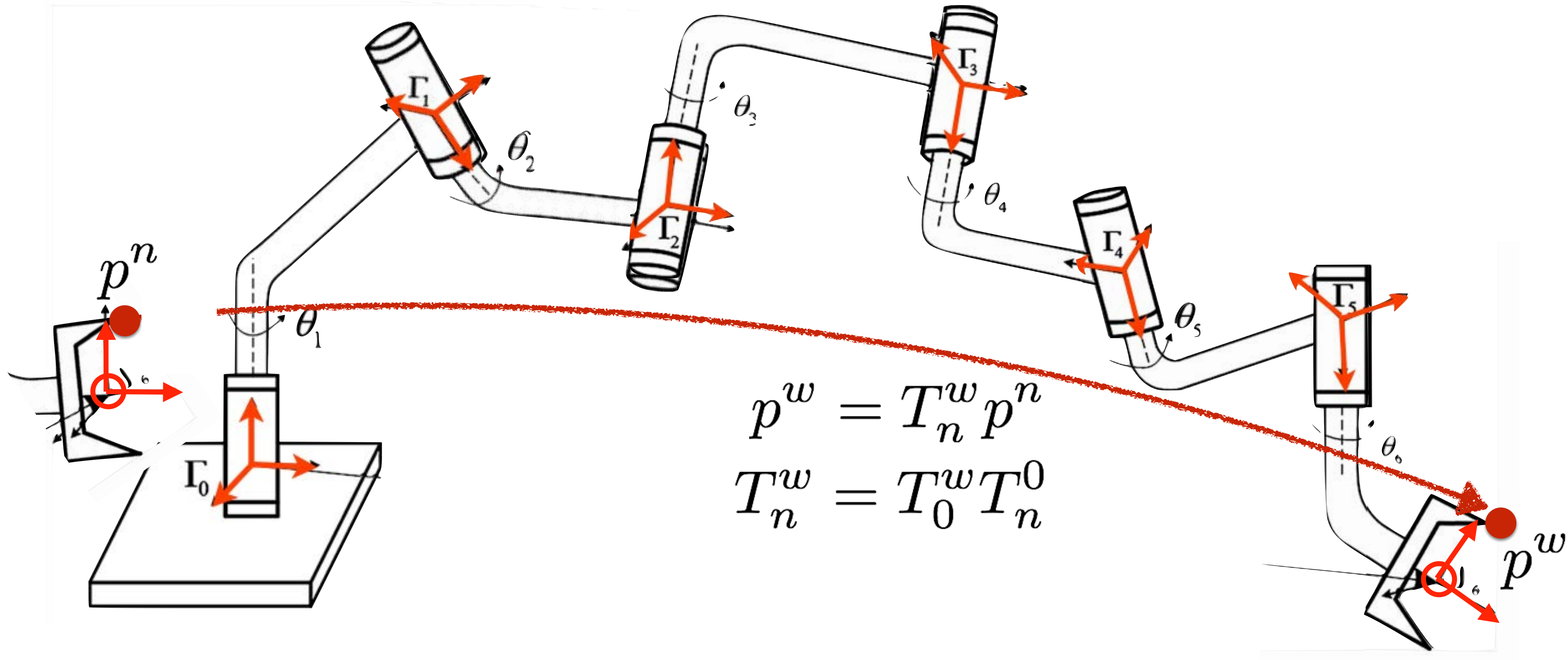




Any point on the endeffector can be transformed to its location in the world



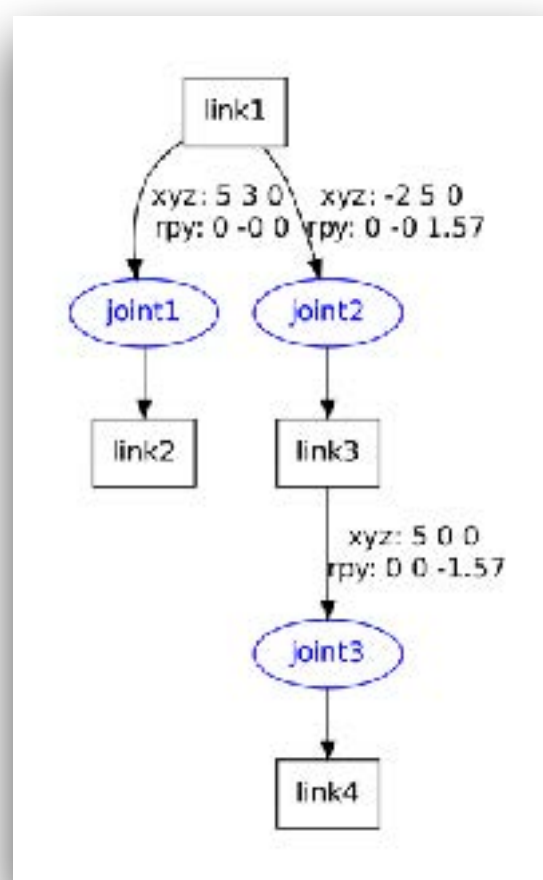
- 1) How to represent homogeneous transforms?
- 2) How to compute transform to endeffector?



1) How to represent homogeneous transforms?

Assuming as given the:

- geometry of each link
- robot's kinematic definition



Homogeneous Transform

defines SE(2): Special Euclidean Group 2

$$H = \begin{bmatrix} R_{00} & R_{01} & d_x \\ R_{10} & R_{11} & d_y \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \mathbf{R}_{2 \times 2} & \mathbf{d}_{2 \times 1} \\ \mathbf{0}_{1 \times 2} & 1 \end{bmatrix}$$

$H \in SE(2)$ $\mathbf{R}_{2 \times 2} \in SO(2)$ $\mathbf{d}_{2 \times 1} \in \mathbb{R}^2$

3D Homogeneous Transform

$$H_3 = \begin{bmatrix} R_{00} & R_{01} & R_{02} & d_x \\ R_{10} & R_{11} & R_{12} & d_y \\ R_{20} & R_{21} & R_{22} & d_z \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \mathbf{R}_{3 \times 3} & \mathbf{d}_{3 \times 1} \\ \mathbf{0}_{1 \times 3} & 1 \end{bmatrix} \in SE(3)$$

if $T_1^0 \in SE(3)$ and $T_2^1 \in SE(3)$ then composition holds:

$$\begin{bmatrix} R_1^0 & d_1^0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} R_2^1 & d_2^1 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} R_1^0 R_2^1 & R_1^0 d_2^1 + d_1^0 \\ 0 & 1 \end{bmatrix}$$

such that points in Frame 2 can be expressed in Frame 0 by:

$$p^0 = T_1^0 T_2^1 p^2$$

2) How to compute transform to endeffector?

Zero configuration

Assuming as given the:

- geometry of each link
- robot's kinematic definition
- **current state of all joints**

Matrix Stack Reloaded

Geometry vertices of link1 can now be transformed into pose in the world frame

Add motor motion

motor transform affects outboard chain

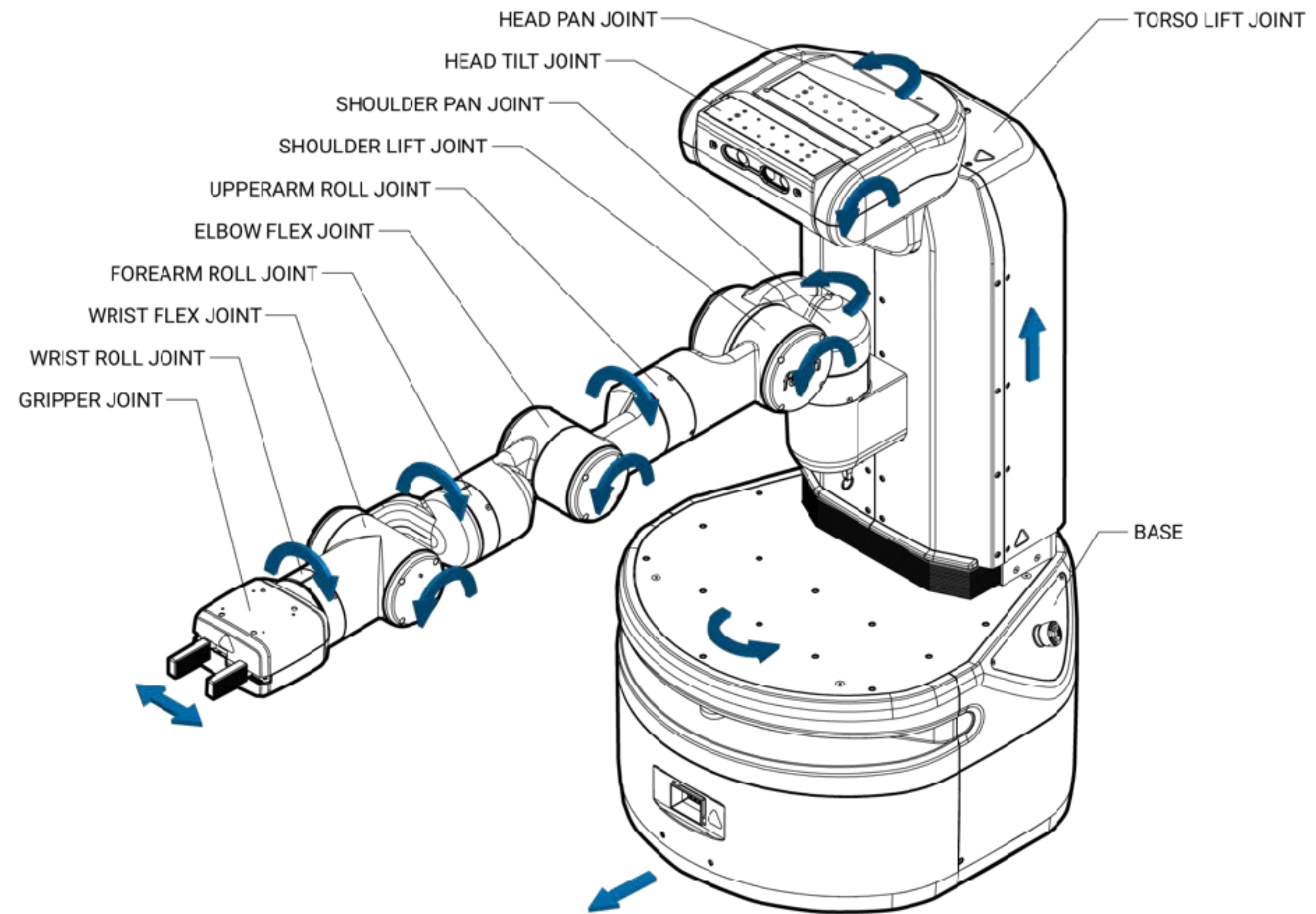
$Link2^{world} = mstack * Link2^{link2}$
 $= (D^w_i * R^w_i * D^l_i * R^l_i * D^o_i(q_i)) * Link2^{link2}$

joint2 is revolute

rotation about unit joint axis u_2 by joint state q_2

// joint motor rotation axis
 robot.joint2["joint2"].axis = [0.707, 0.0, 0.707]

Can a joint move infinitely far?



Joint Limits

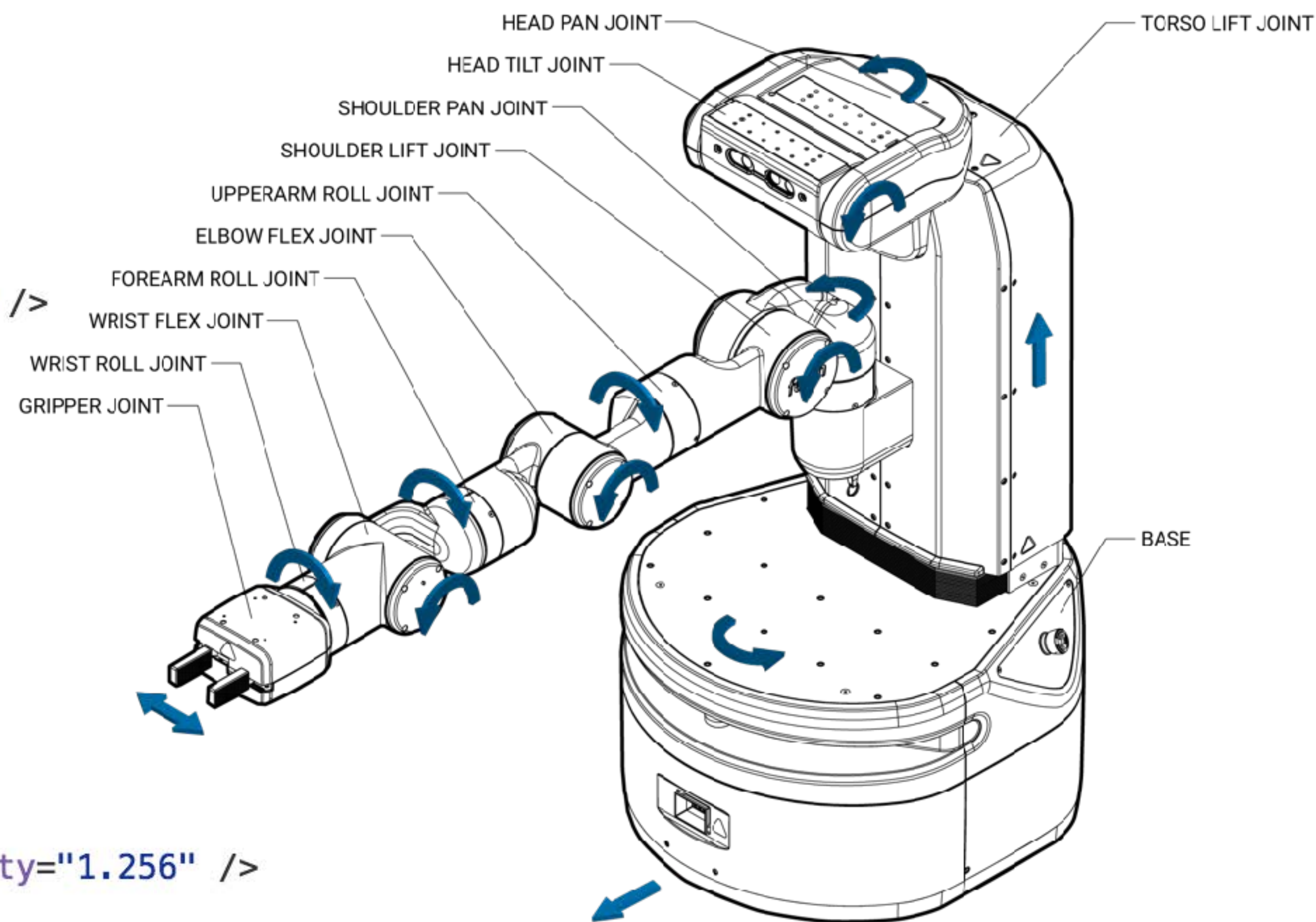
Prismatic joint description

```
<joint name="torso_lift_joint" type="prismatic">  
  <origin rpy="-6.123E-17 0 0" xyz="-0.086875 0 0.37743" />  
  <parent link="base_link" />  
  <child link="torso_lift_link" />  
  <axis xyz="0 0 1" />  
  <limit effort="450.0" lower="0" upper="0.4" velocity="0.1" />  
<dynamics damping="100.0" /></joint>
```

Revolute joint description

```
<joint name="shoulder_pan_joint" type="revolute">  
  <origin rpy="0 0 0" xyz="0.119525 0 0.34858" />  
  <parent link="torso_lift_link" />  
  <child link="shoulder_pan_link" />  
  <axis xyz="0 0 1" />  
  <dynamics damping="1.0" />  
  <limit effort="33.82" lower="-1.6056" upper="1.6056" velocity="1.256" />  
</joint>
```

Continuous joints have no limits



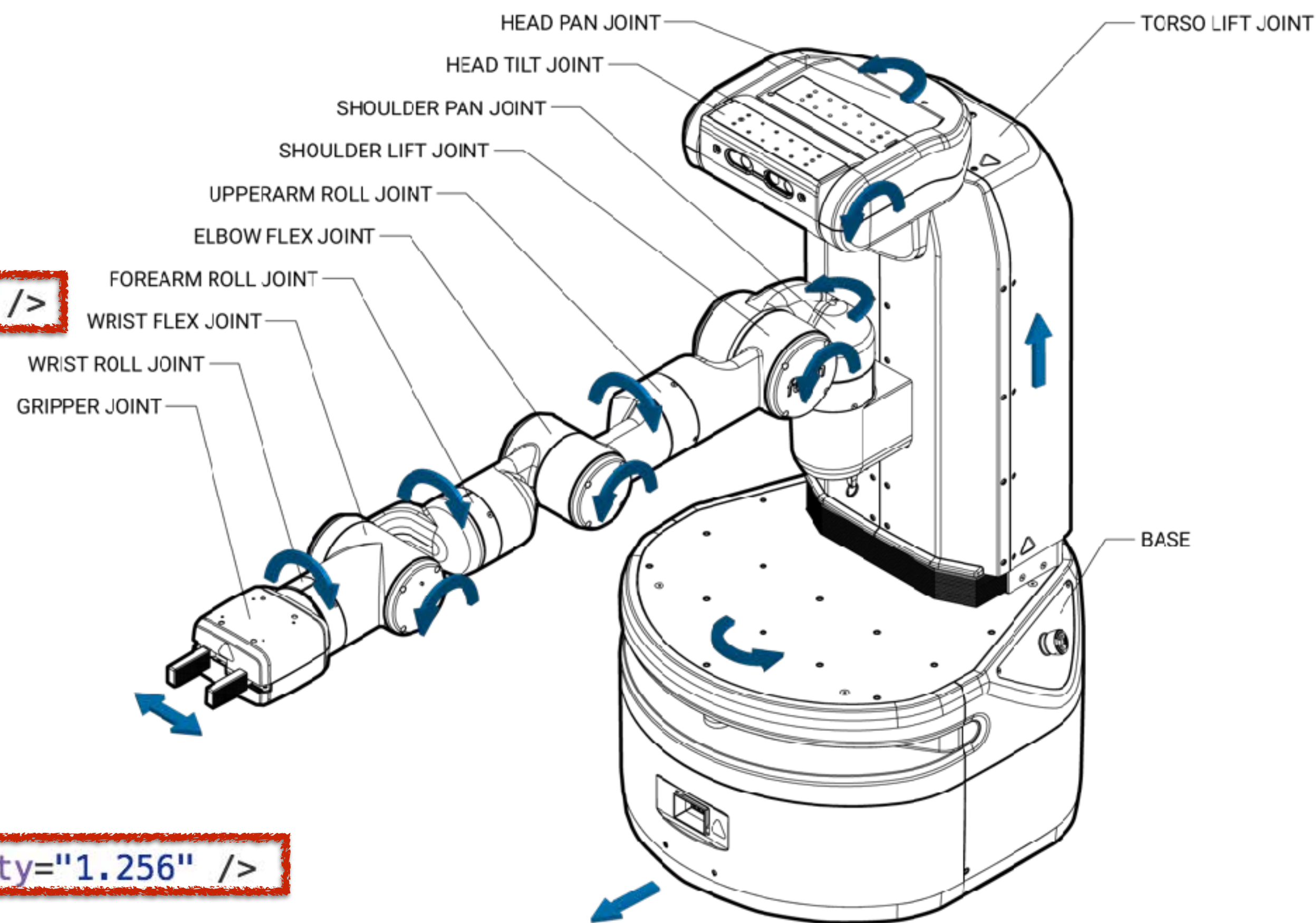
Joint Limits

Prismatic joint description

```
<joint name="torso_lift_joint" type="prismatic">  
  <origin rpy="-6.123E-17 0 0" xyz="-0.086875 0 0.37743" />  
  <parent link="base_link" />  
  <child link="torso_lift_link" />  
  <axis xyz="0 0 1" />  
  <limit effort="450.0" lower="0" upper="0.4" velocity="0.1" />  
<dynamics damping="100.0" /></joint>
```

Revolute joint description

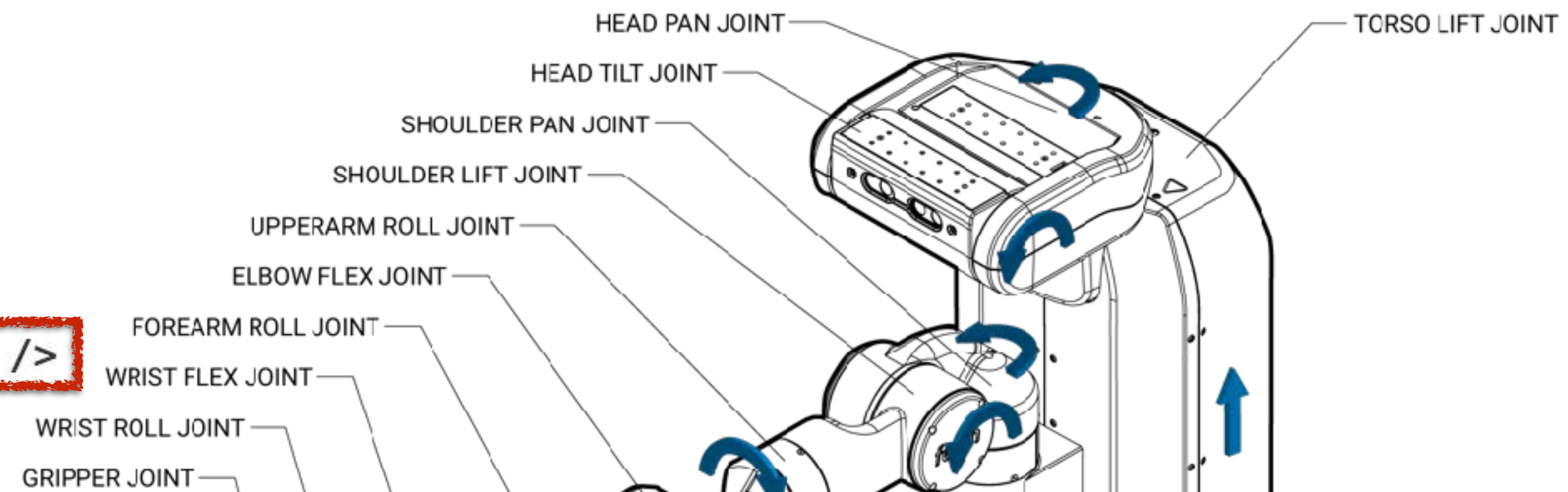
```
<joint name="shoulder_pan_joint" type="revolute">  
  <origin rpy="0 0 0" xyz="0.119525 0 0.34858" />  
  <parent link="torso_lift_link" />  
  <child link="shoulder_pan_link" />  
  <axis xyz="0 0 1" />  
  <dynamics damping="1.0" />  
  <limit effort="33.82" lower="-1.6056" upper="1.6056" velocity="1.256" />  
</joint>
```




```
robot.joints.torso_lift_joint = {parent:"base_link", child:"torso_lift_link"};
robot.joints.torso_lift_joint.axis = [0,0,1];
robot.joints.torso_lift_joint.type = "prismatic";
robot.joints.torso_lift_joint.origin = {xyz: [-0.086875,0,0.37743], rpy: [-6.123E-17,0,0]};
robot.joints.torso_lift_joint.limit = {lower:0, upper:0.4};
```

Prismatic joint description

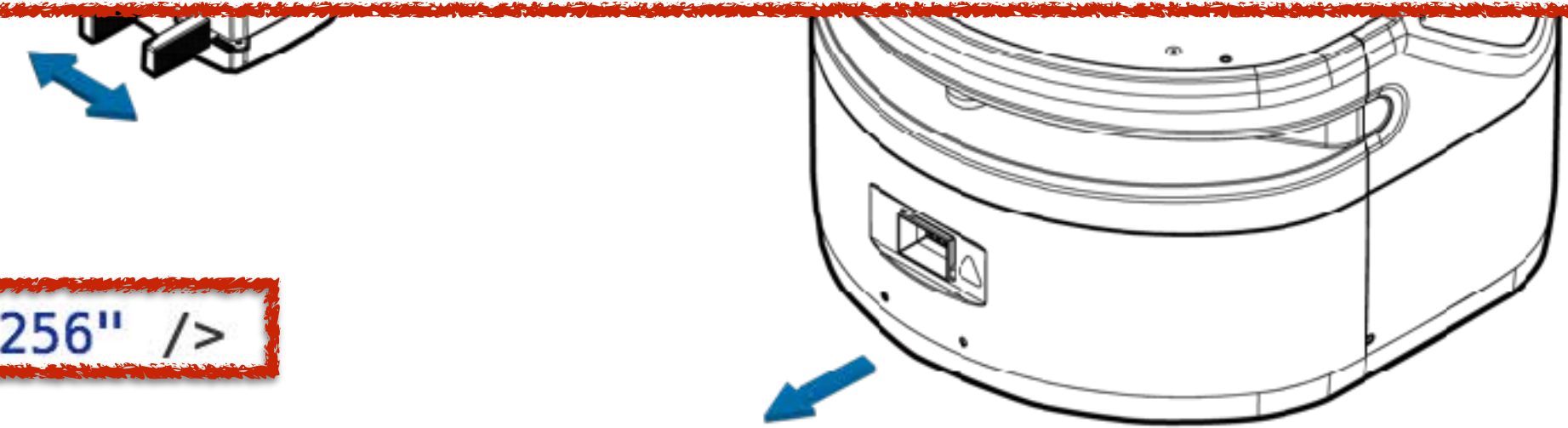
```
<joint name="torso_lift_joint" type="prismatic">
  <origin rpy="-6.123E-17 0 0" xyz="-0.086875 0 0.37743" />
  <parent link="base_link" />
  <child link="torso_lift_link" />
  <axis xyz="0 0 1" />
  <limit effort="450.0" lower="0" upper="0.4" velocity="0.1" />
<dynamics damping="100.0" /></joint>
```



Revolute joint description

```
<joint name="shoulder_pan_joint" type="revolute">
  <origin rpy="0 0 0" xyz="0.119525 0 0.34858" />
  <parent link="torso_lift_link" />
  <child link="shoulder_pan_link" />
  <axis xyz="0 0 1" />
  <dynamics damping="1.0" />
  <limit effort="33.82" lower="-1.6056" upper="1.6056" velocity="1.256" />
</joint>
```

```
robot.joints.shoulder_pan_joint = {parent:"torso_lift_link", child:"shoulder_pan_link"};
robot.joints.shoulder_pan_joint.axis = [0,0,1];
robot.joints.shoulder_pan_joint.type = "revolute";
robot.joints.shoulder_pan_joint.origin = {xyz: [0.119525,0,0.34858], rpy: [0,0,0]};
robot.joints.shoulder_pan_joint.limit = {lower:-1.6056, upper:1.6056};
```



Important notes



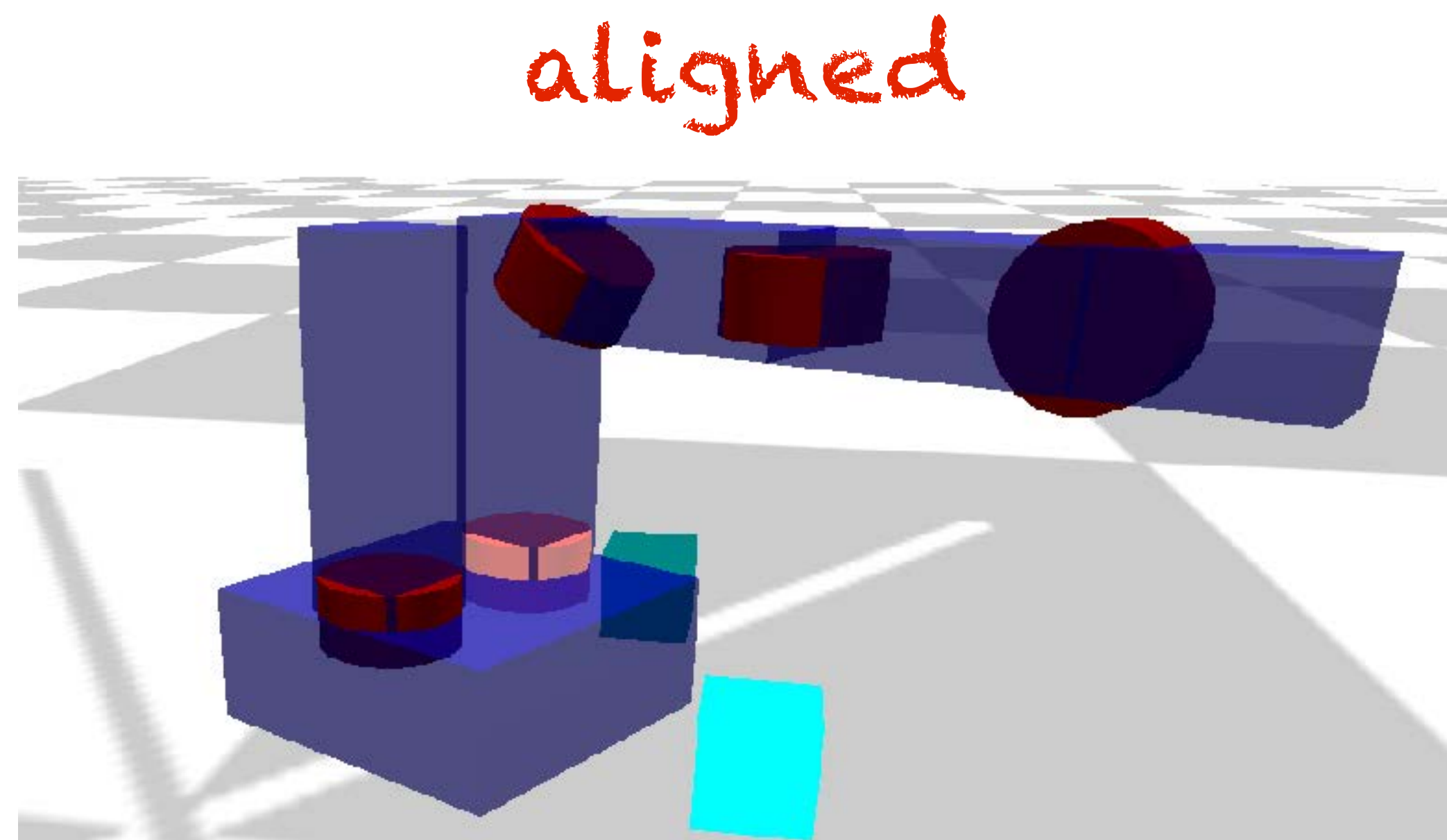
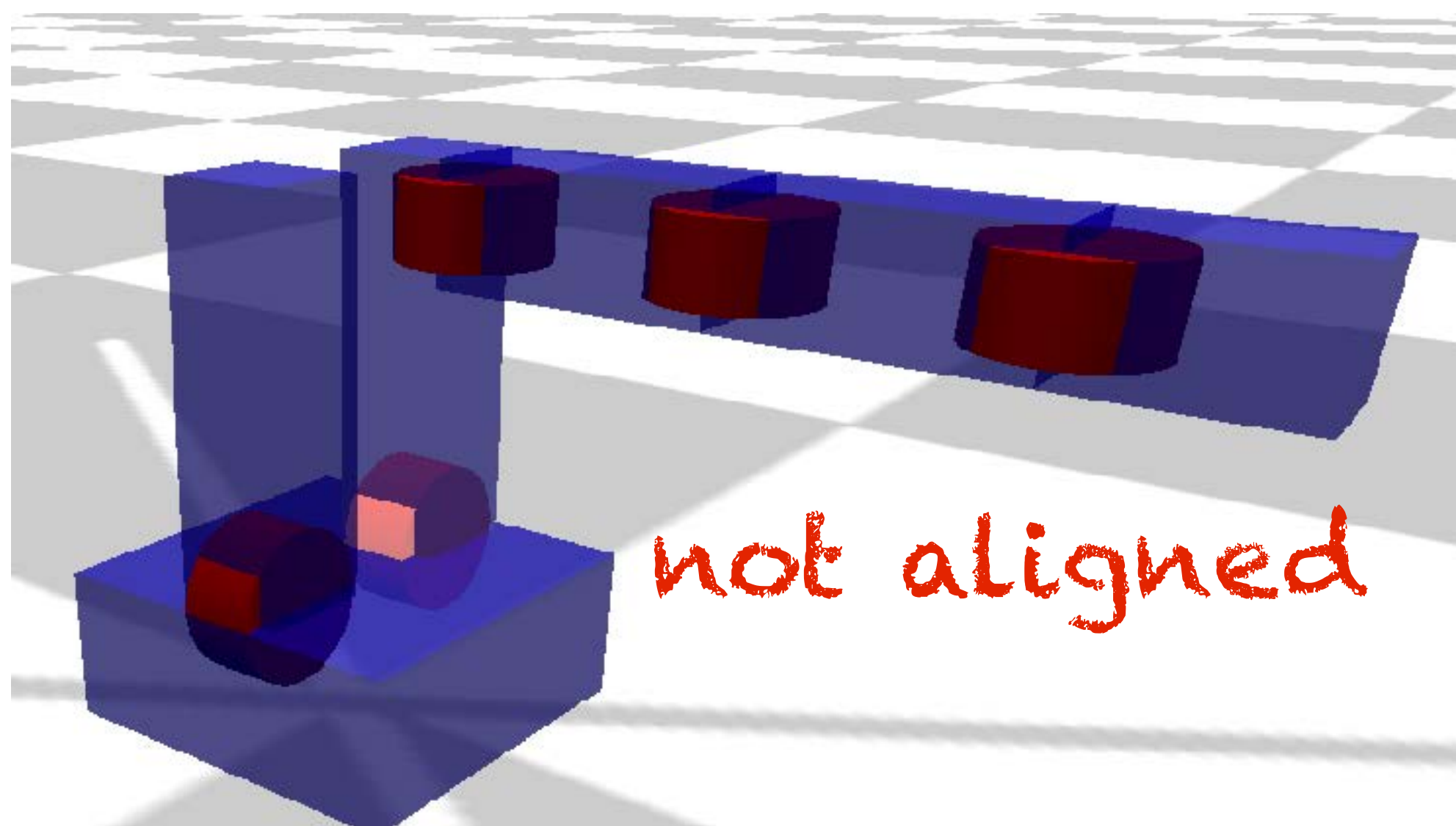
Important notes

- Rotation order I use: **XYZ** ($R_z R_y R_x$)
- `vector_cross()`: code stencil tests for and uses this function
- A joint and its child link will share the same coordinate frame



KinEval joint cylinder rendering

- threejs creates cylinders with axes aligned along y-axis
- you need to implement `vector_cross()` for KinEval to render joint cylinders properly along joint axis



Global controls for base

- Assume we have a base that is holonomic wrt. ground plane
 - holonomic: can move in any direction
- `kineval_userinput.js` assumes:

How to perform this
base movement?

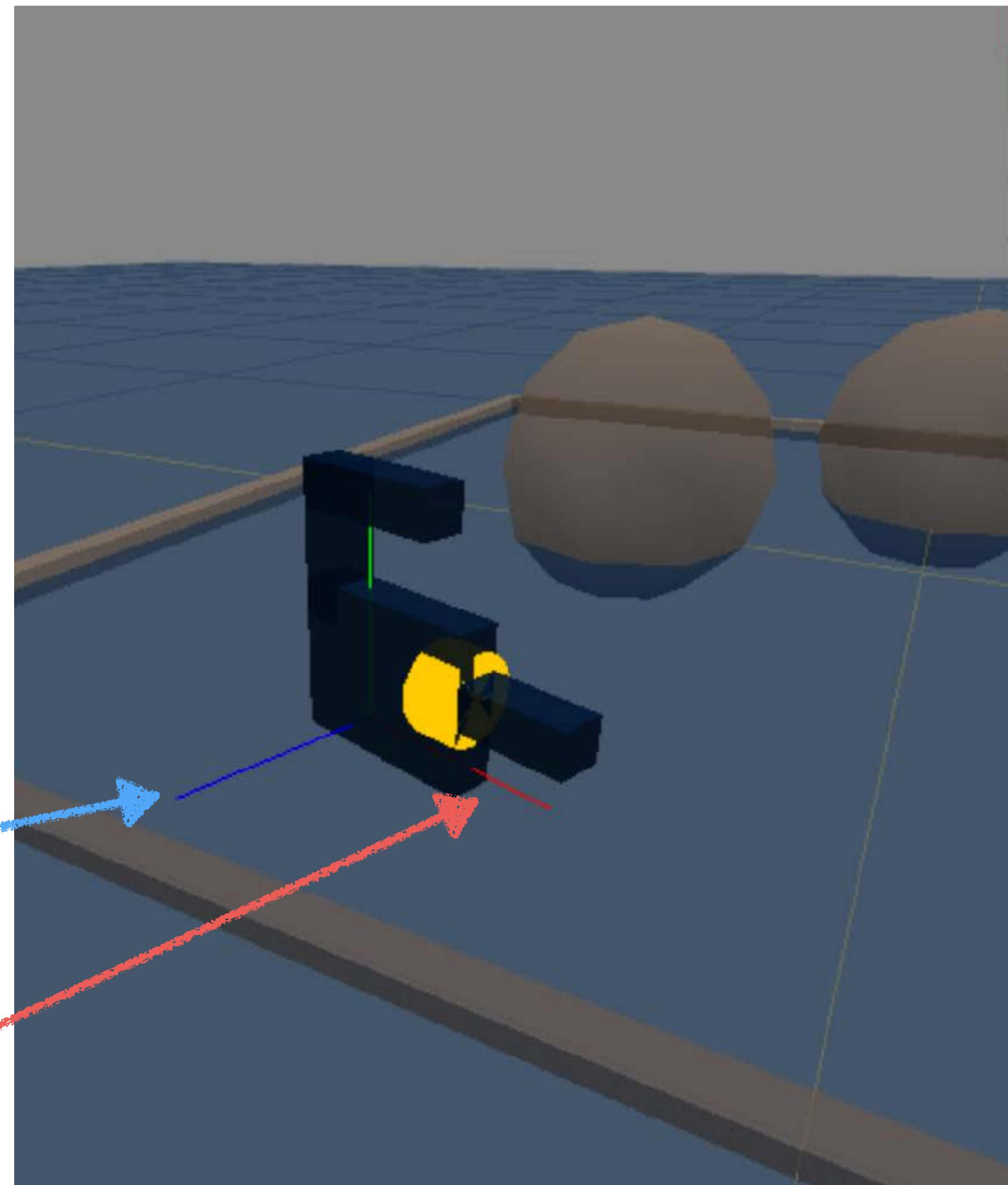


Transform vectors for heading (local z-axis) and lateral (local x-axis) of robot base into world coordinates

Store transformed vectors in variables "robot_heading" and "robot_lateral"

Forward heading of the robot

Lateral heading of the robot



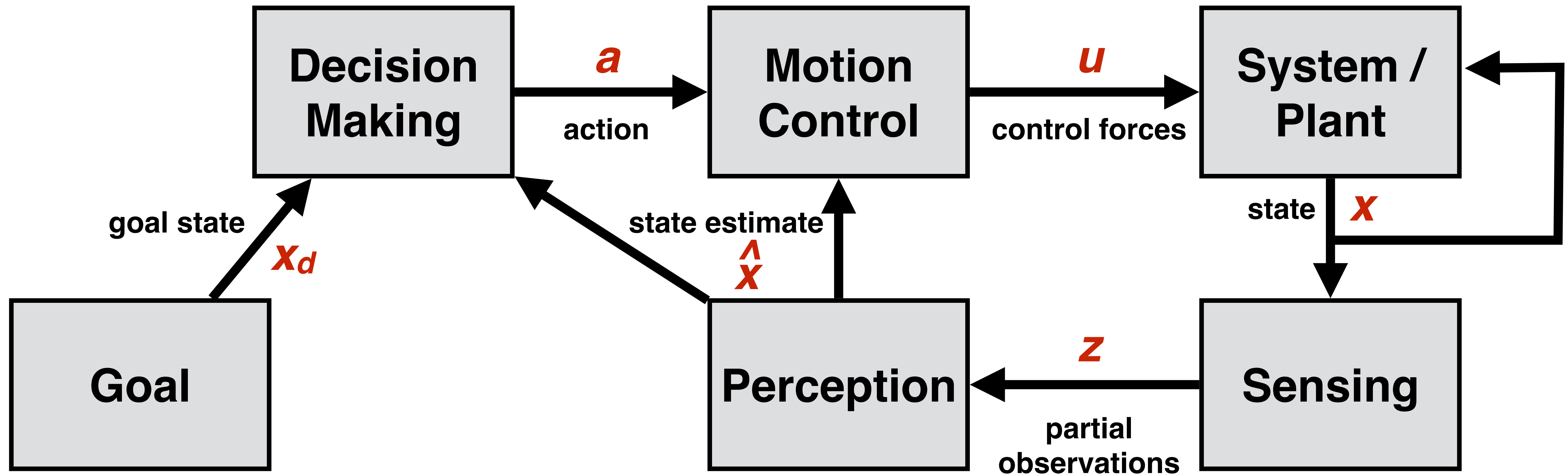
- kineval
- just_starting
- User Parameters
- Robot
- Forward Kinematics
- Inverse Kinematics
- Motion Planning
- ▾ Display
 - ▾ Geometries and Axes
 - display_links
 - display_links_...
 - display_base_...
 - display_joints
 - display_joints_...
 - display_joints_...
 - display_joints_...
 - display_wirefr...
 - display_collisi...
 - Colors



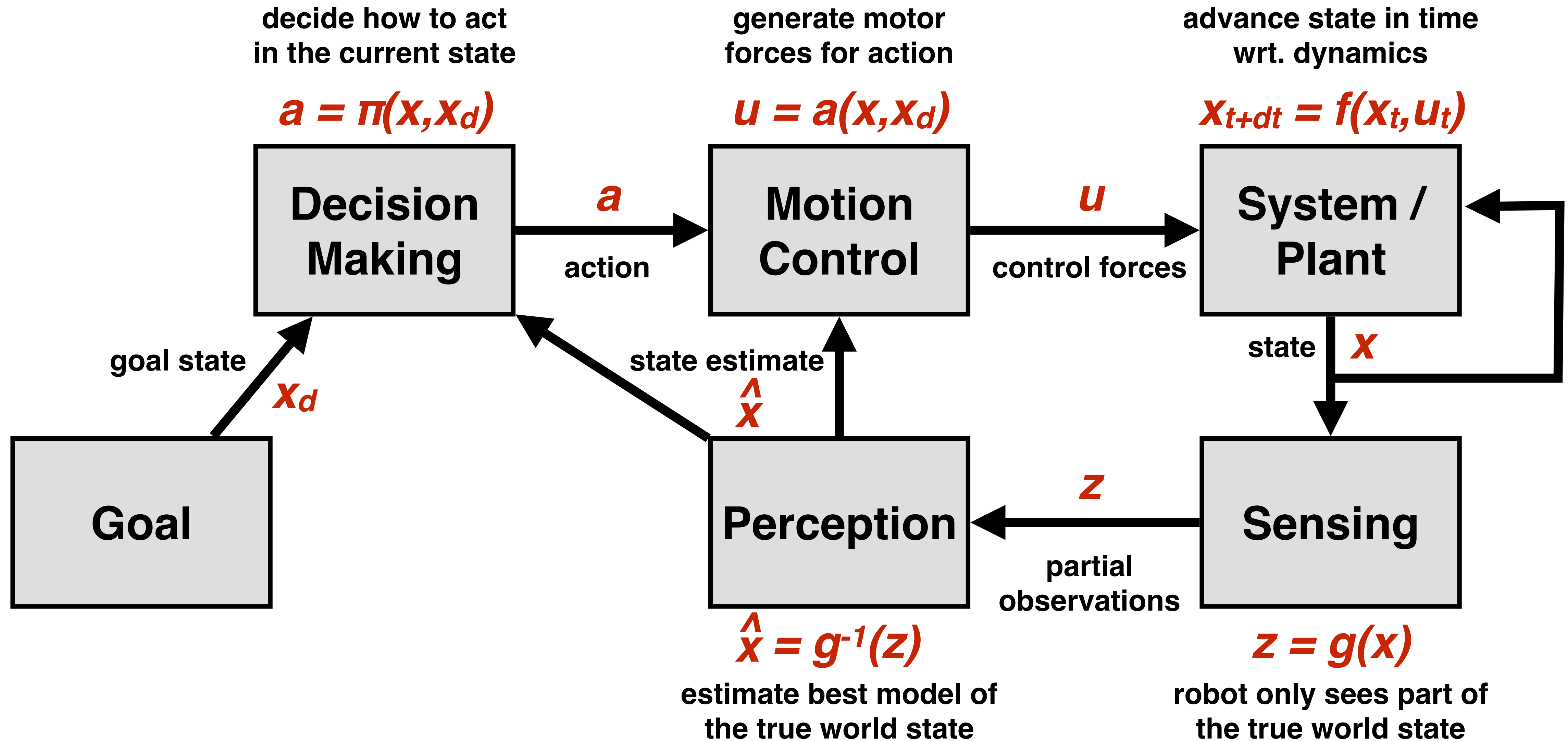
Decision Making



Robot Control Loop

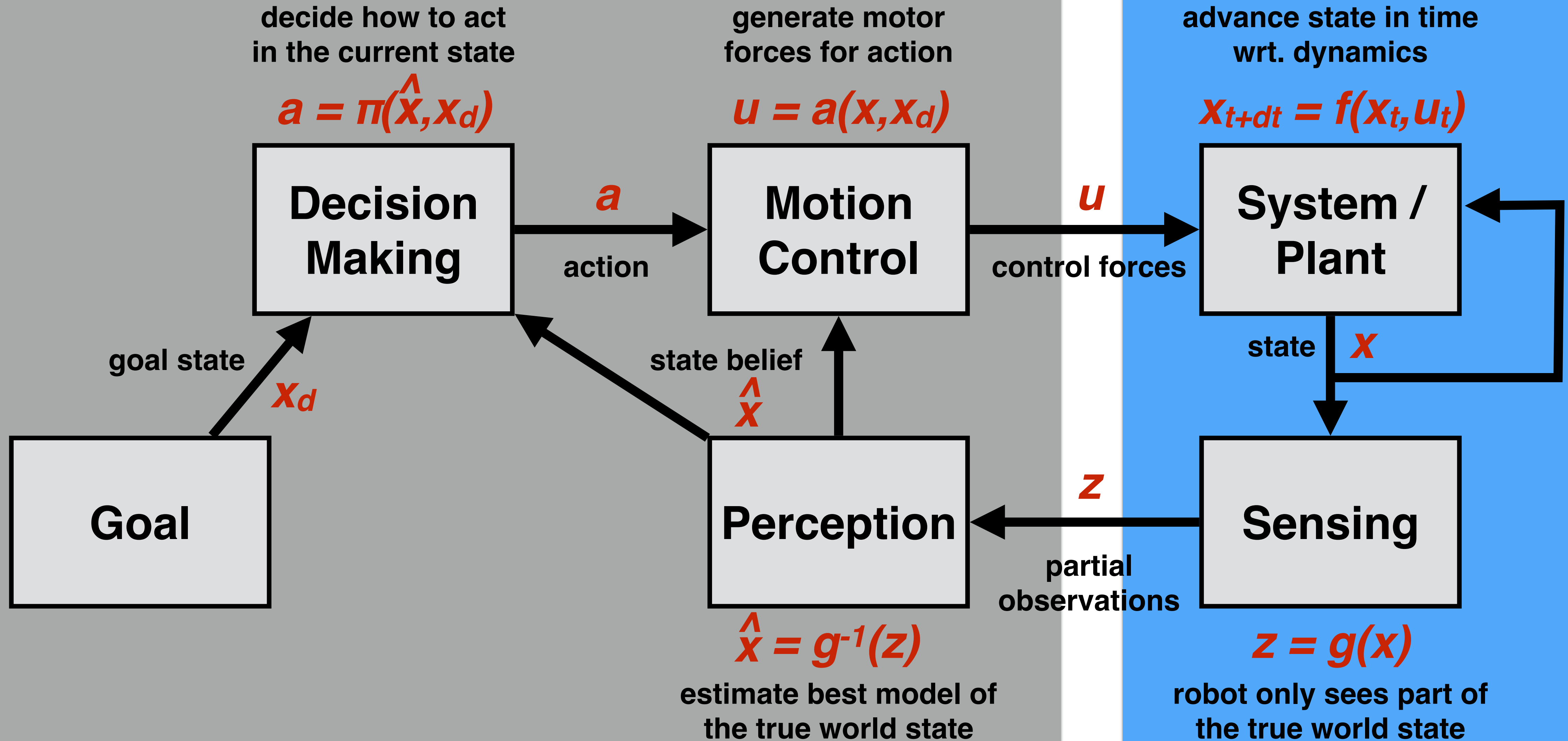


Robot Control Loop



Autonomy

Embodiment



App

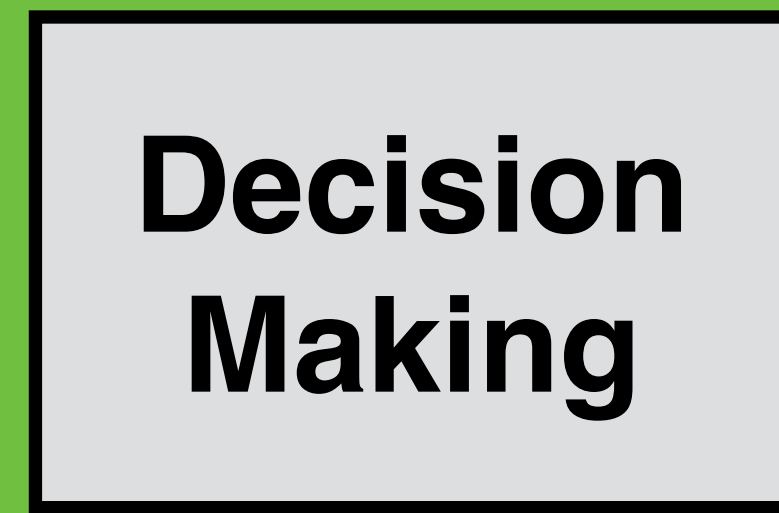
Task

State-Action

Embodiment

decide how to act
in the current state

$$a = \pi(\hat{x}, x_d)$$



a
action

generate motor
forces for action

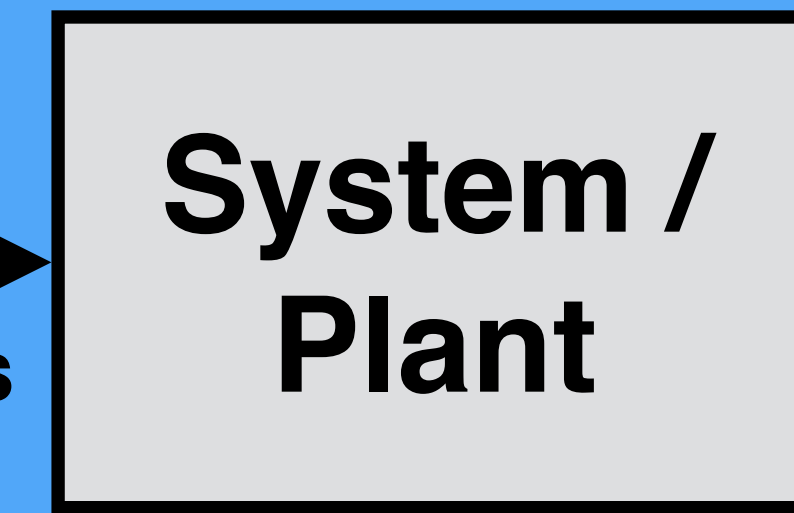
$$u = a(x, x_d)$$



u
control forces

advance state in time
wrt. dynamics

$$x_{t+dt} = f(x_t, u_t)$$



state x

Sensing

z
partial observations

Perception

state belief
 \hat{x}

$$\hat{x} = g^{-1}(z)$$

estimate best model of
the true world state

$$z = g(x)$$

robot only sees part of
the true world state

goal state

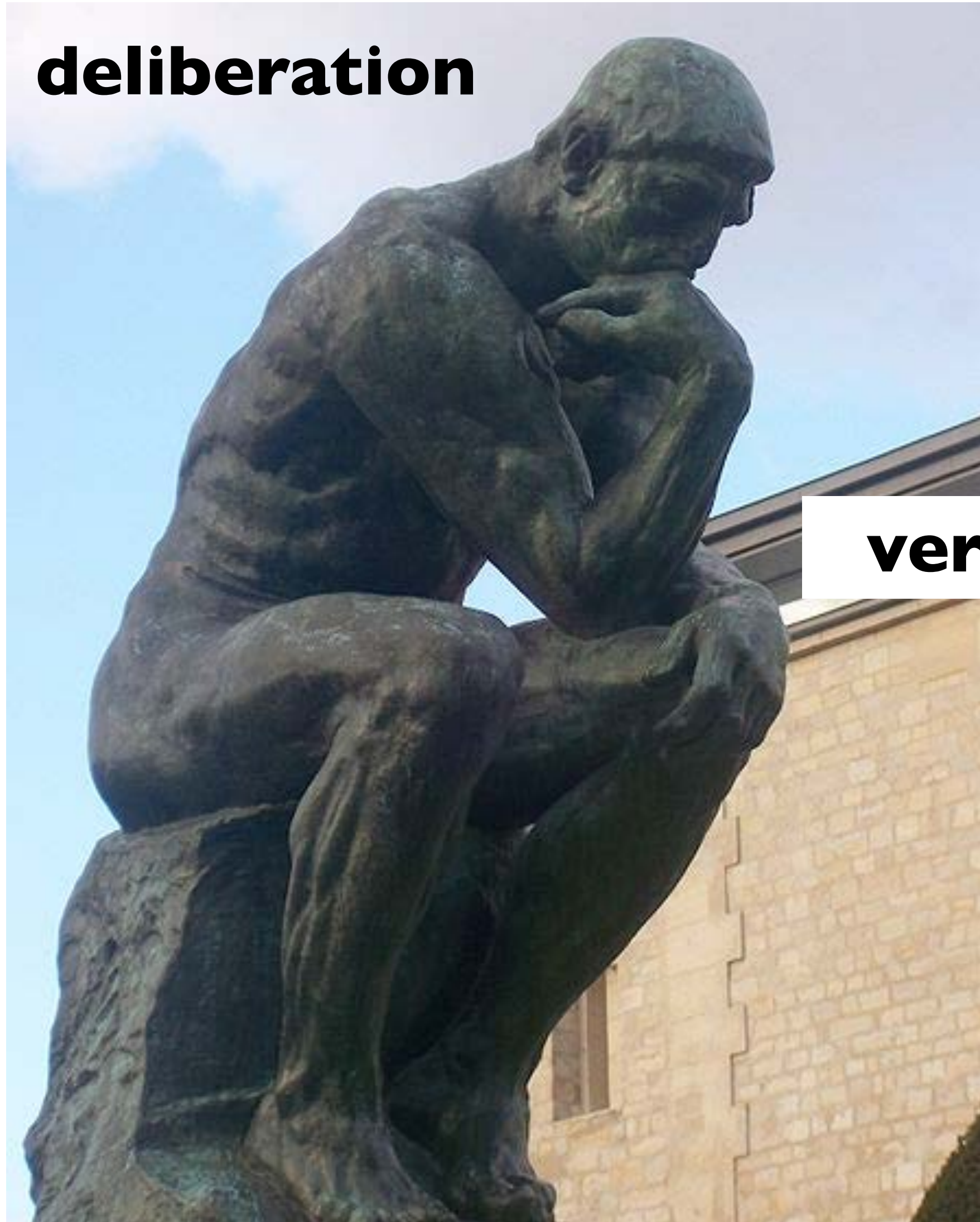
x_d

Goal



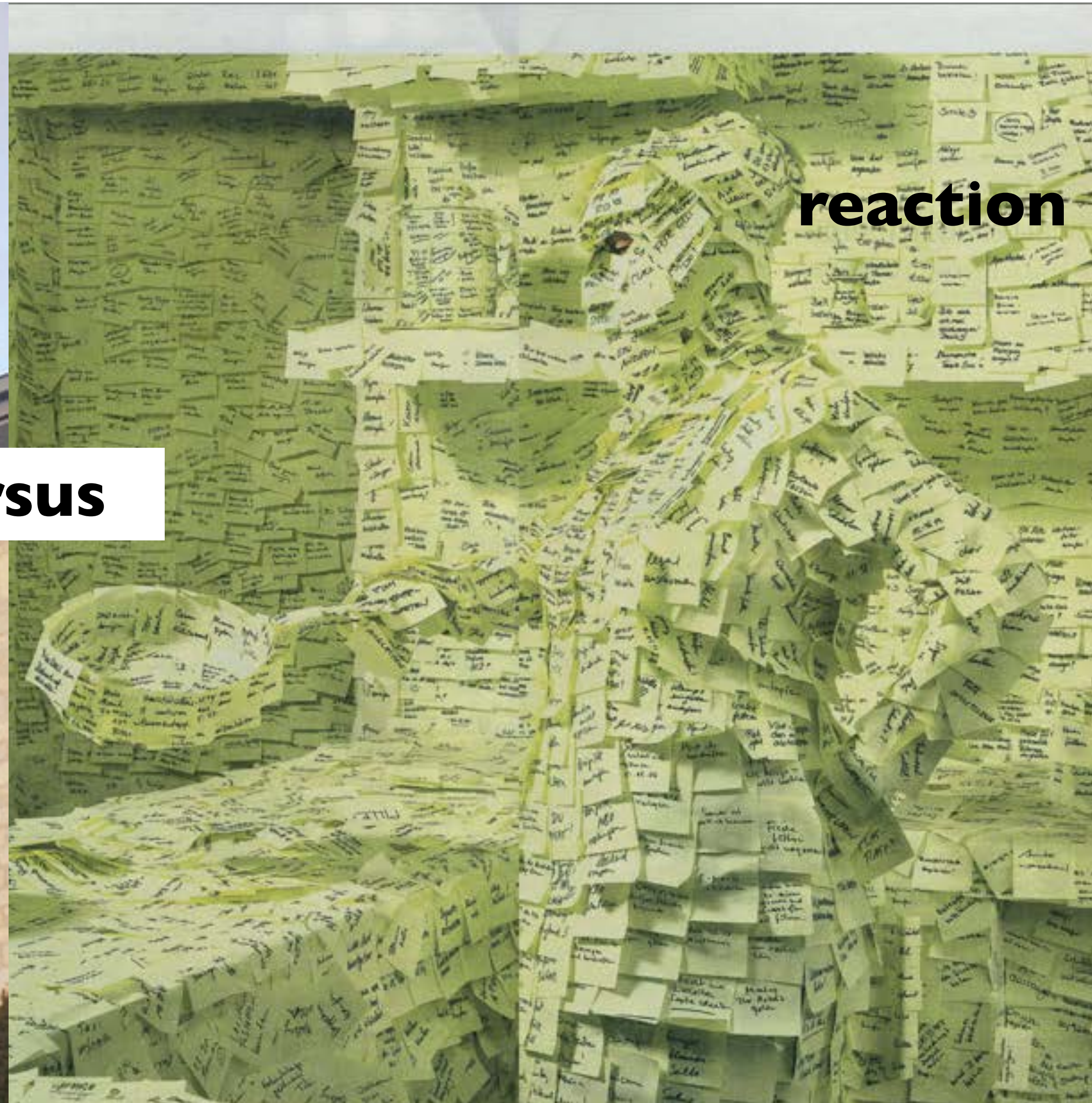
Robot Decision Making

deliberation

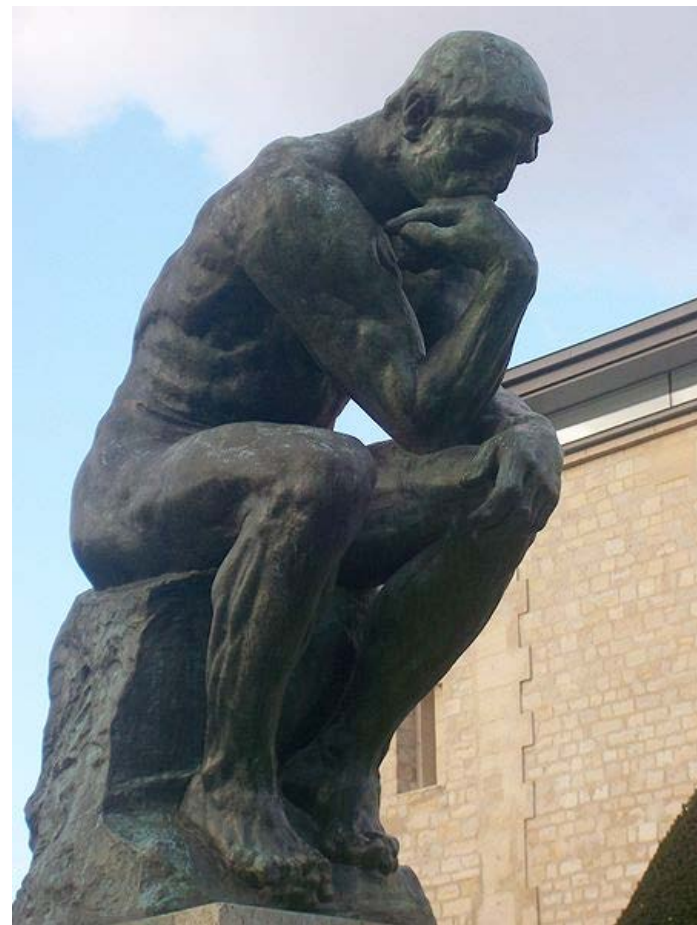
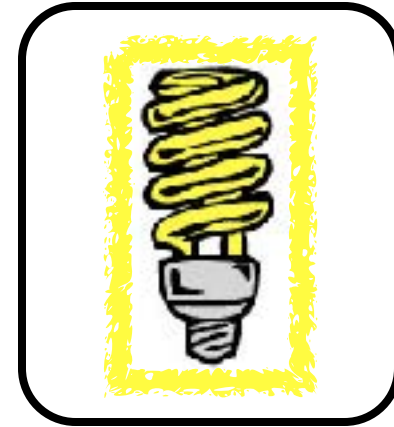


versus

reaction

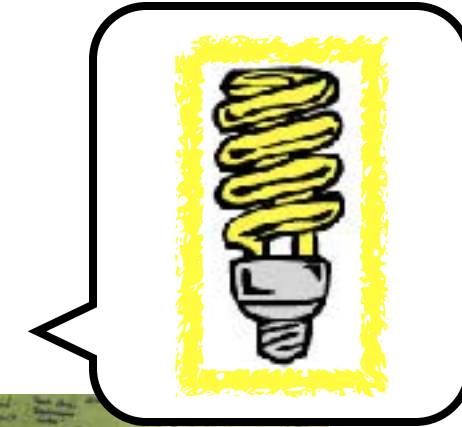


Should your robot's decision making



fully think through
solving a problem?

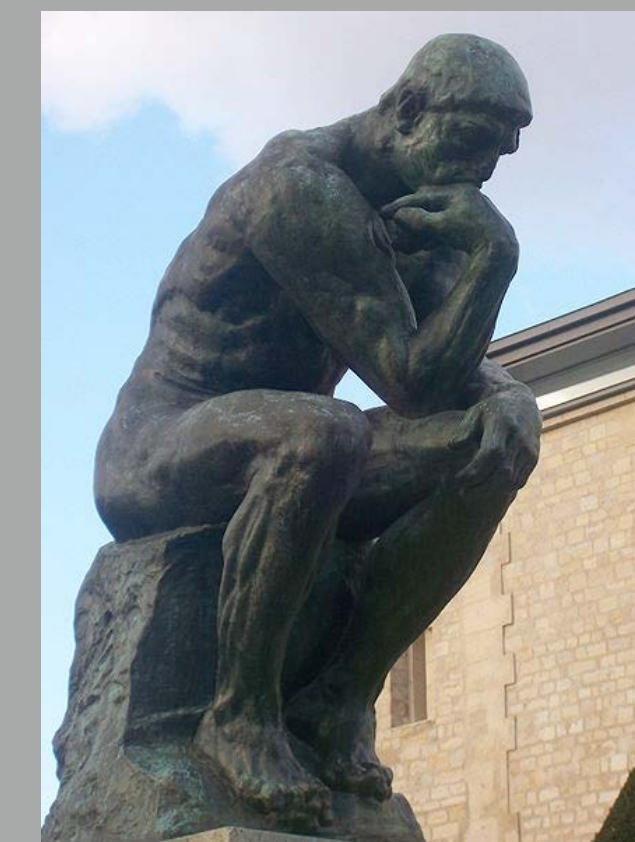
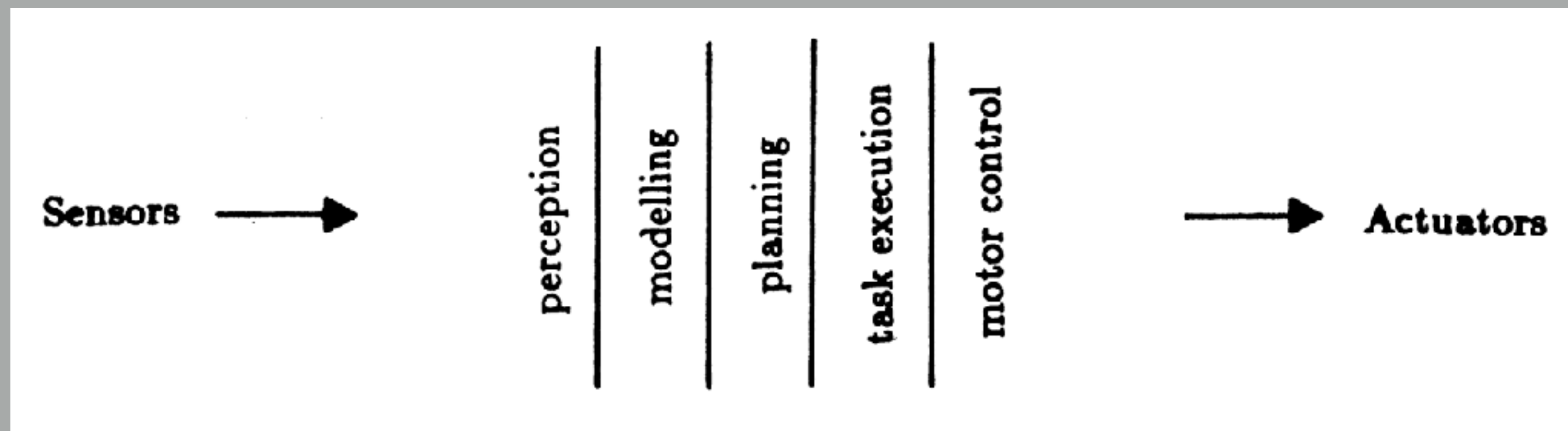
OR



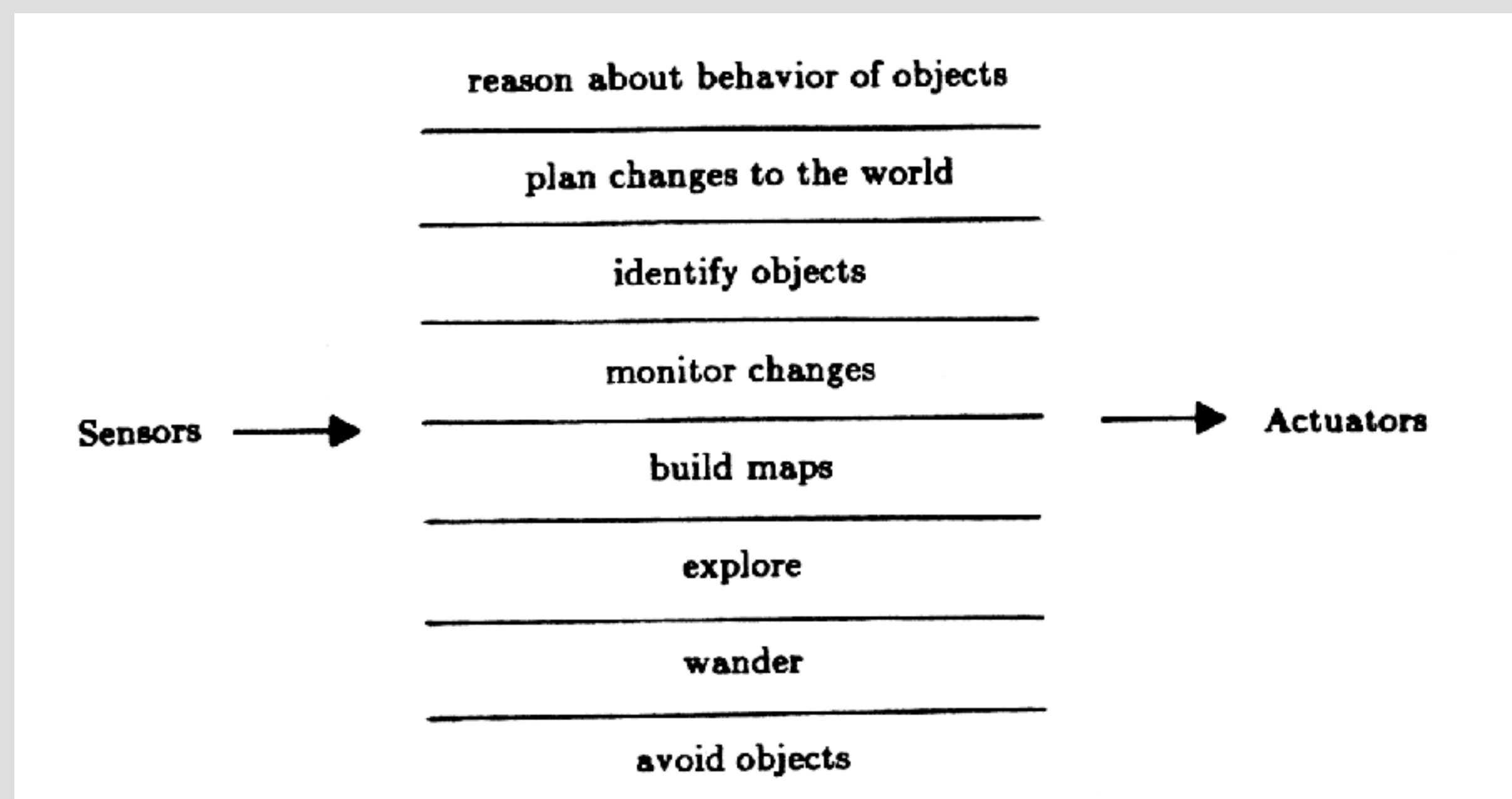
react quickly to
changes in its world?

Deliberation v. Reaction

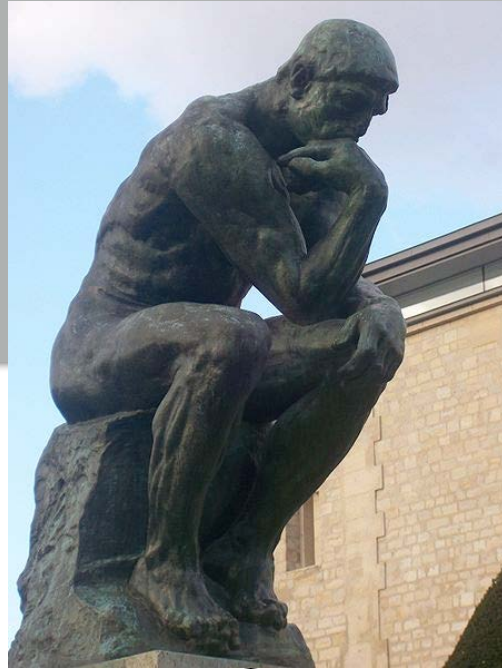
deliberative:
sense-plan-act,
path planning
motion planning



reaction:
controllers acting in parallel
subsumption,
Finite State Machine

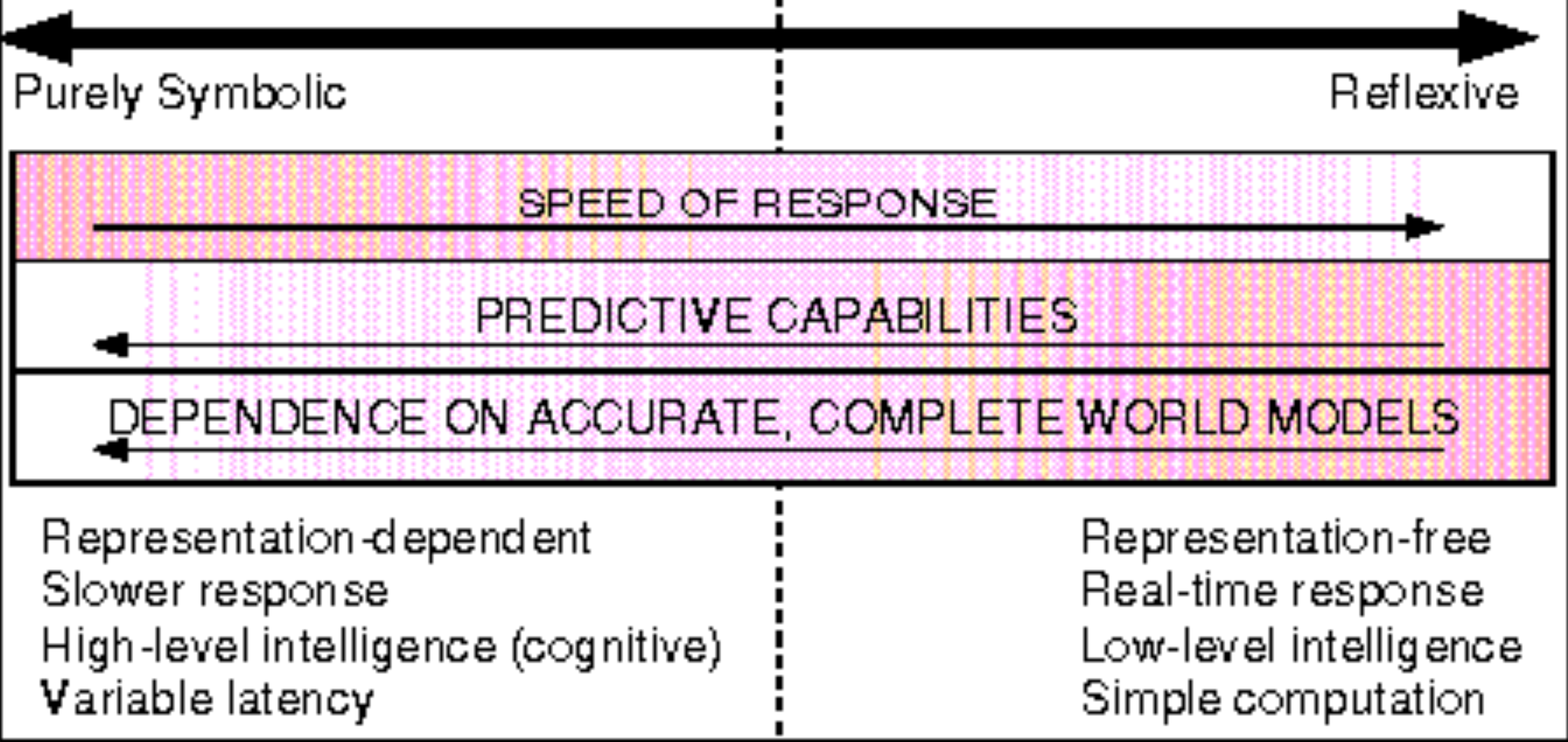


Deliberation-Reaction spectrum



DELIBERATIVE

REACTIVE



Complete
Adaptive
Optimal
Slower

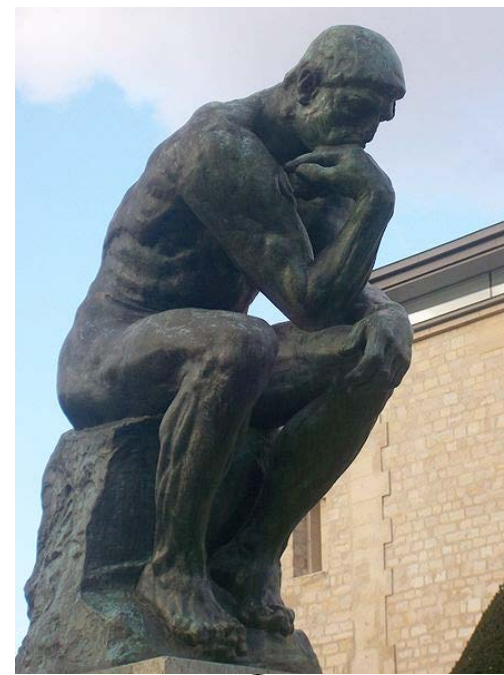
Faster
Cheaper
More robust
Forgetful

Requires
complete model
of the world

Requires a
complete design
of the problem



Examples?



DELIBERATIVE

REACTIVE

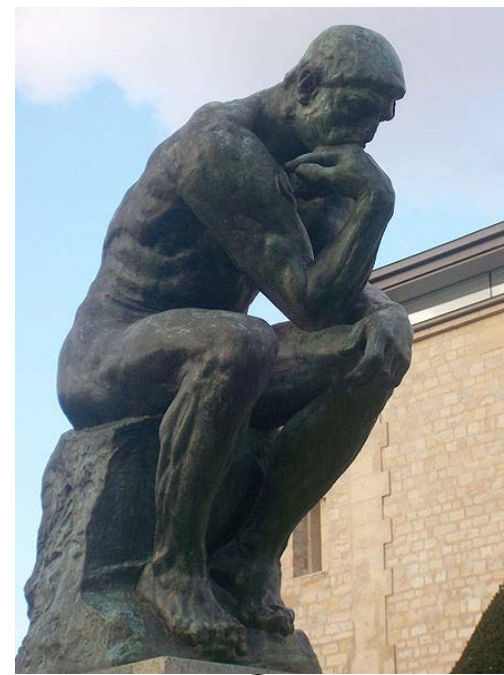


Purely Symbolic

Reflexive

example???

Examples?



DELIBERATIVE

REACTIVE



Purely Symbolic

Reflexive



<https://www.youtube.com/watch?v=jCB3pd-wBw0>

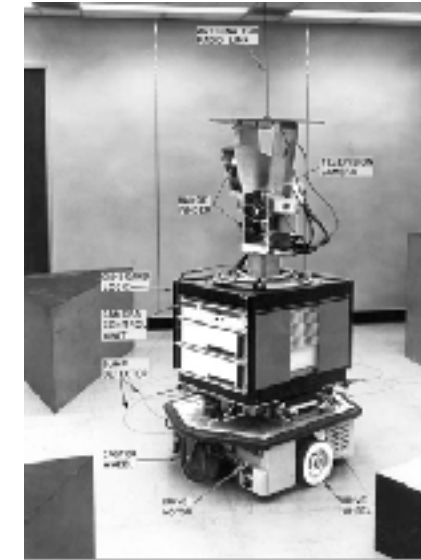


Deliberation

“Sense-Plan-Act” paradigm

- sense: build most complete model of world
 - GPS, SLAM, 3D reconstruction, affordances
- plan: search over all possible outcomes
 - Graph search, Roadmap planning
- act: execute plan through motor forces
 - PID control, Model predictive control

Sensors →



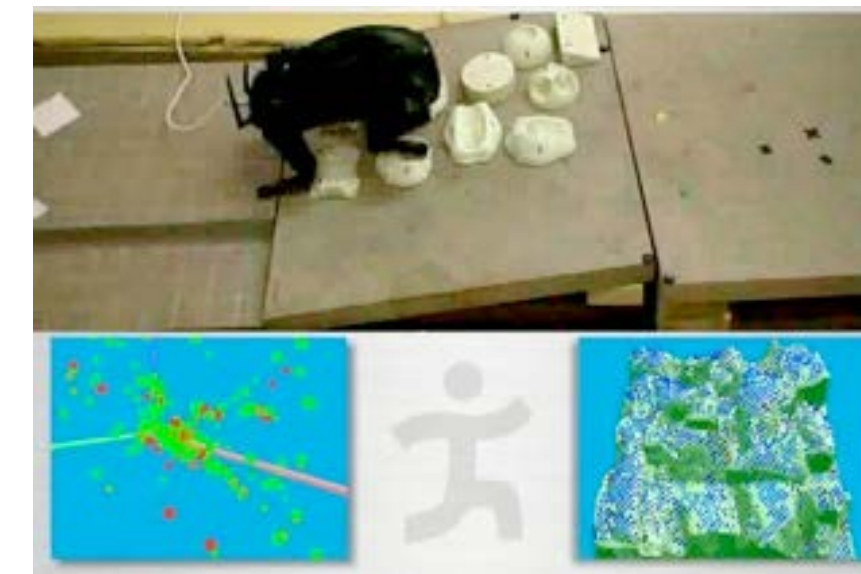
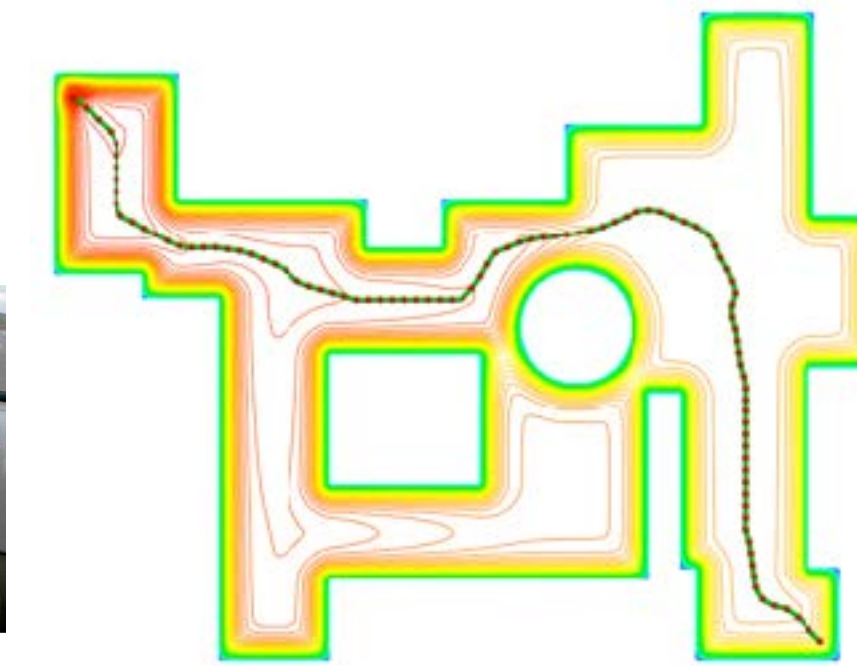
Sense

Model

Plan

Act

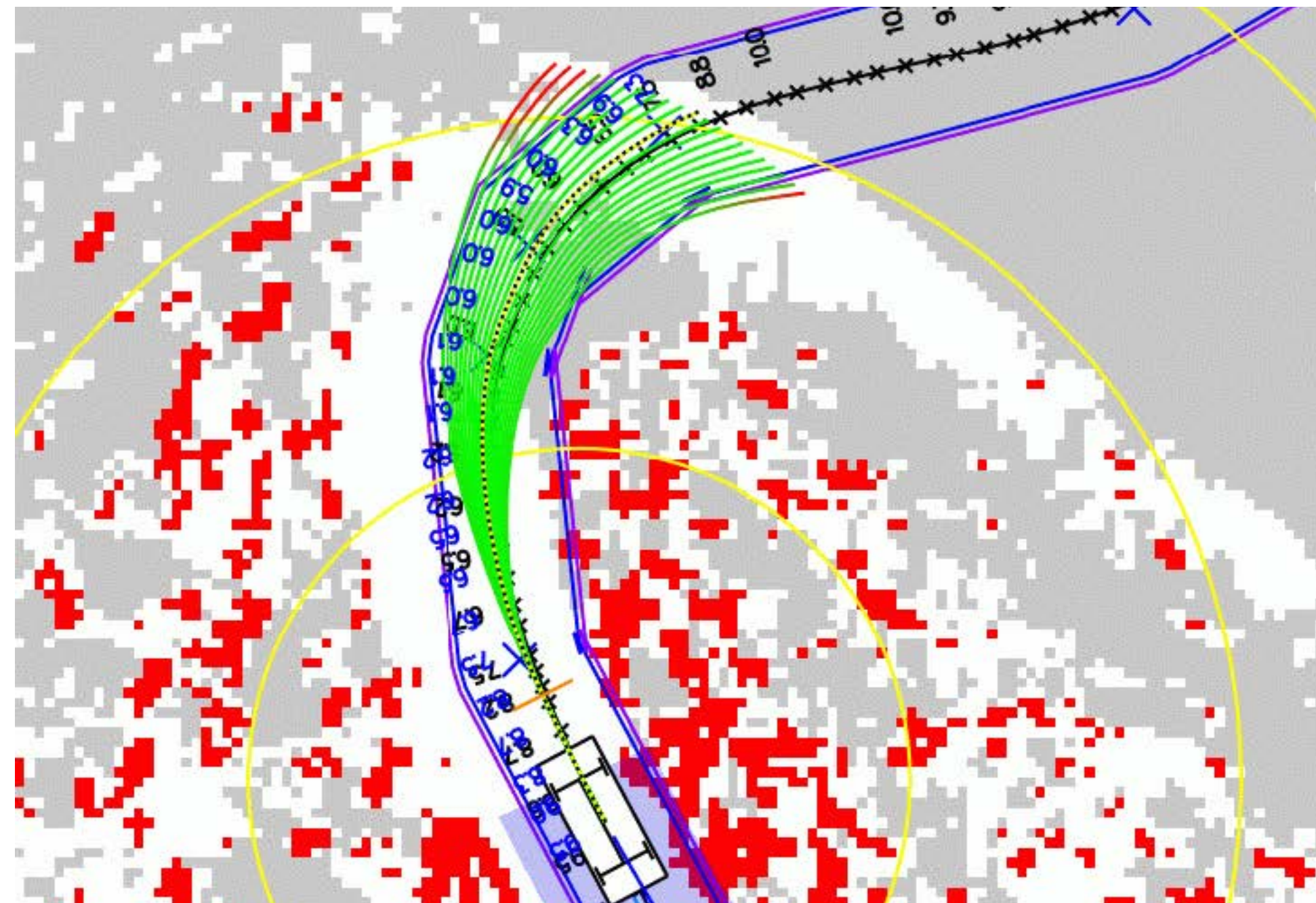
→ Actuators



Stanley (Grand Challenge)



Road detection



Navigation

2005



MIT Talos (Urban Challenge)



2007



2013



Deliberation
requires a model of the world





Color+Depth Camera



Laser Rangefinder



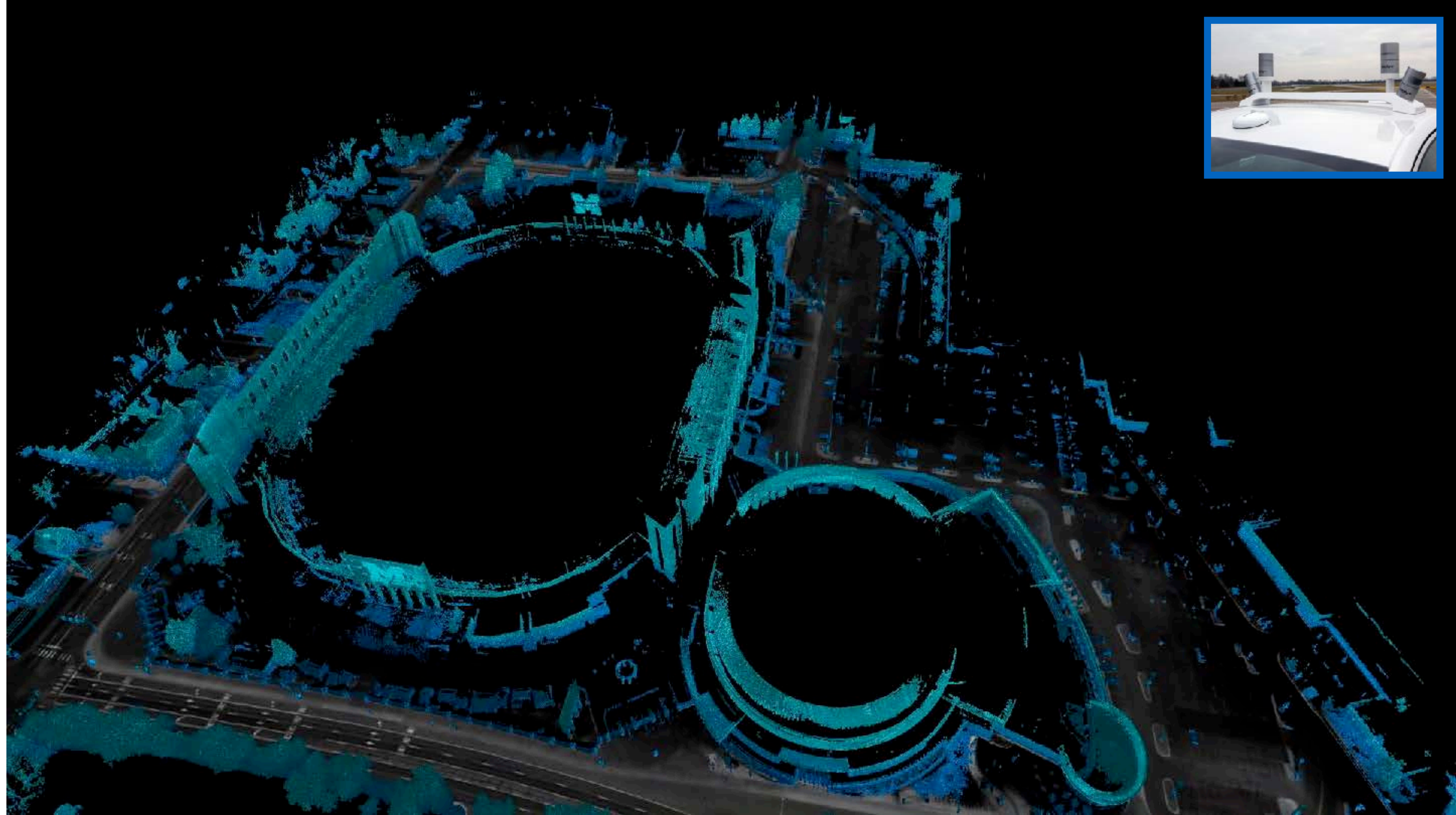
Simultaneous Localization and Mapping



Autonomous robot navigation
from previously built map



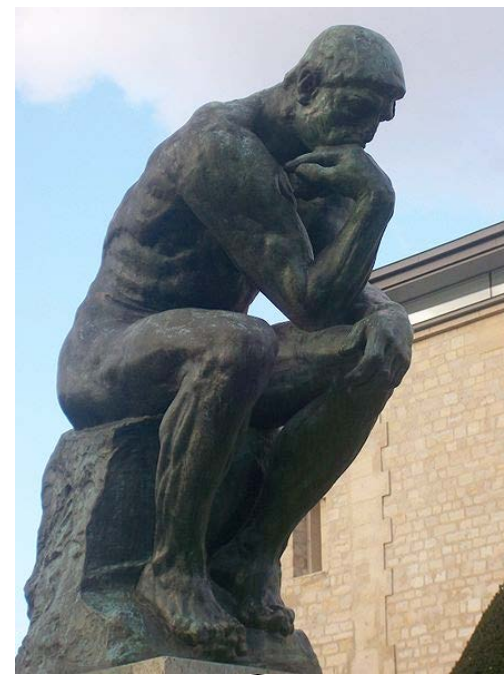
Michigan Next Generation Vehicle (Eustice, Olson et al.)



Autonomous Transportation

Michigan Next Generation Vehicle (Eustice, Olson et al.)

Examples?



DELIBERATIVE

REACTIVE



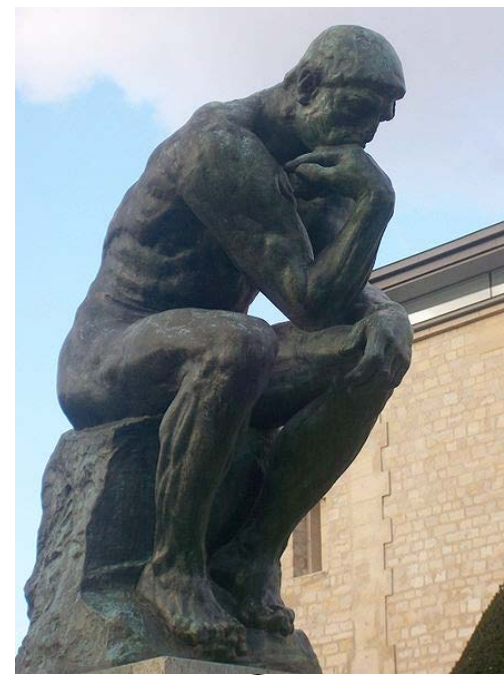
Purely Symbolic

Reflexive



**more common
example???**

Examples?



DELIBERATIVE



REACTIVE

Purely Symbolic

Reflexive



Reaction

- No representation of state
 - Typically, fast hardcoded rules
- Embodied intelligence
 - behavior \leftarrow control + embodiment
 - Stigmergy (e.g, ant scouts using pheromones)
- Finite State Machines
 - most common
- Subsumption architecture
 - prioritized reactive policies

Sensors \longrightarrow \longrightarrow Actuators

Explore

Wander Around

Avoid Obstacles

Avoid Collision



Roomba cleaning pattern



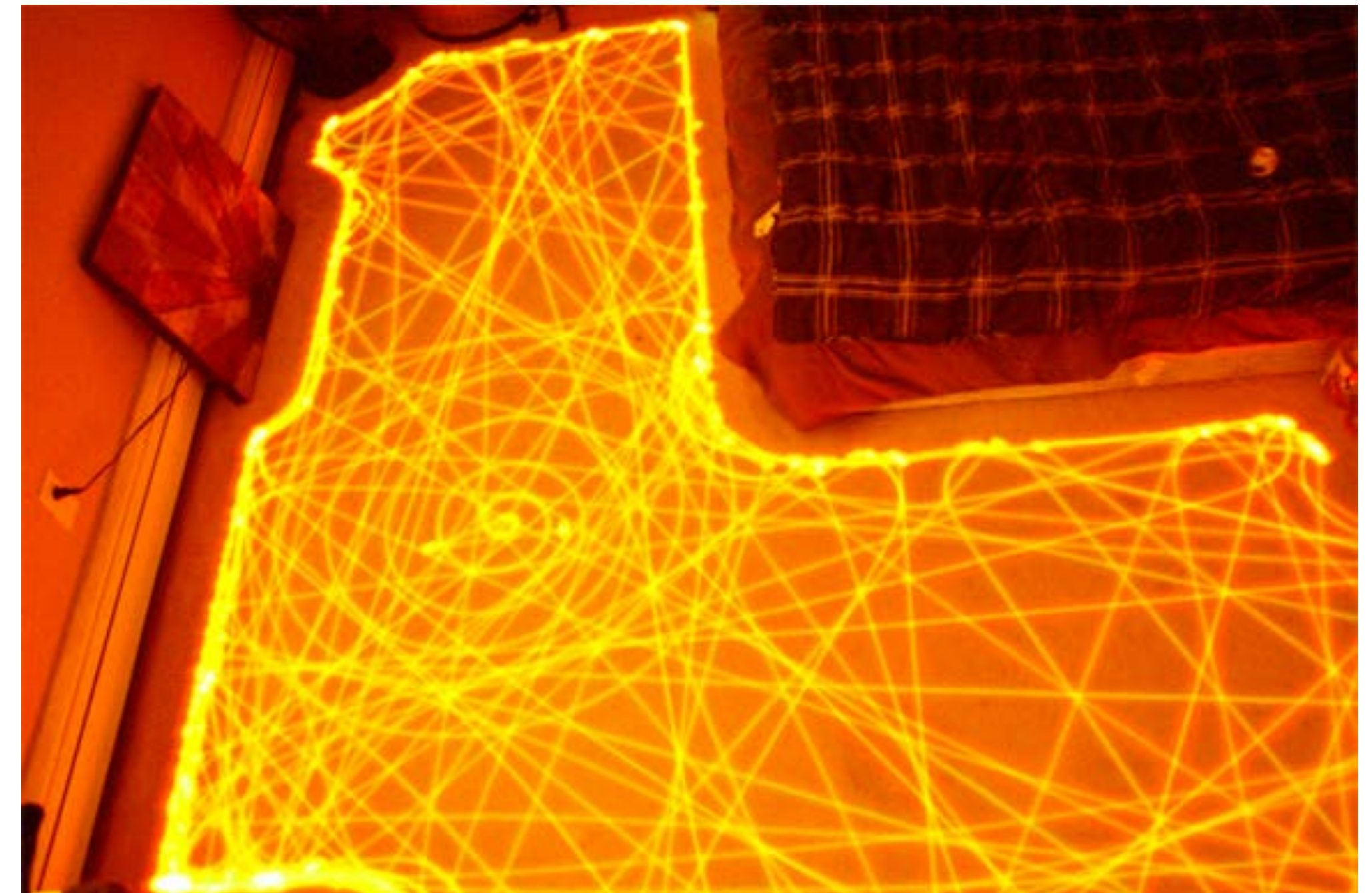
roomba cleaning "pattern"



miro ledajaks

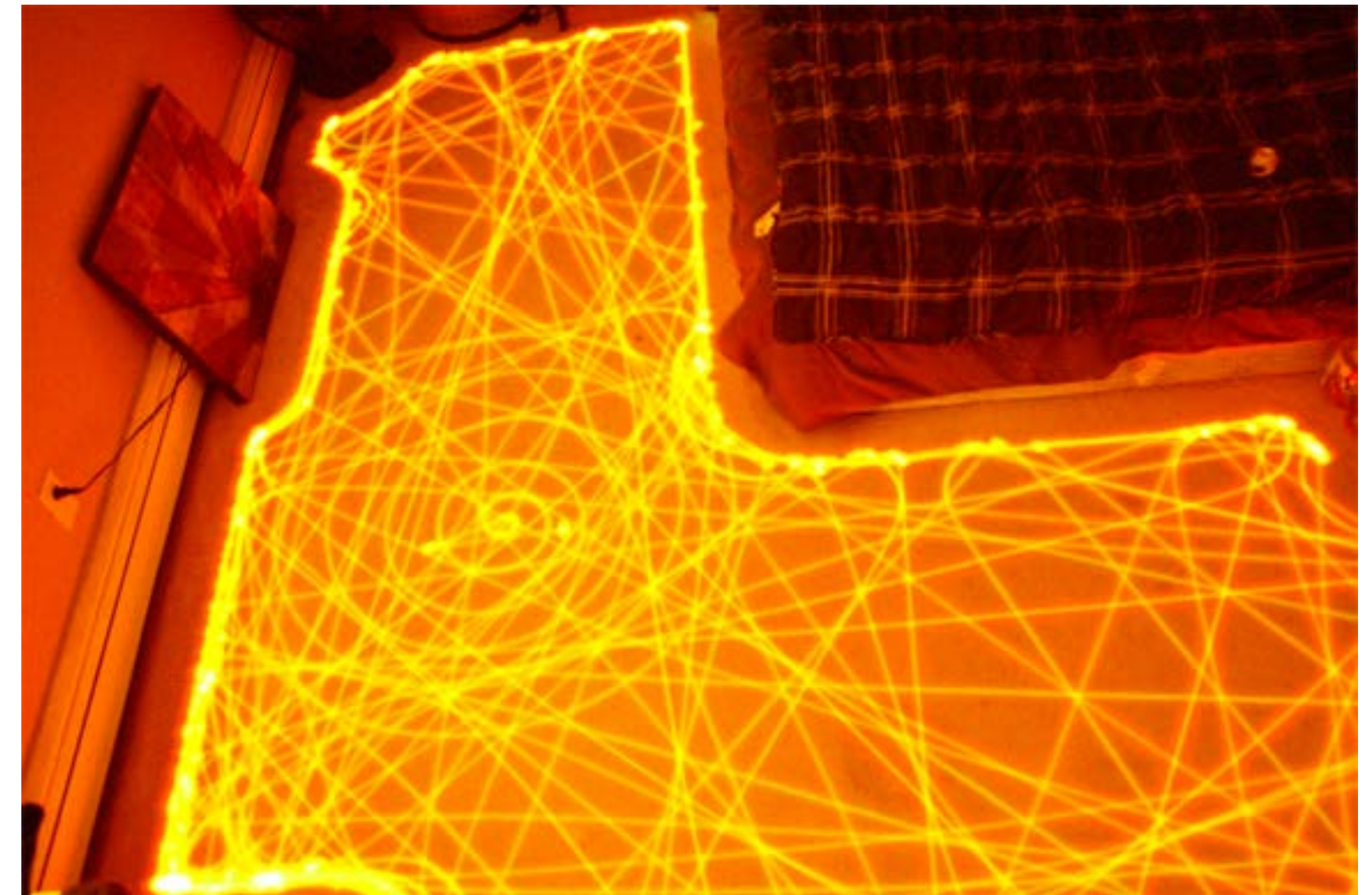
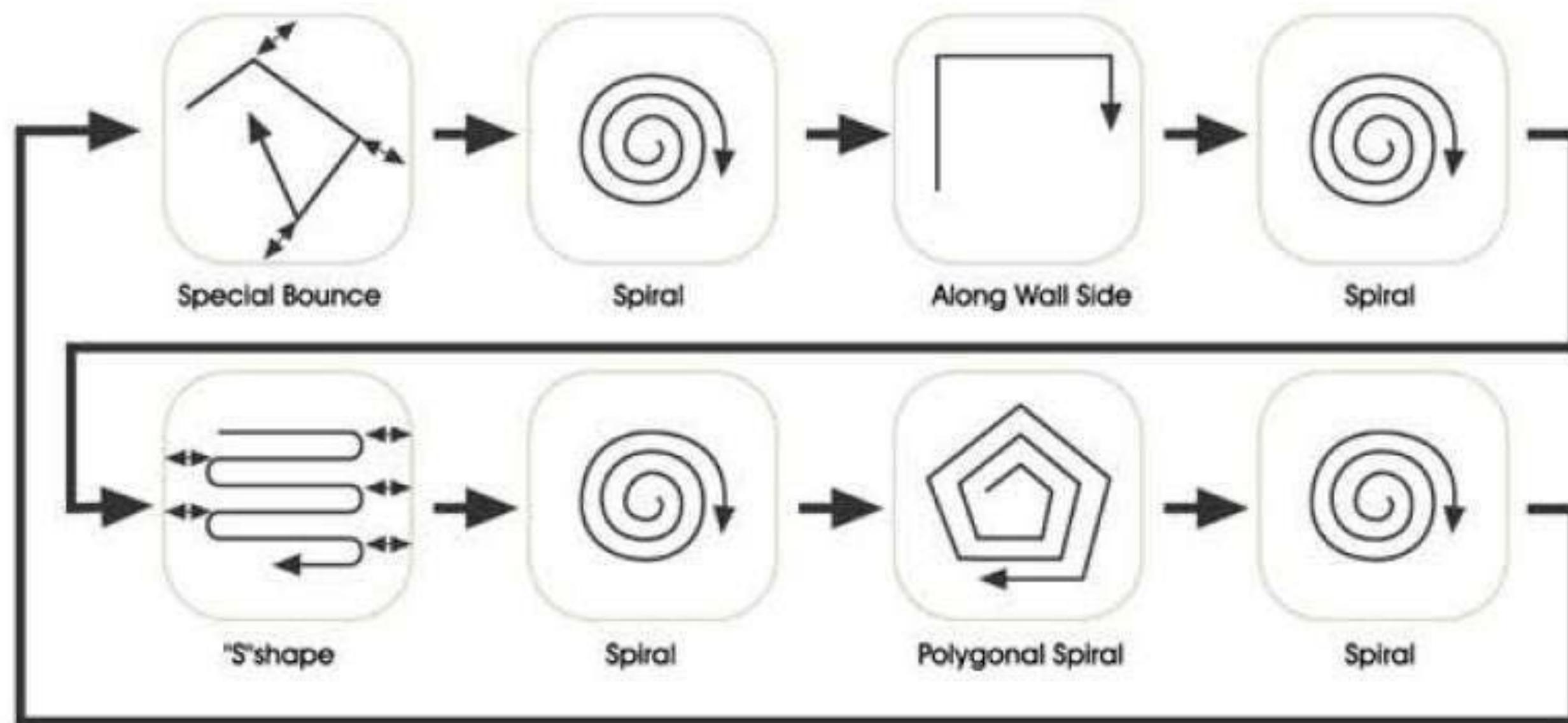


196 views

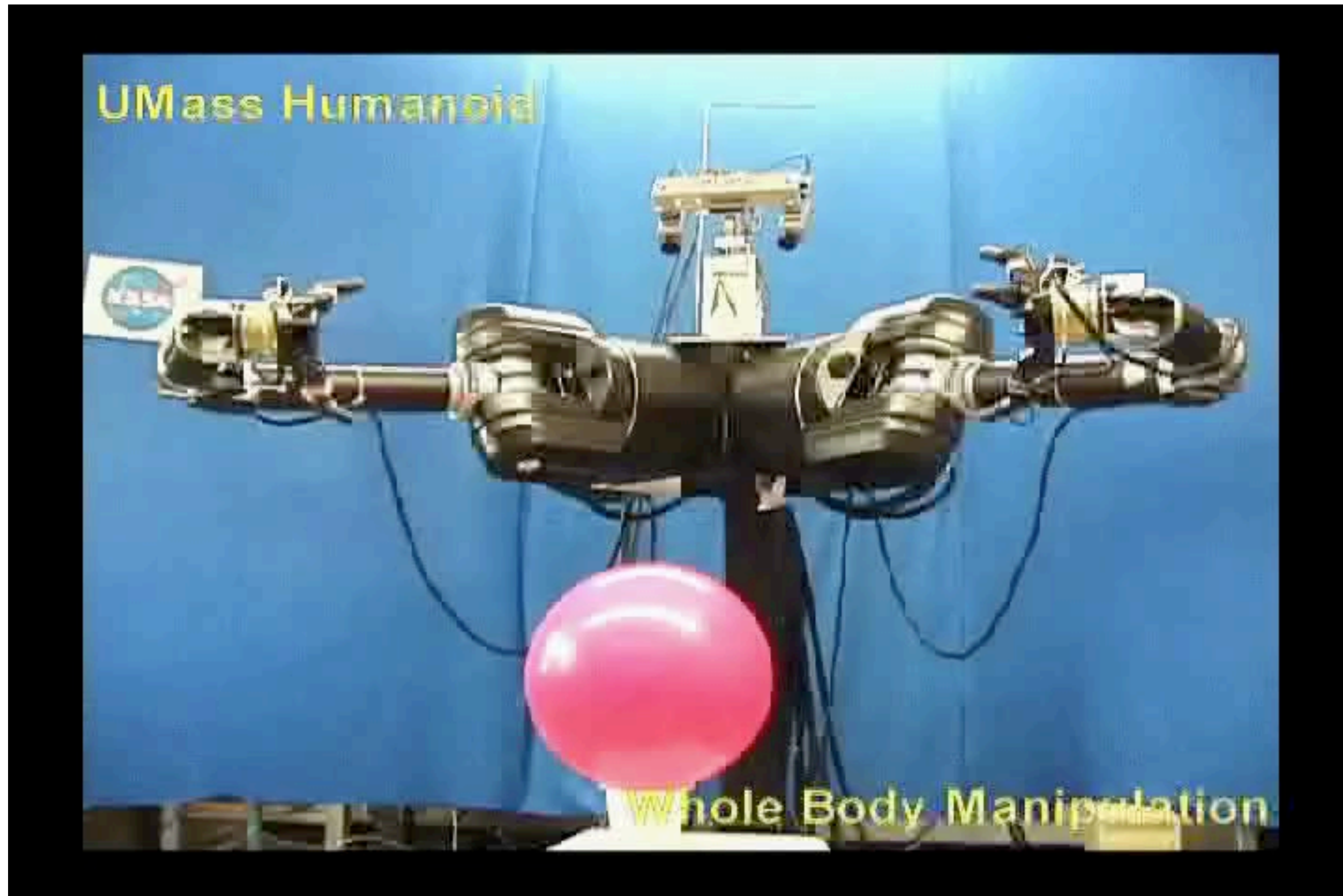


<https://www.youtube.com/watch?v=G4ocrevf4ng>

Vacuuming Finite State Machine



Manipulation Gaits



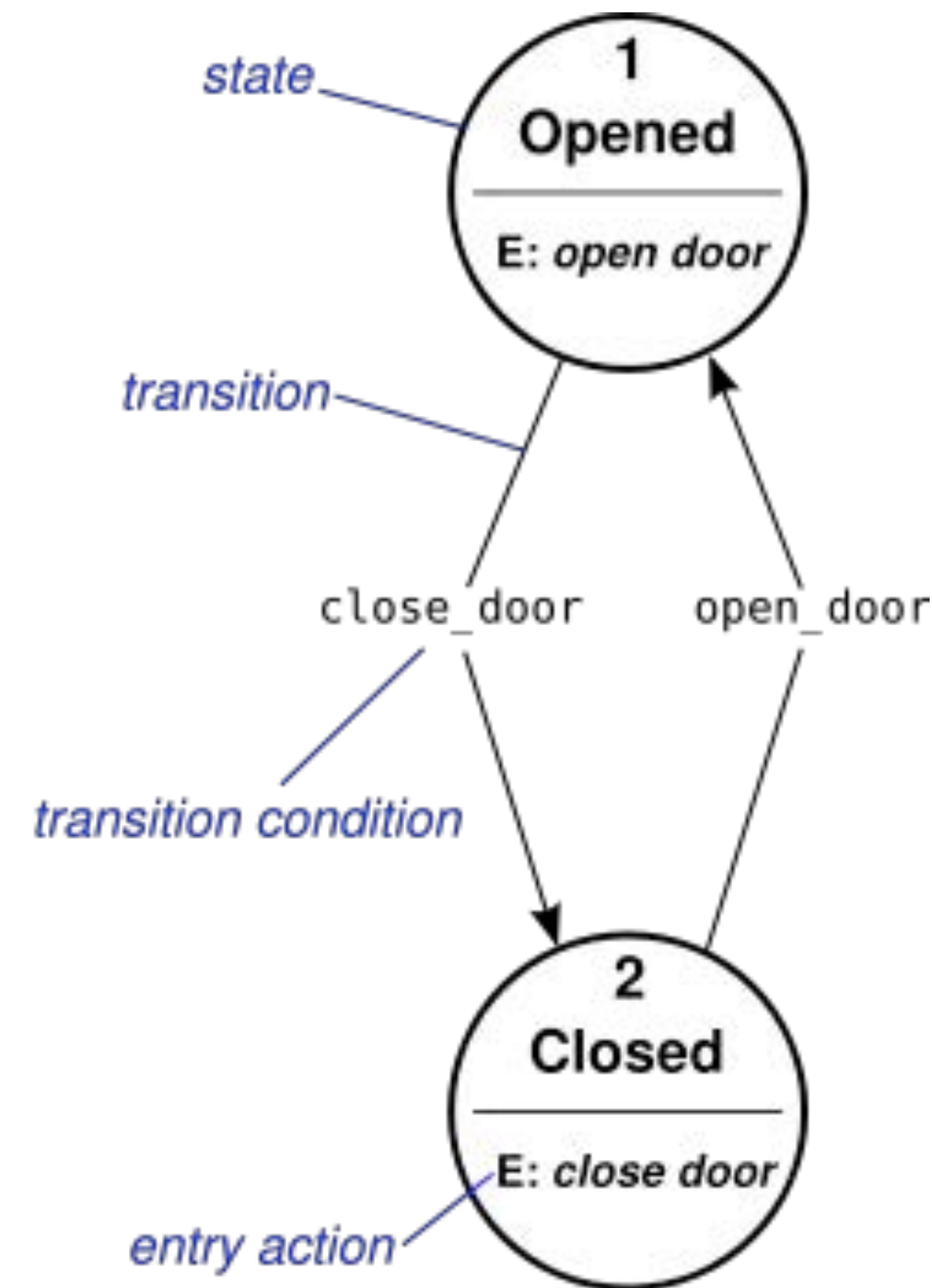
Collections of robust manipulation controllers

How do we computationally
represent reactive control?



Finite State Machines

- Components
 - alphabet (or inputs)
 - “observations” in robotics
 - states (some robot action)
 - transitions (between states)
 - stopping condition
- Commonly, implemented as switch-case or if-else within a while loop

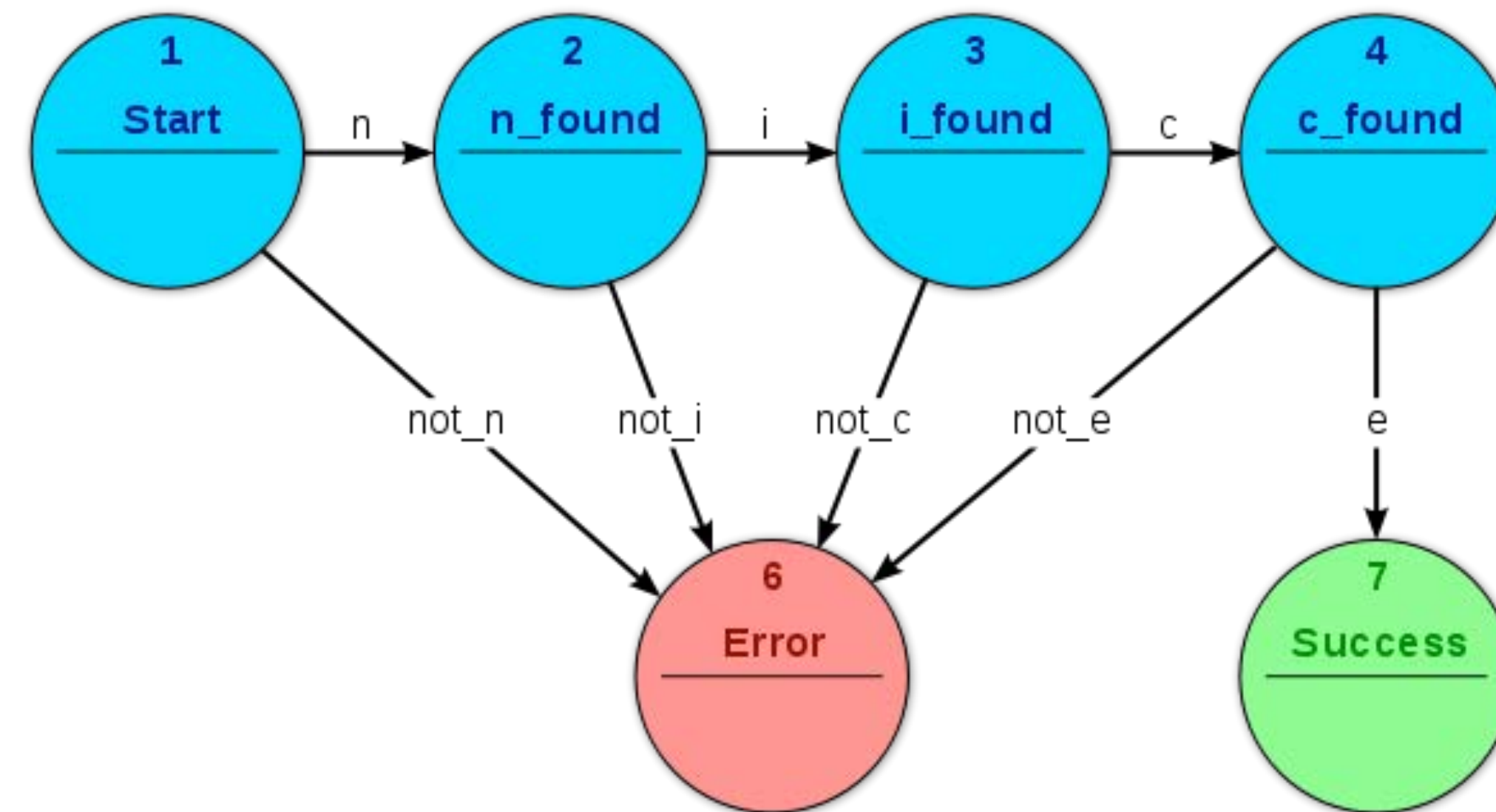


http://en.wikipedia.org/wiki/Switch_statement

“nice” recognizer

- recognize the string “nice” from input

- if input is “nice”
 - output **success**
- if input not “nice”
 - output **error**



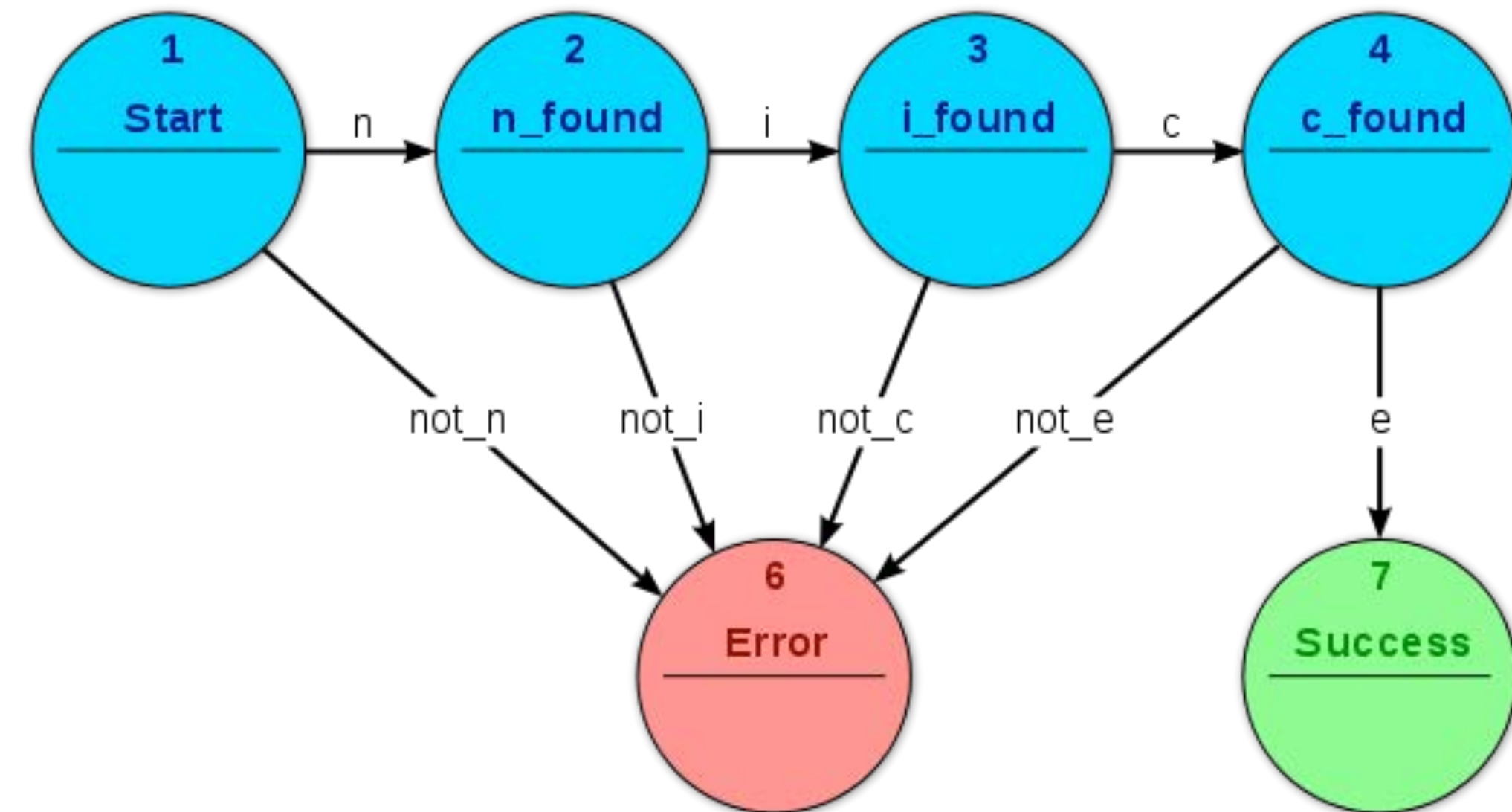
- robotics uses
 - preconditions (enter state)
 - postconditions (exit state)

```

state ← start
while state != success and state != error
  token ← <next string character from input>
  switch (state):
    case start:
      if token = "n" then state ← n_found
      else state ← error
      break
    case n_found:
      if token = "i" then state ← i_found
      else state ← error
      break
    case i_found:
      if token = "c" then state ← c_found
      else state ← error
      break
    case c_found:
      if token = "e" then state ← success
      else state ← error
      break
  end while loop
output ← state

```

"nice" recognizer



Consider input: "nice"

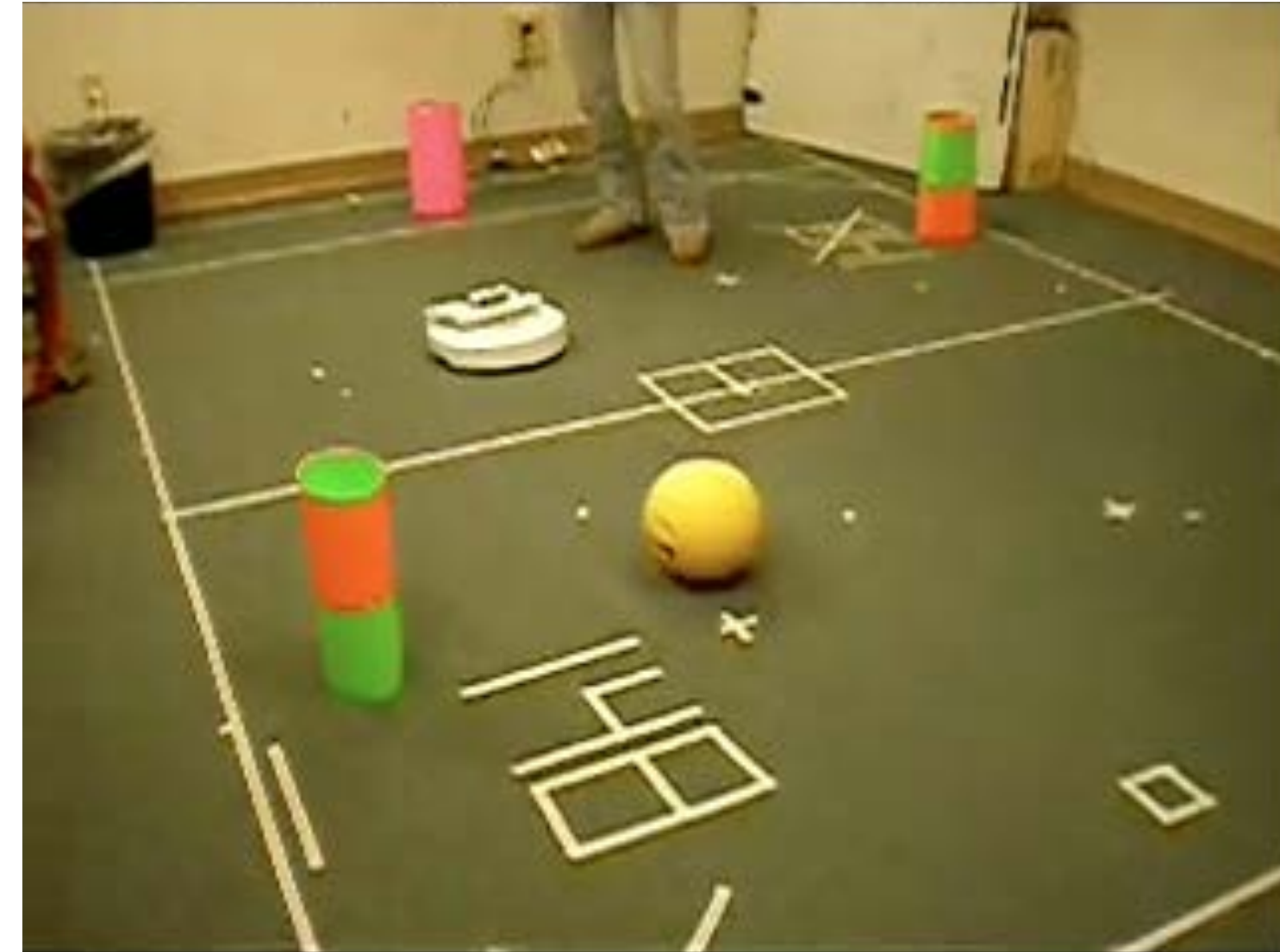
Consider input: "robotics"

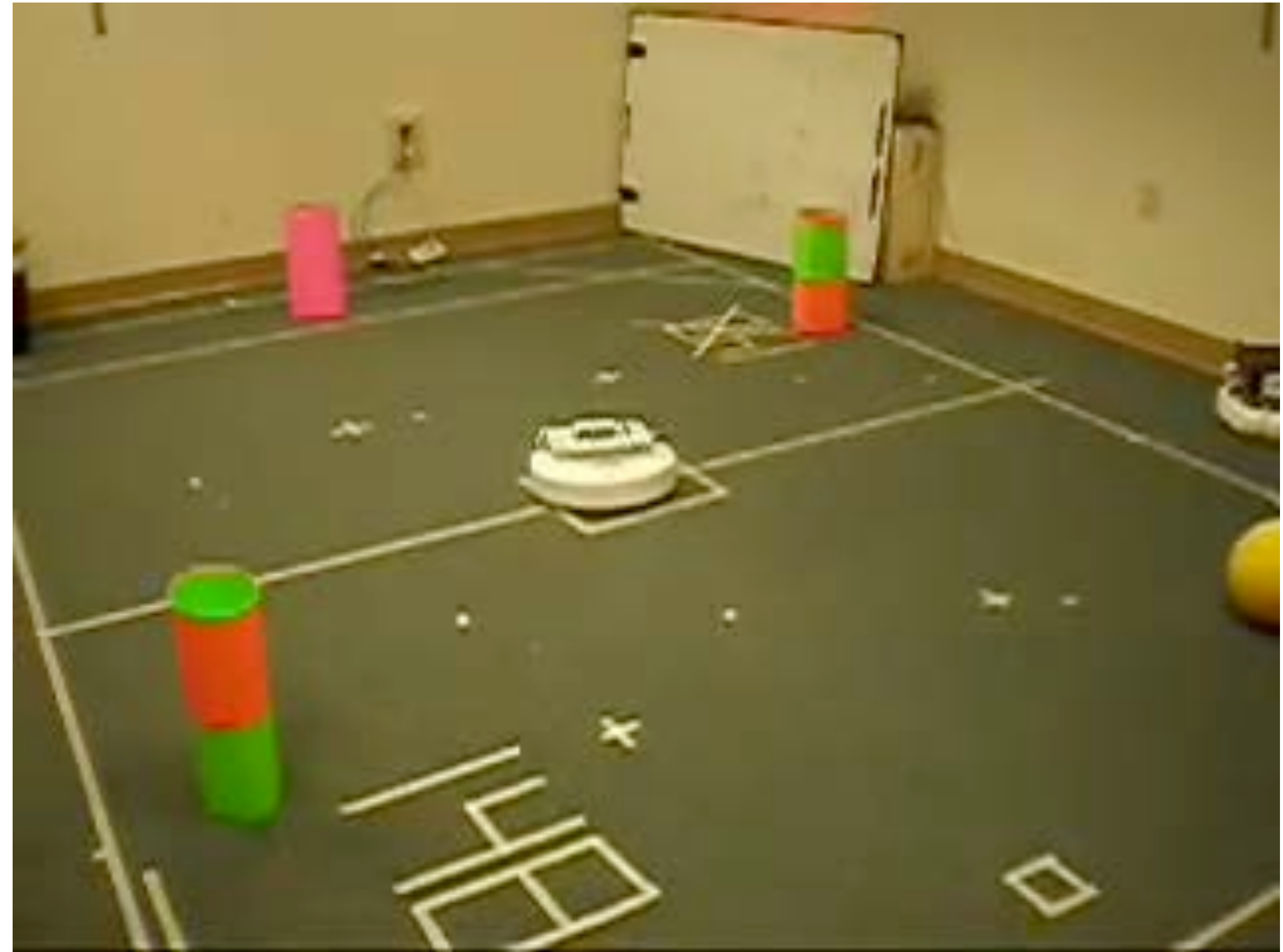
Consider input: "niece"



Move to objects in sequence?

- How to move a mobile robot to a given sequence of objects?
 - yellow ball
 - green/orange landmark
 - pink landmark
 - orange/green landmark



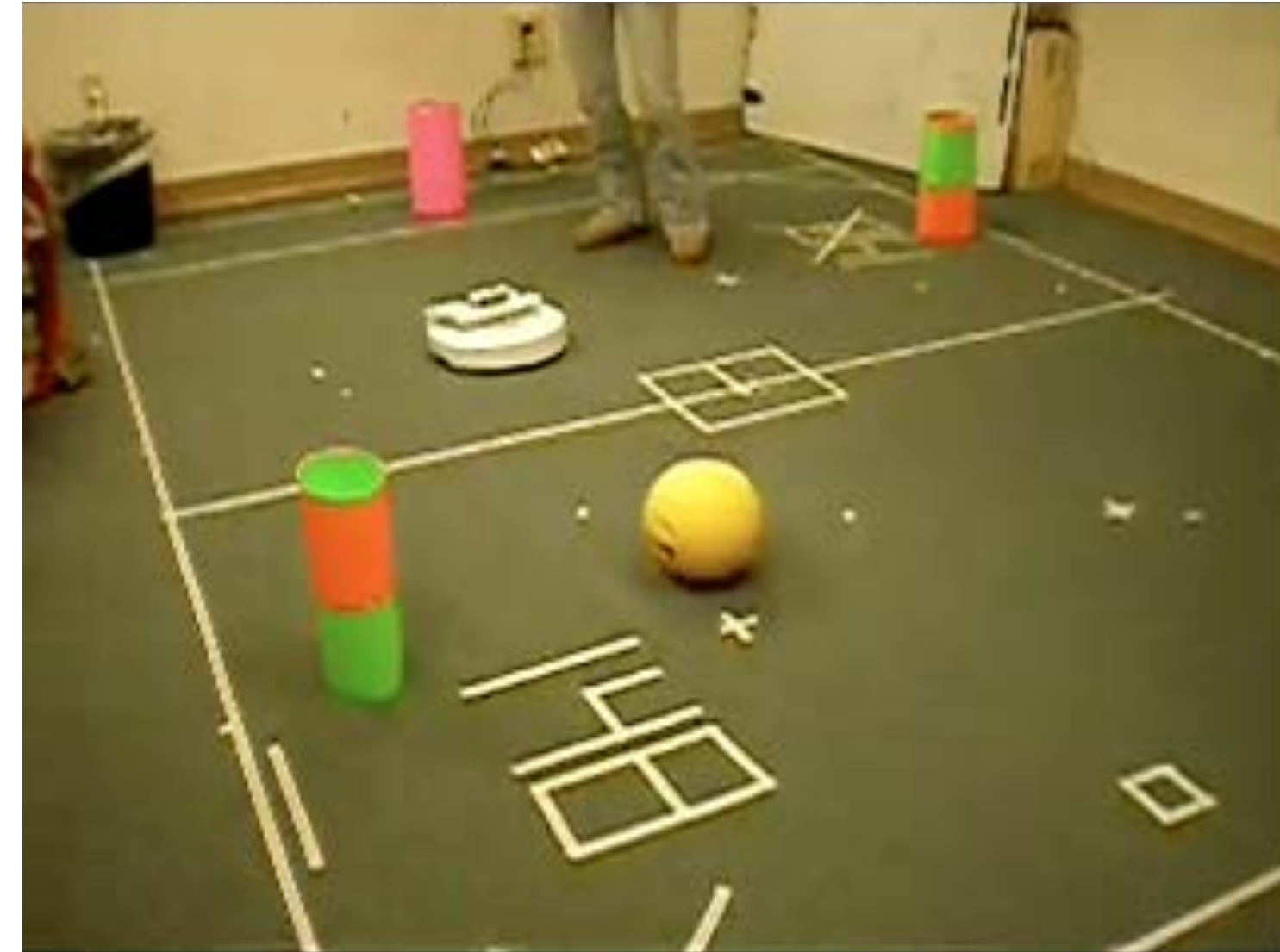


Object Seeking

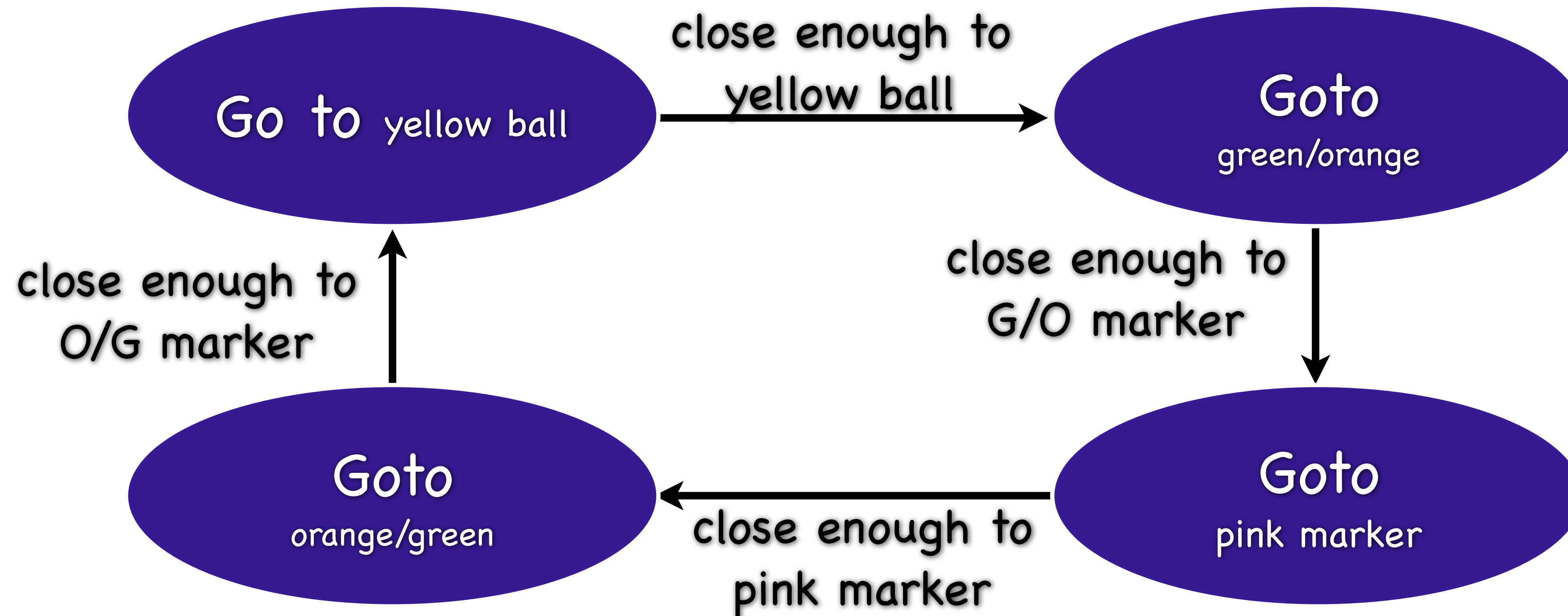
<http://www.youtube.com/watch?v=-hOA0jMUggg>

Move to objects in sequence?

- What are the states?
- What are the transitions?
- Preconditions for states?
- Postconditions for states?



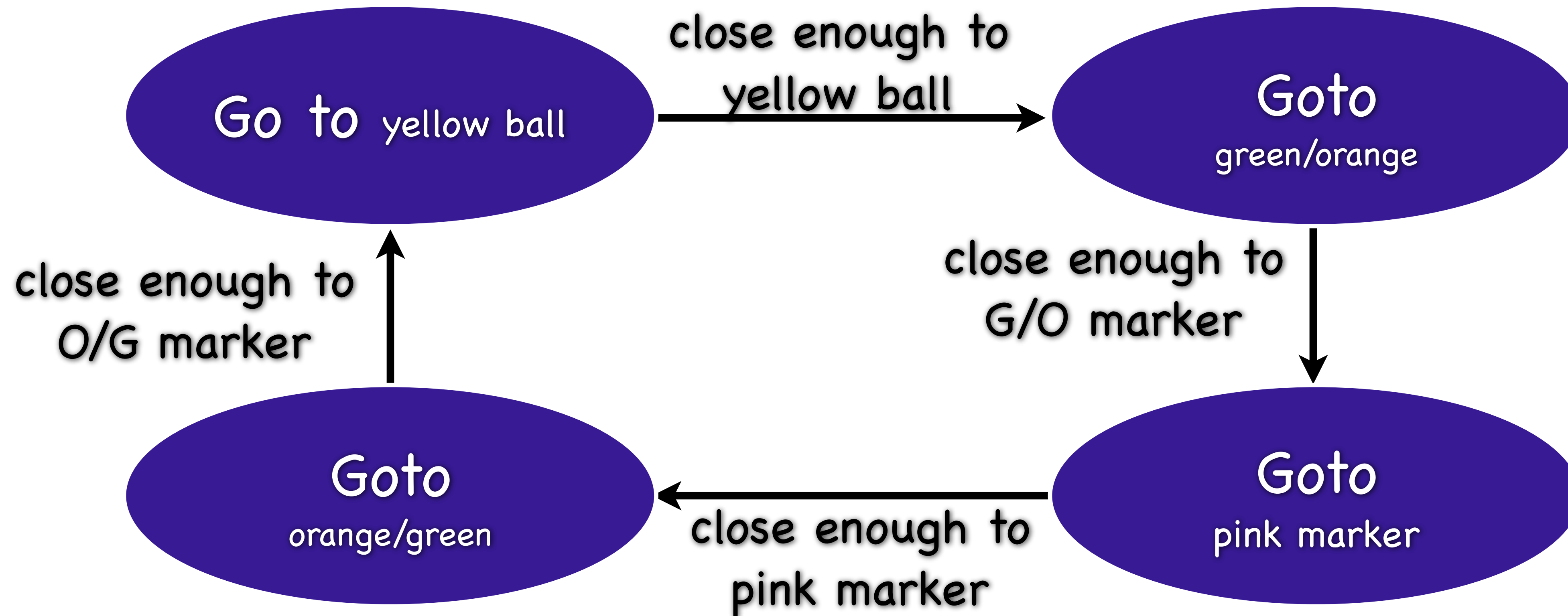
Object seeking FSM



Object seeking FSM

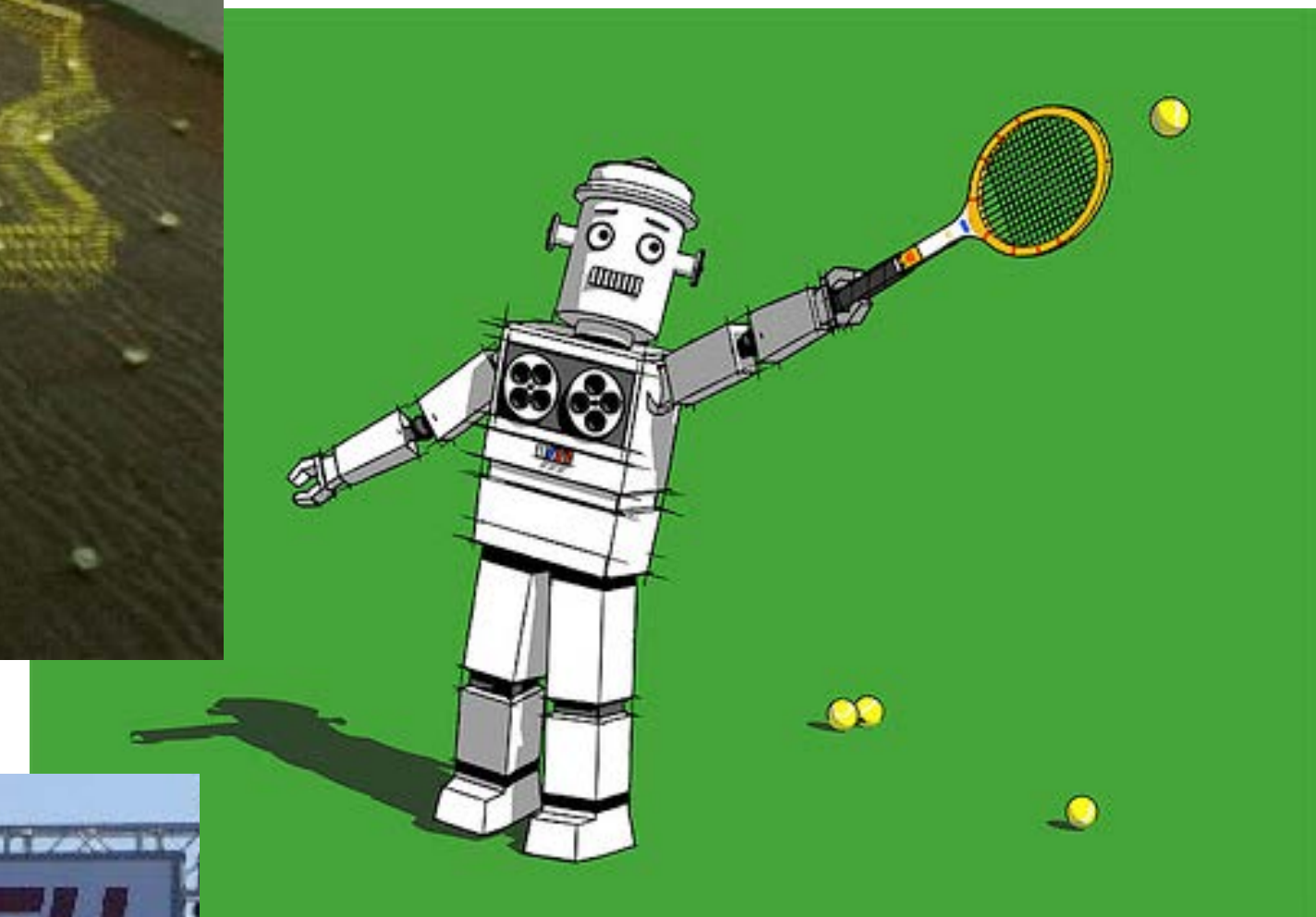
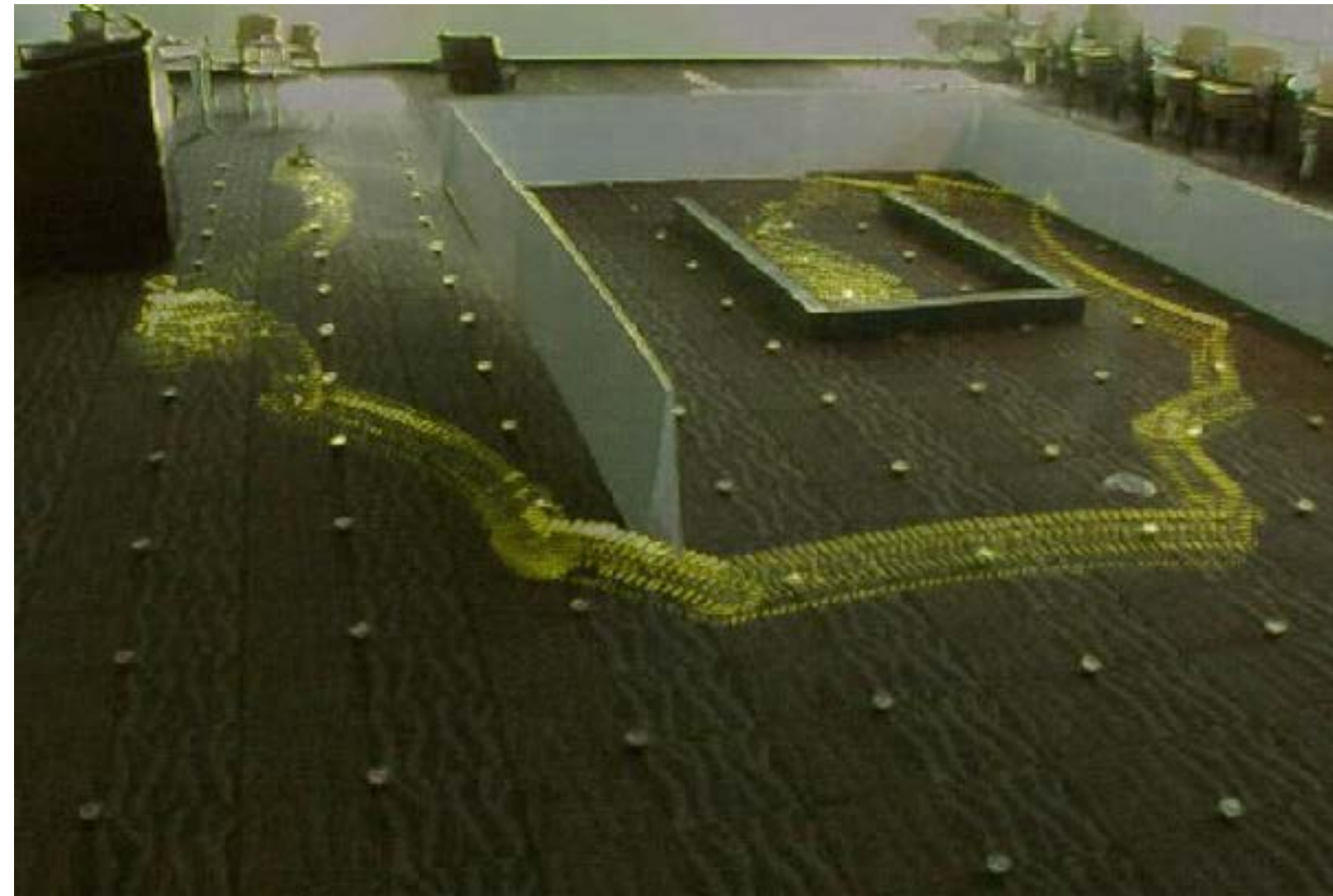
How to implement state?

How to detect "close enough"?

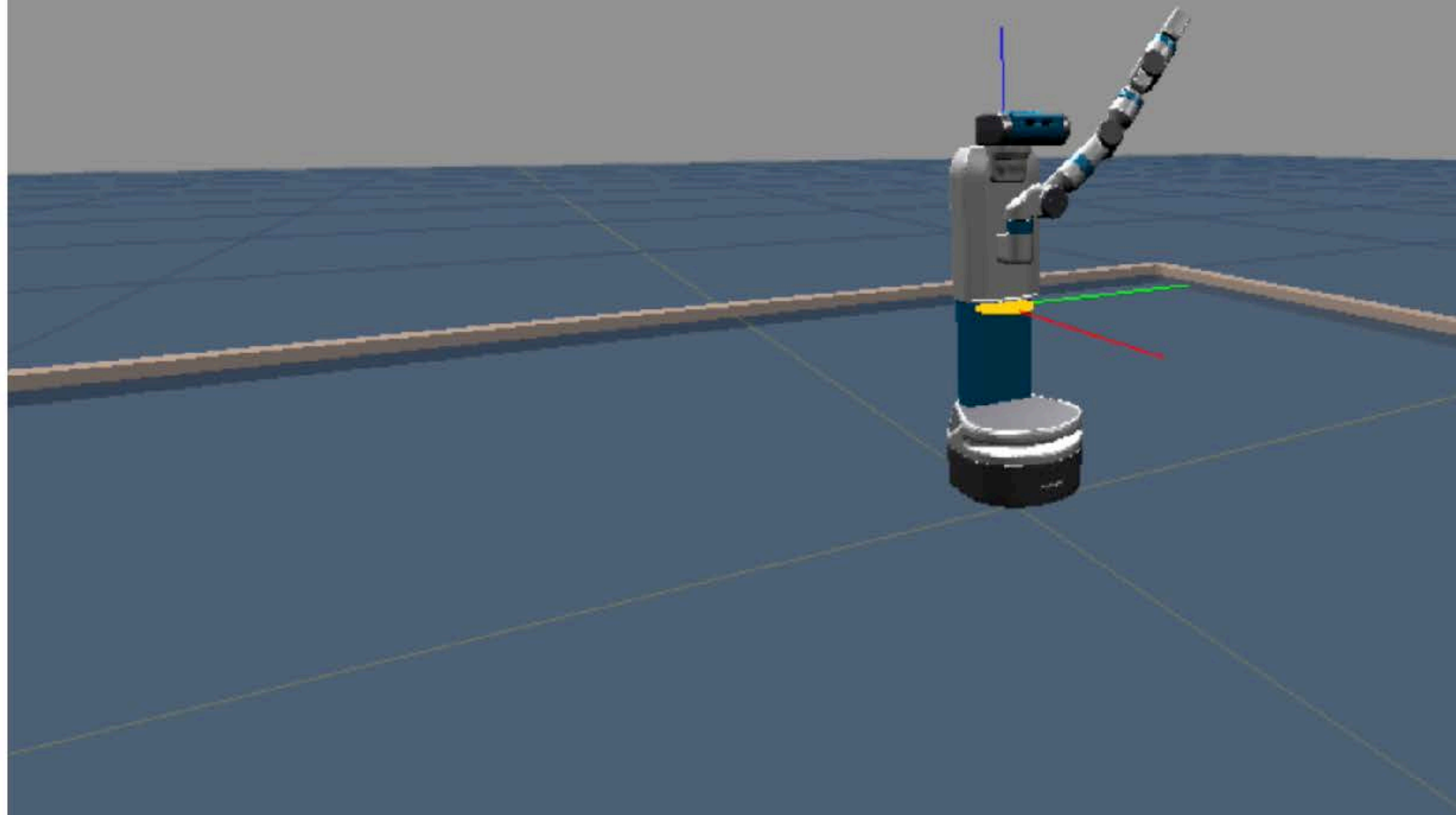


FSMs for Other Tasks

- Robot foraging?
- Robot tennis/pong?
- Pushing a ball into a goal?
- Vacuuming a room
- Driving a car?
- Robot dancing!



joint servo controller has been invoked
executing dance routine, pose 2 of 10

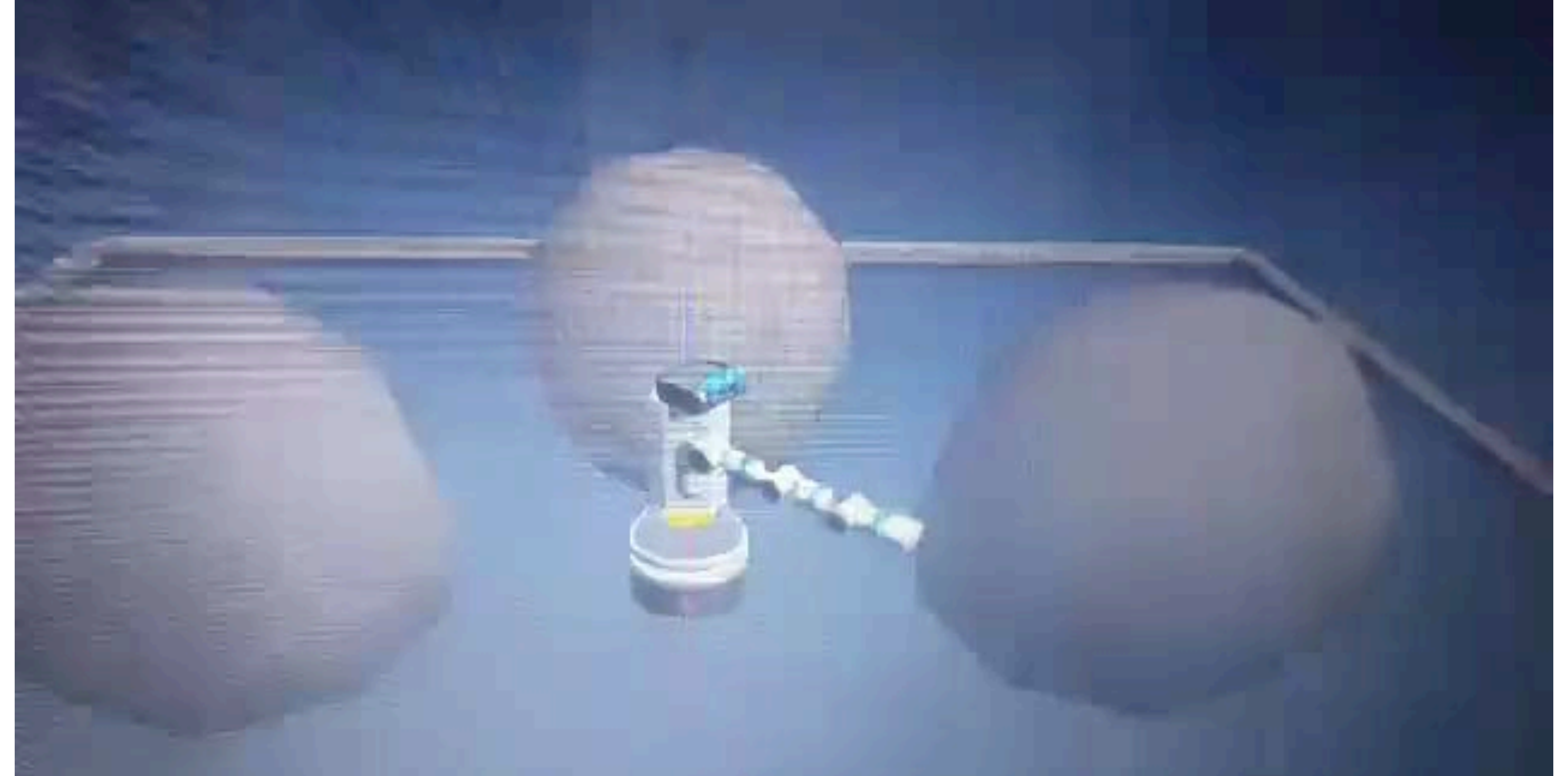


- kineval
- just_starting
- User Parameters
- Robot
- ▾ Forward Kinematics
 - persist_pd
 - update_pd_clock
 - update_pd_da...
 - torso_lift_joint
 - shoulder_pan_joint
 - shoulder_lift_joint
 - upperarm_roll_joint
 - elbow_flex_joint
 - forearm_roll_joint
 - wrist_flex_joint
 - wrist_roll_joint
 - gripper_axis
 - head_pan_joint
 - head_tilt_joint
 - torso_fixed_joint
- Inverse Kinematics

P3 robot dance (by ohseejay)

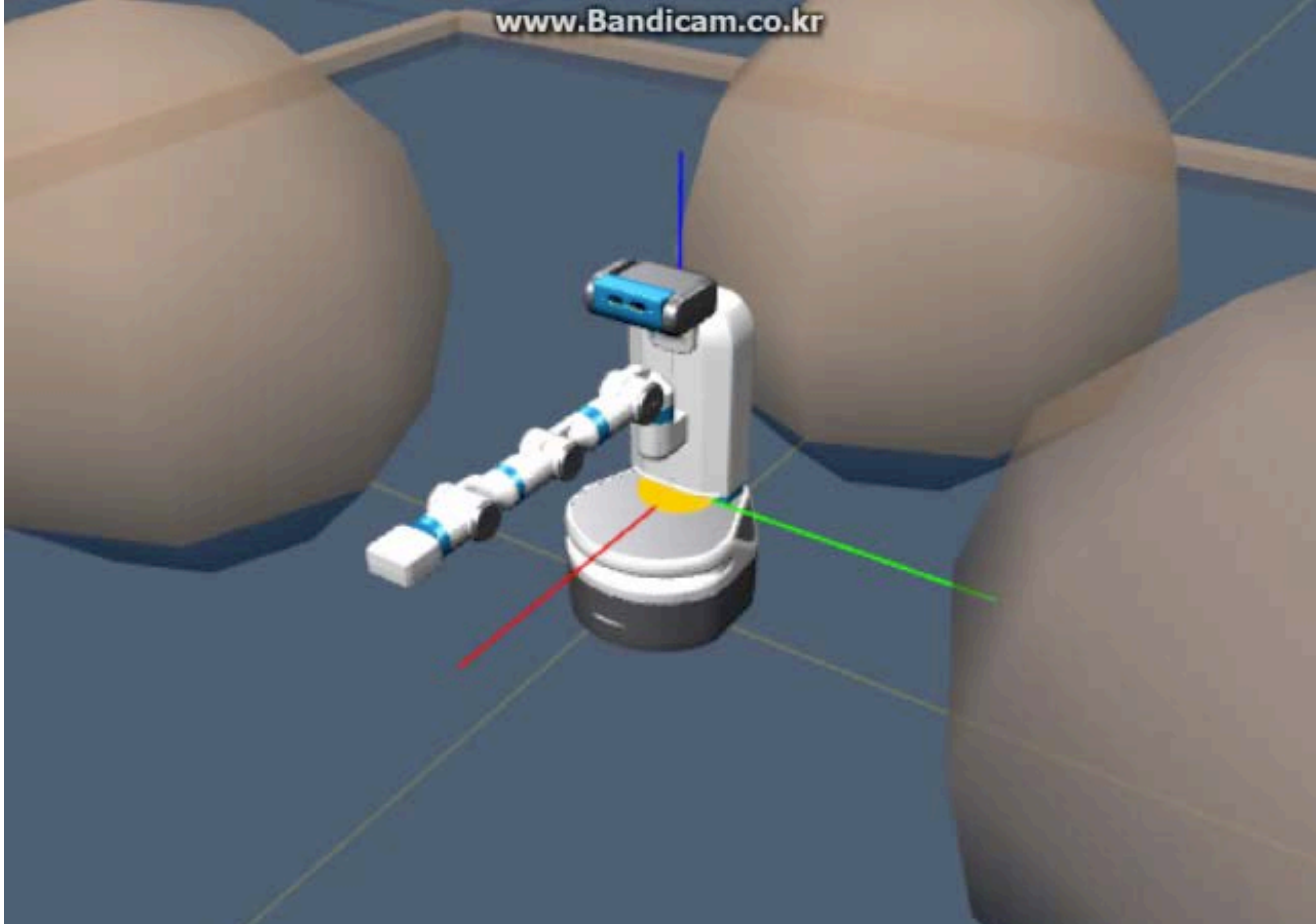
<https://www.youtube.com/watch?v=WyQ9aoB3bpI>



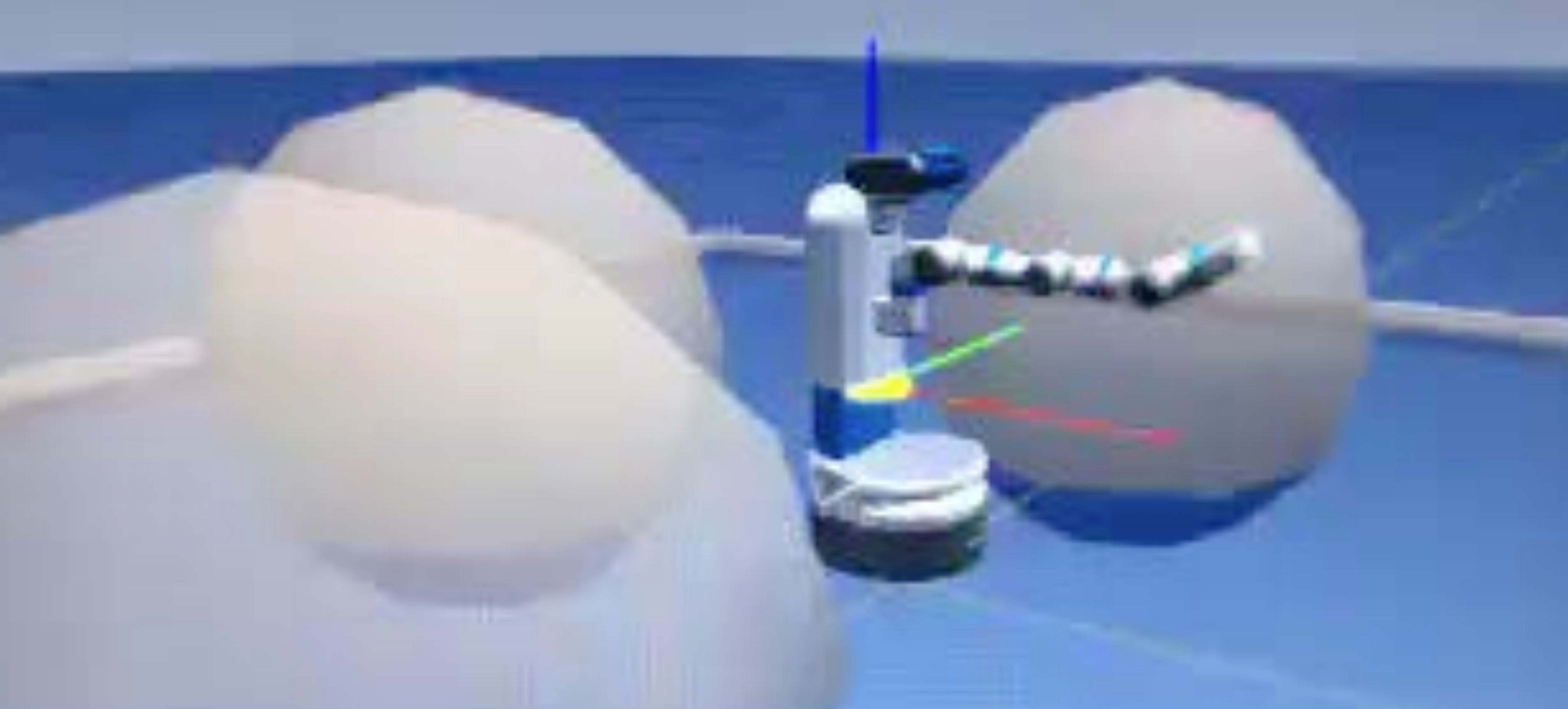


sreesha



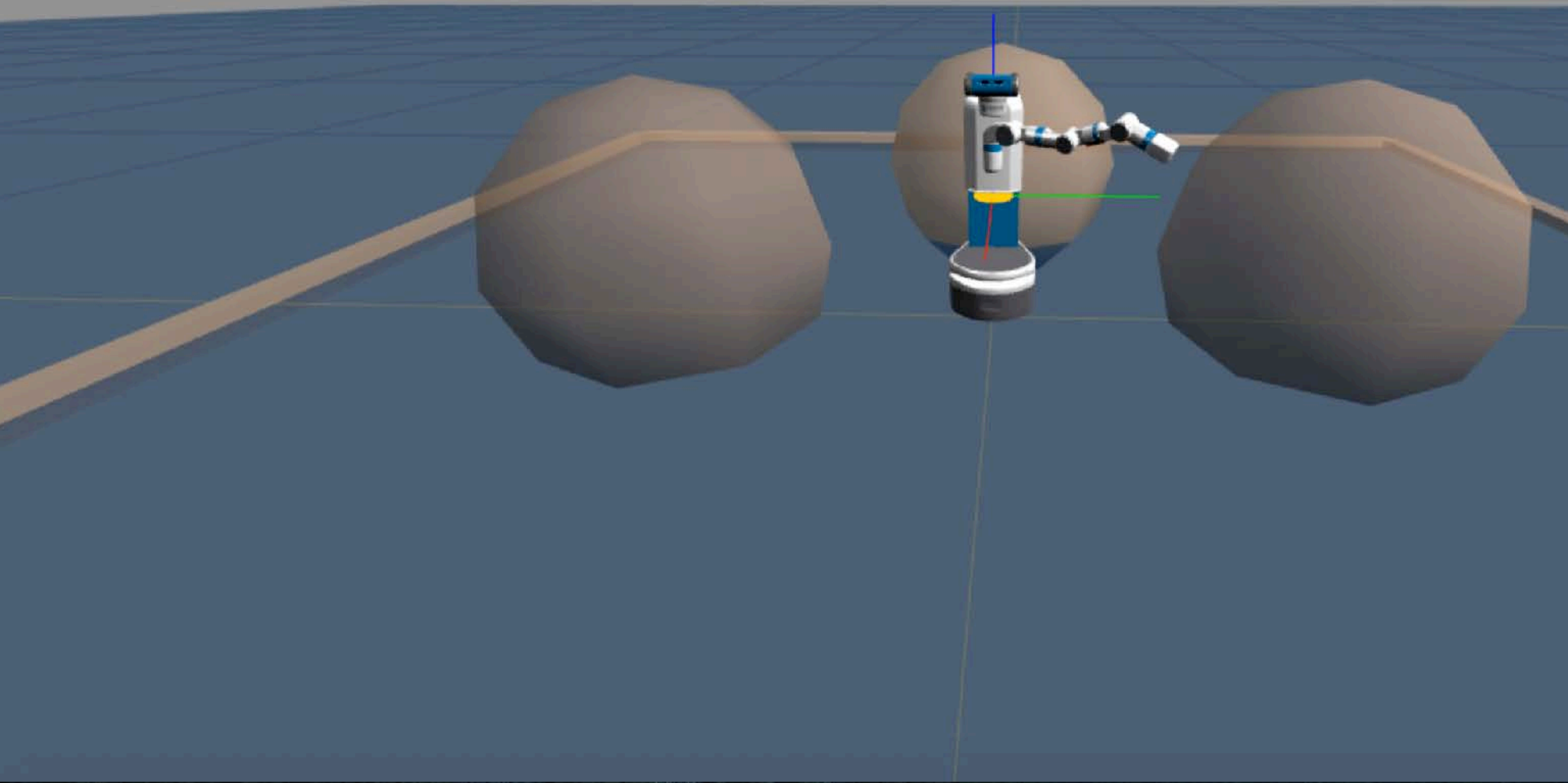


noah



joint servo controller has been invoked
executing dance routine, pose 4 of 10

cneeruko



kineval

just_starting

▸ User Parameters

▸ Robot

▾ Forward Kinematics

persist_pd

update_pd_clock

update_pd_da...

▸ torso_lift_joint

▸ shoulder_pan_joint

▸ shoulder_lift_joint

▸ upperarm_roll_joint

▸ elbow_flex_joint

▸ forearm_roll_joint

▸ wrist_flex_joint

▸ wrist_roll_joint

▸ gripper_axis

▸ head_pan_joint

▸ head_tilt_joint

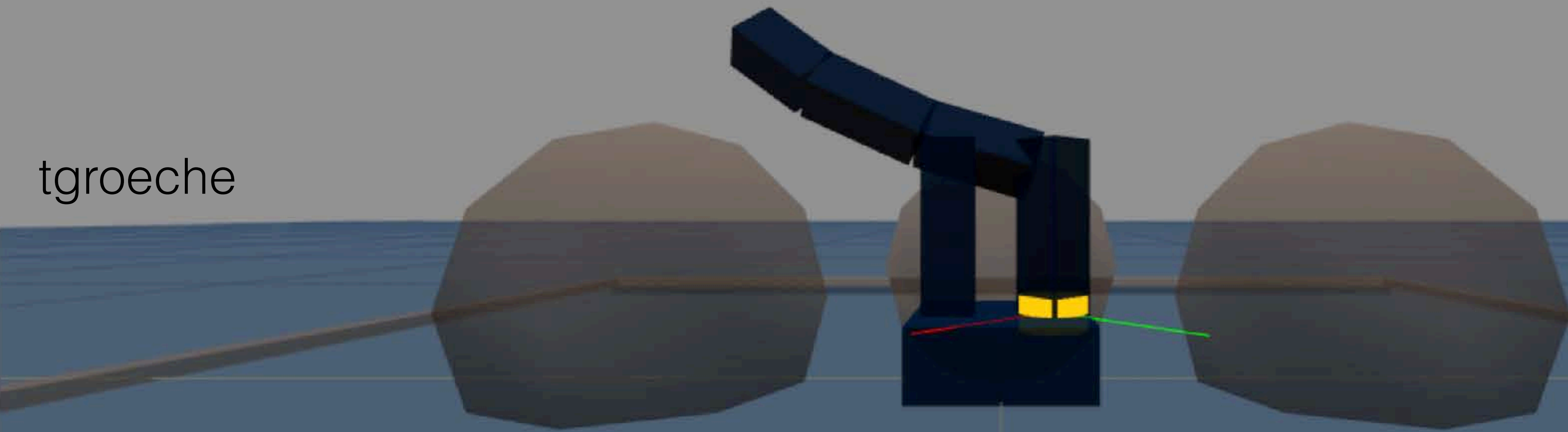
▸ torso_fixed_joint

▸ Inverse Kinematics

Close Controls

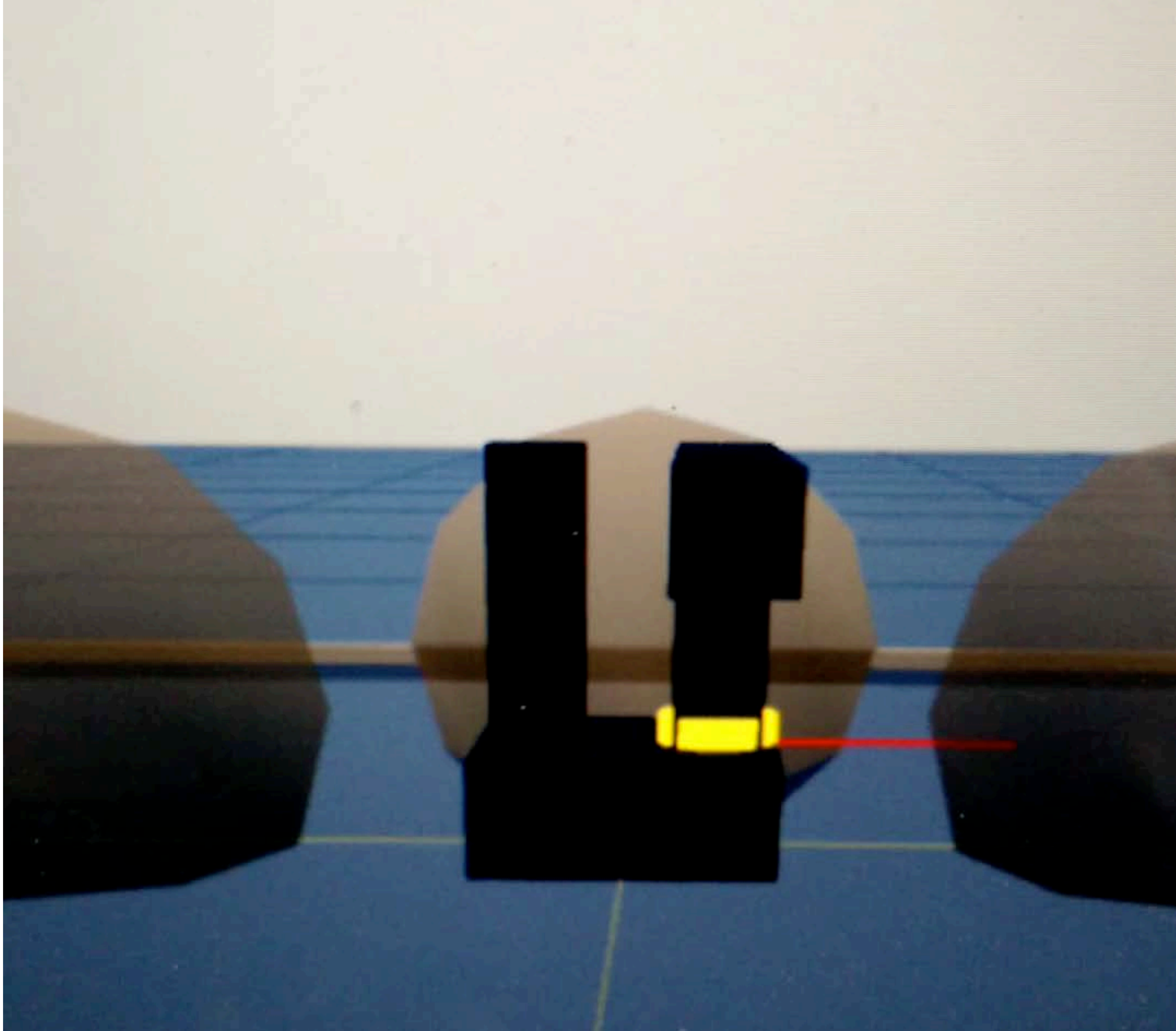
joint servo controller has been invoked
executing dance routine, pose 9 of 10

tgroeche



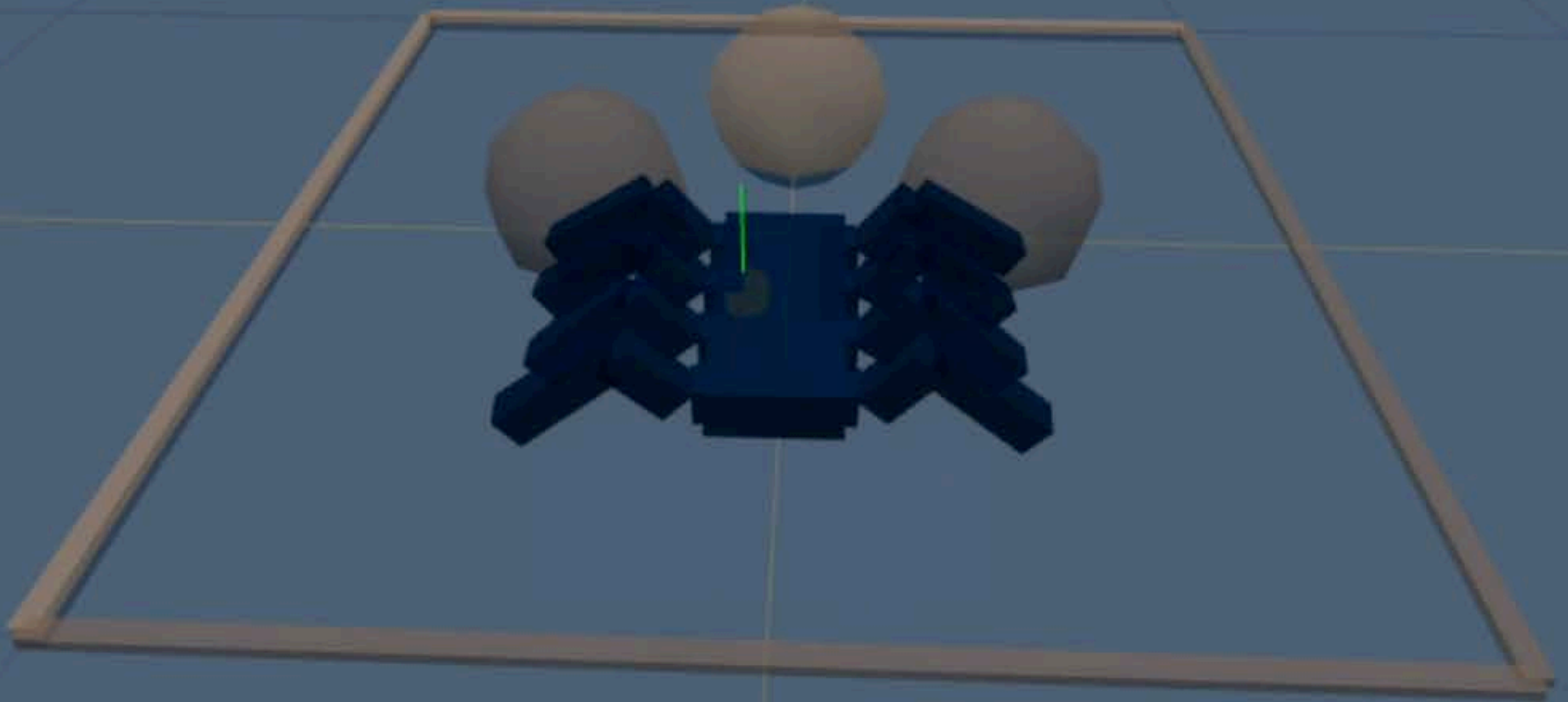
- kineval
- just_starting
- User Parameters
- Robot
- ▾ Forward Kinematics
 - persist_pd
 - update_pd_clock
 - update_pd_da...
 - clavicle_right_yaw
 - shoulder_right_yaw
 - upperarm_right_pitch
 - forearm_right_yaw
 - clavicle_left_roll
- Inverse Kinematics
- Motion Planning
- Display
- Close Controls



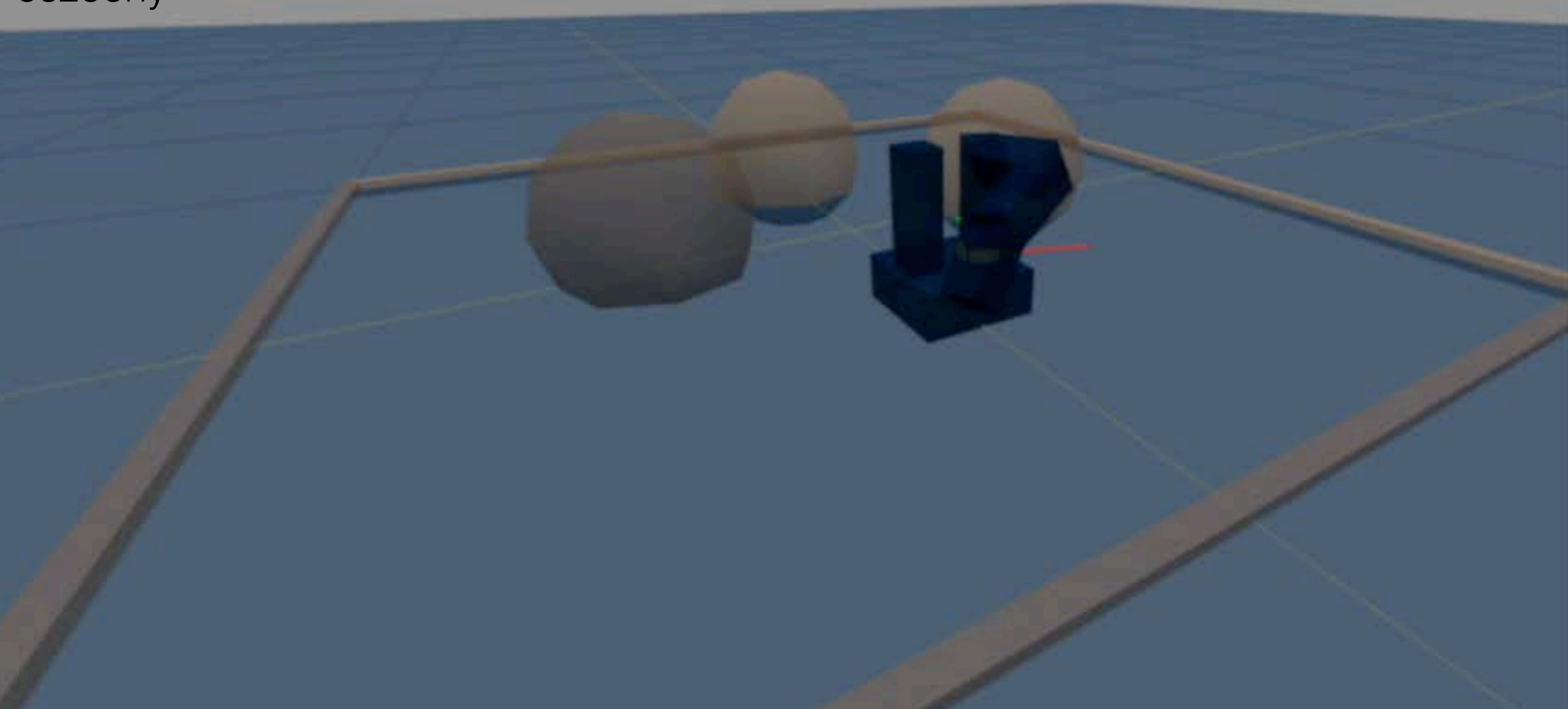


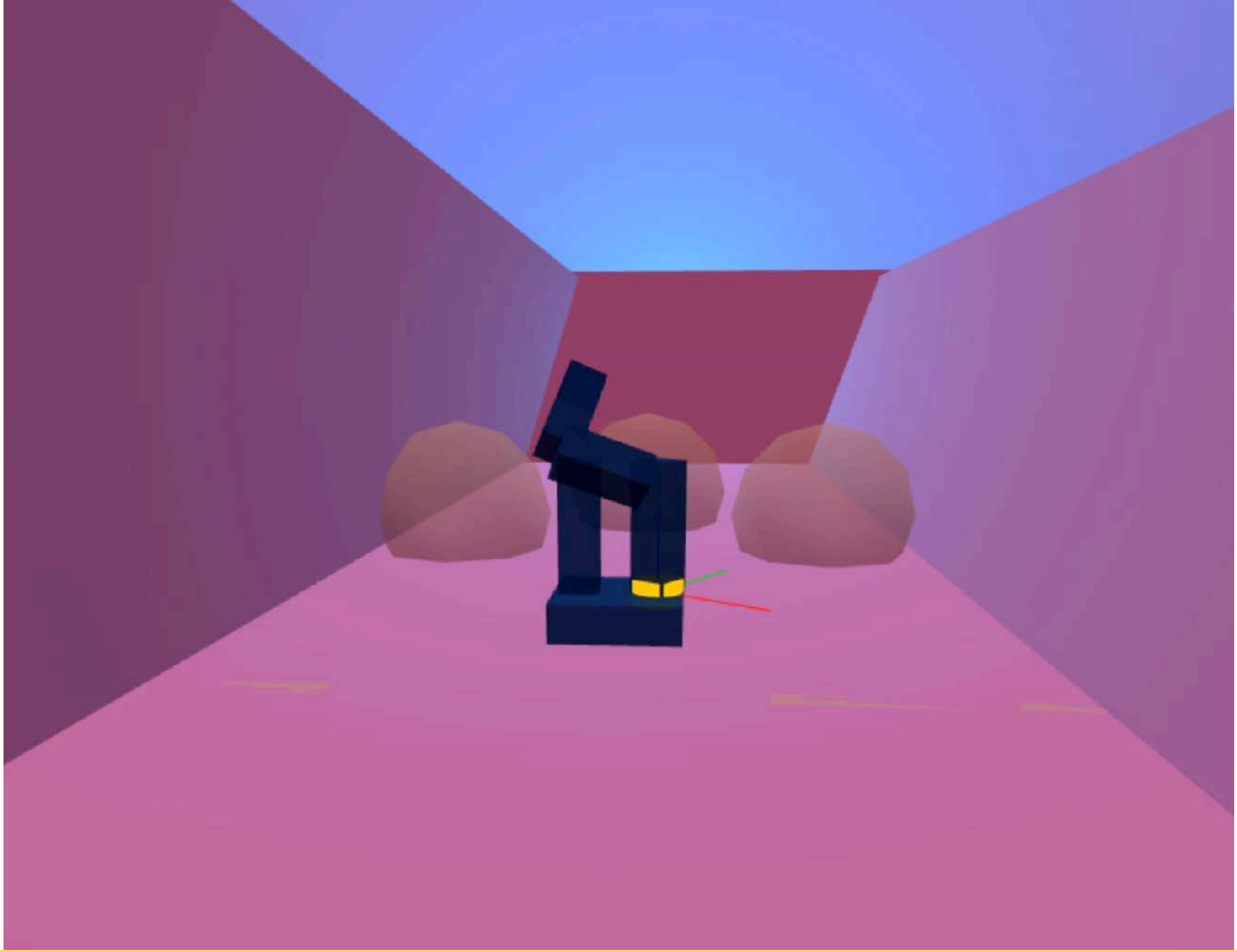
ankit





cszechy





cszechy
ohseejay



Let's generalize FSMs
for robot control



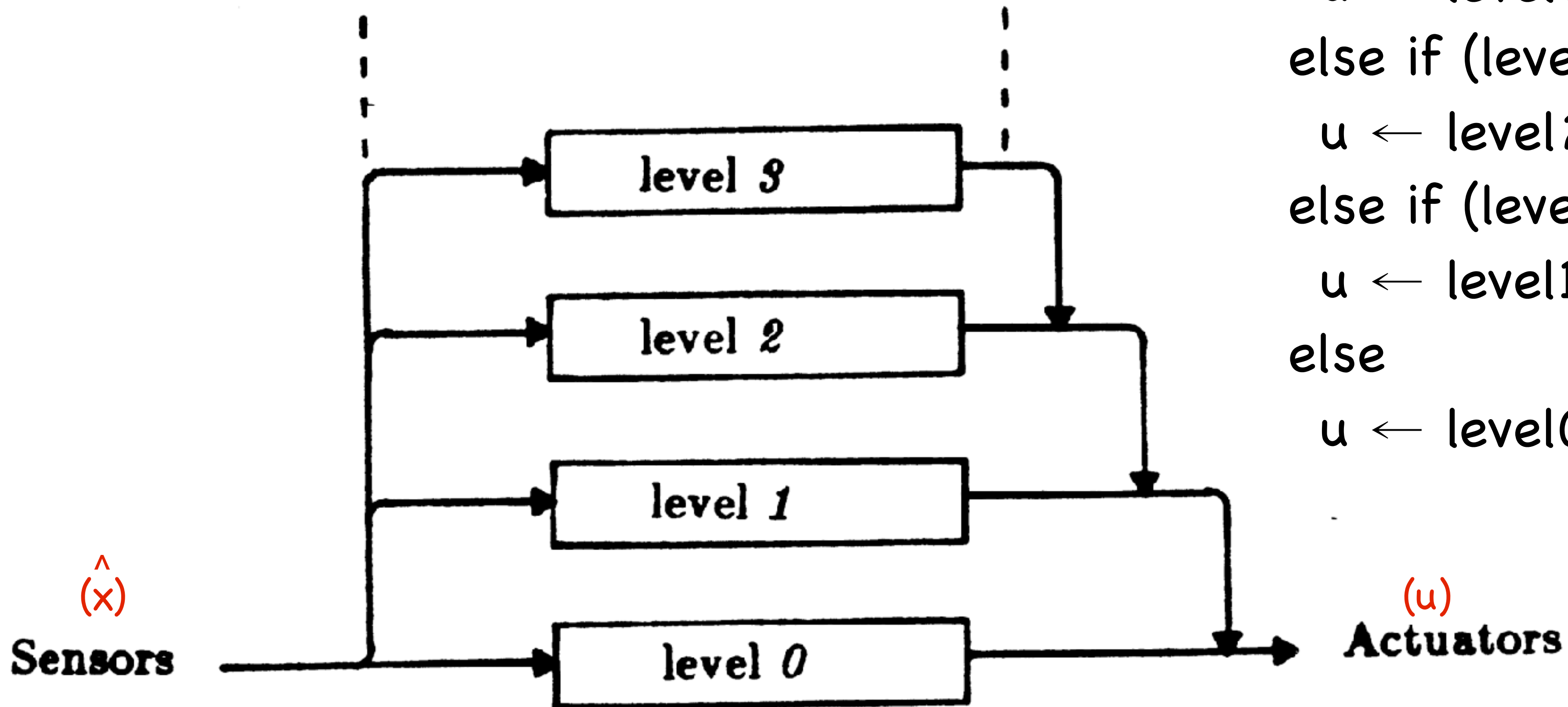
Subsumption Architecture

[Brooks 1986]

- Generalization of FSM-based control
- Collection of modular reactive controllers in a priority hierarchy
- Controllers can be FSMs
- Large nested if-else statement
- Most robots are controlled by some form of subsumption



Subsumption Architecture



```
if (level3_condition)
  u ← level3_control
else if (level2_condition)
  u ← level2_control
else if (level1_condition)
  u ← level1_control
else
  u ← level0_control
```

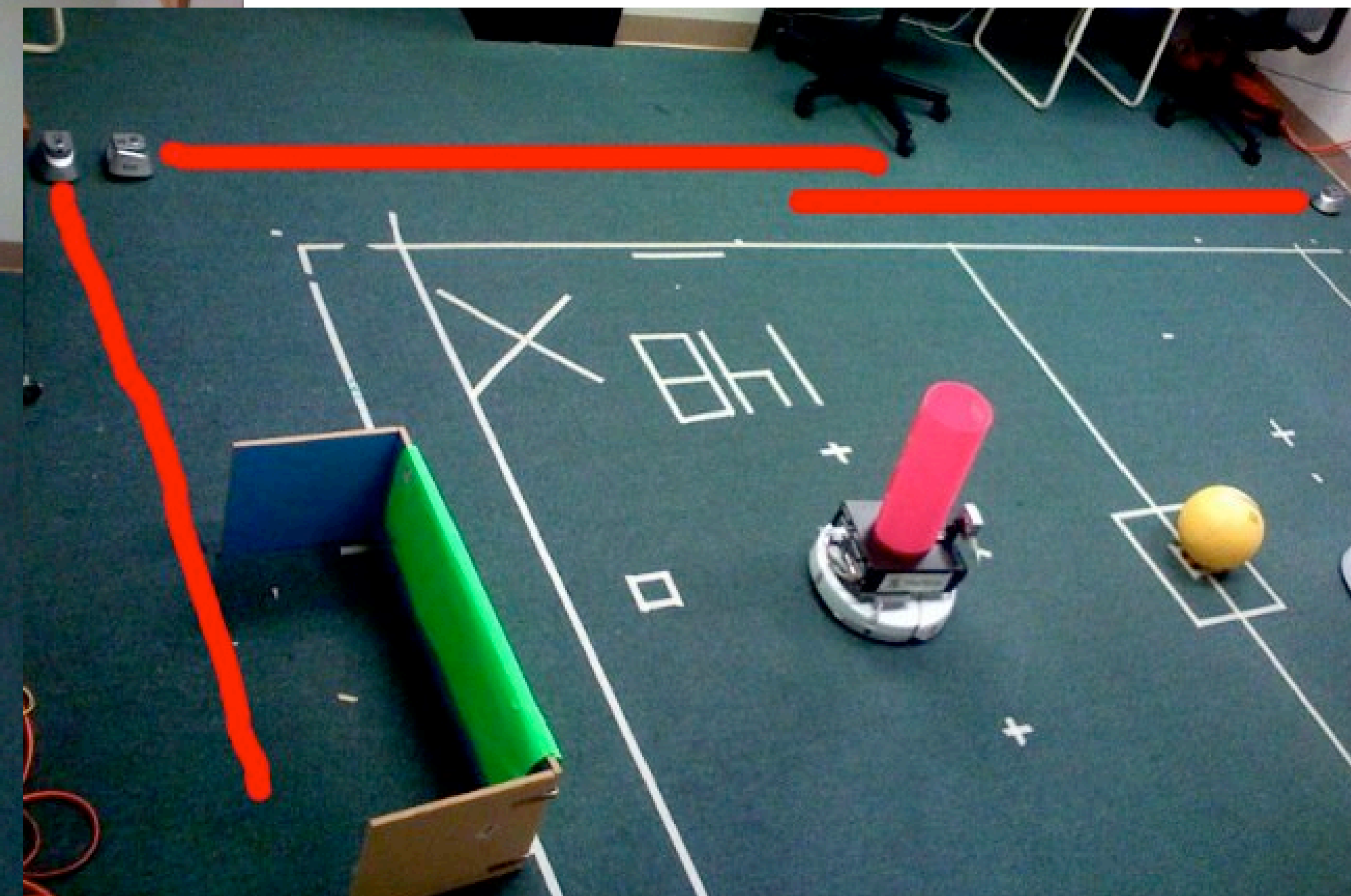
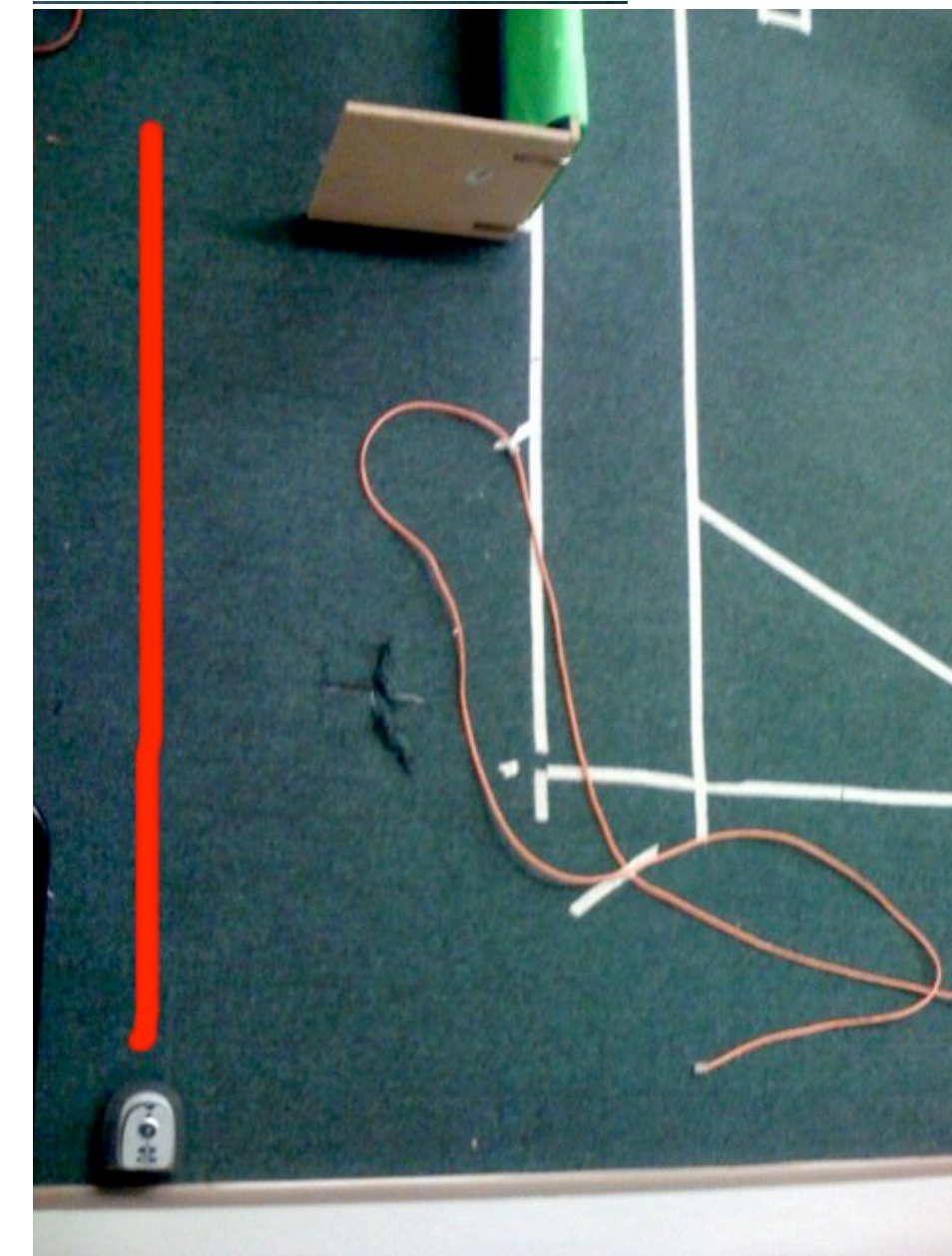

Subsumption Design Process

- 1. Divide your problem into basic competencies** ordered simple to more complex. Designate a level for each basic competency.
- 2. Subdivide each level into multiple simple components** that interact through shared variables. Limit the sharing of variables among levels to avoid incomprehensible code.
- 3. Implement each module as a separate light-weight thread.** You might think of setting the priorities for these threads s.t. modules in a given level have the same priority.
- 4. Implement "arbitration" processes** for suppression and inhibition as one or more separate that serve to control access to shared variables. You might want to control access using semaphores.



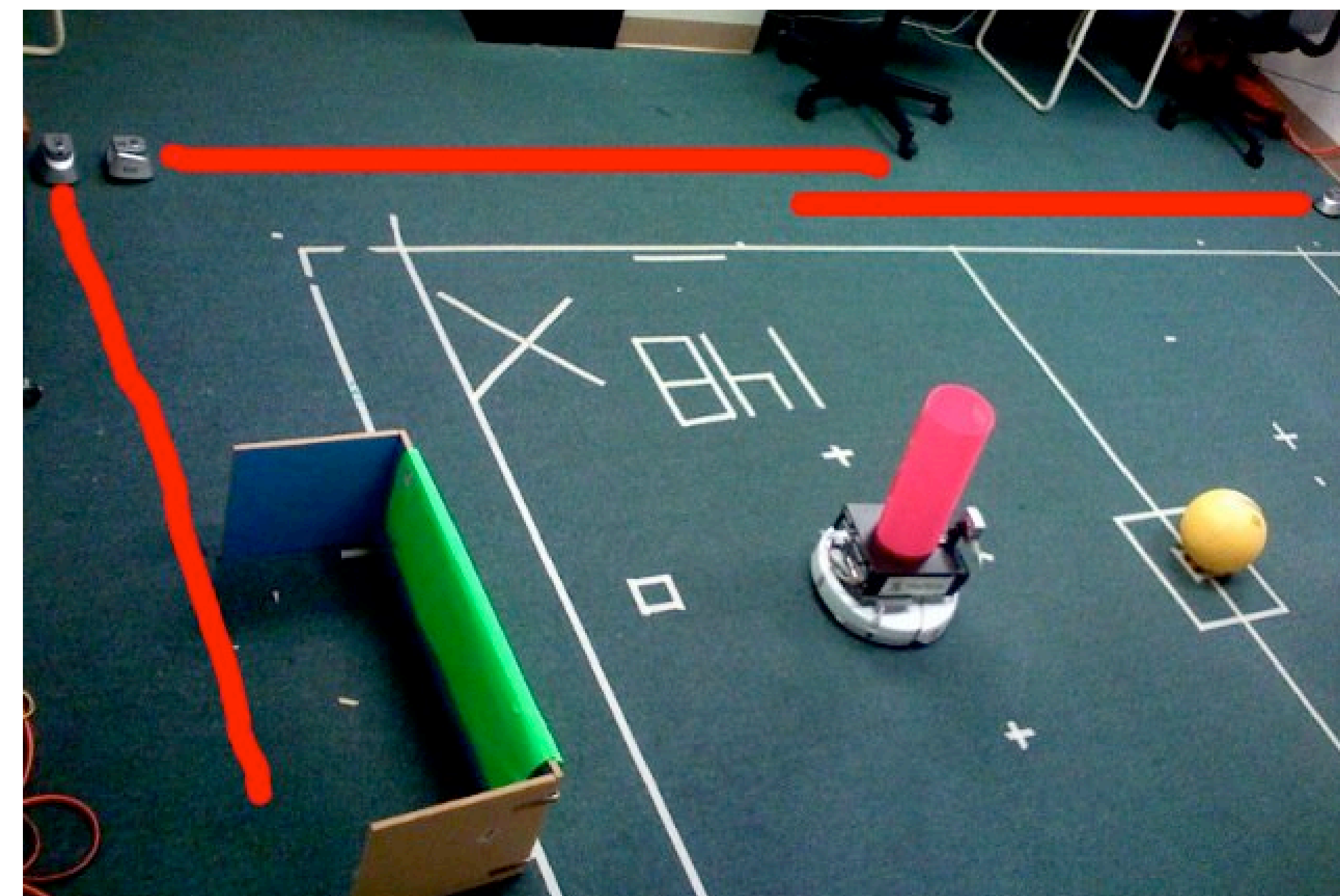
Subsumption for robot soccer

- Propose modules and priority?



What behavior will result?

1. Avoid IR Wall
2. Avoid Robot
3. Avoid Fiducial
4. Bumper Hit
5. Go To Opposite Goal
6. Go To Any Goal
7. Line Up On Ball
8. Go To Ball
9. Score Goal
10. At Ball
11. Look For Ball



Snappy's Subsumption: Goal Scoring

1. Avoid IR Wall
2. Avoid Robot
3. Avoid Fiducial
4. Bumper Hit
5. Go To Opposite Goal
6. Go To Any Goal
7. Line Up On Ball
8. Go To Ball
9. Score Goal
10. At Ball
11. Look For Ball



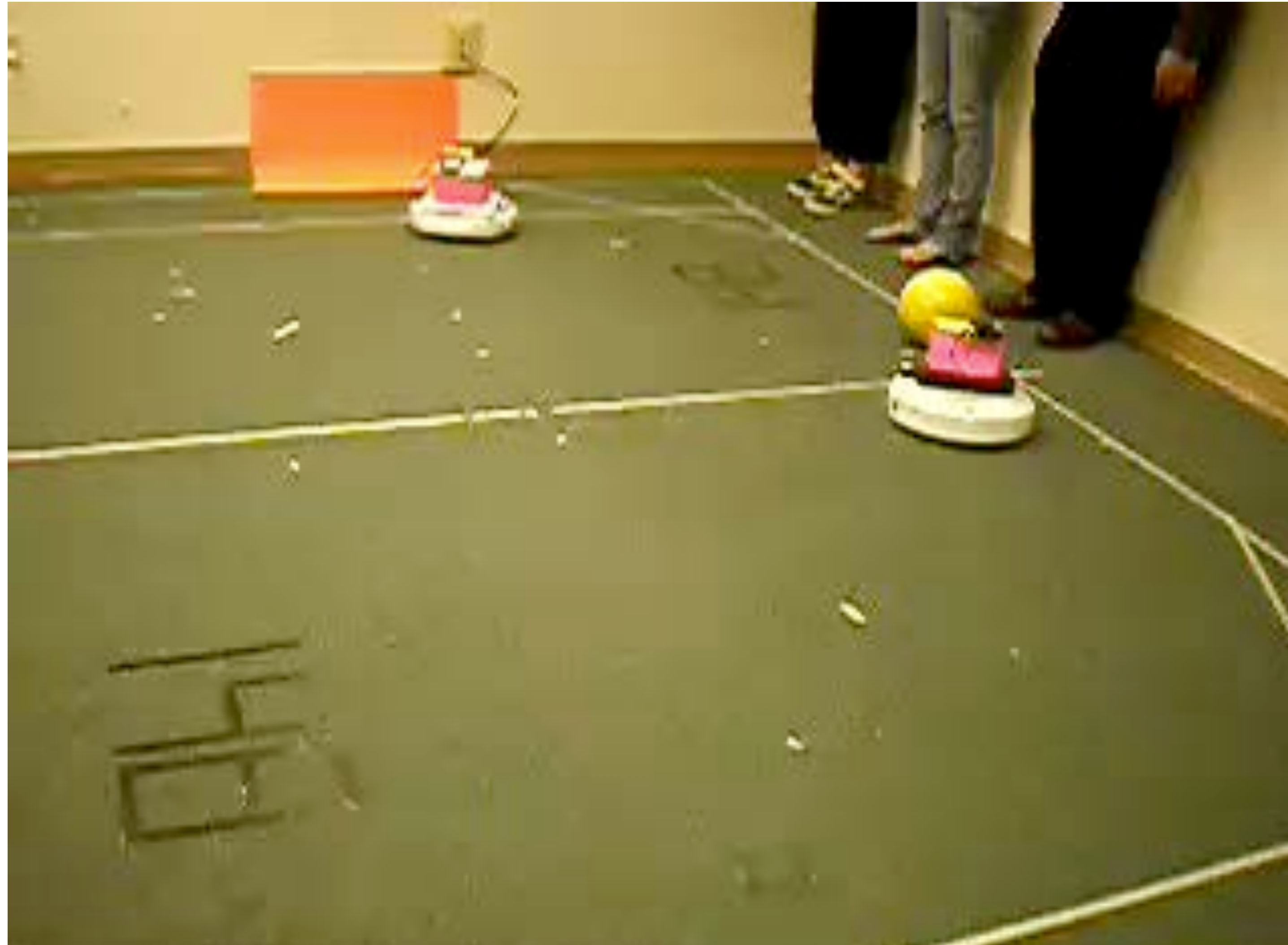
Goal Scoring Challenge - Put ball on orange

Snappy's Subsumption: Navigate to Ball

1. Avoid IR Wall
2. Avoid Robot
3. Avoid Fiducial
4. Bumper Hit
5. Go To Opposite Goal
6. Go To Any Goal
7. Line Up On Ball
8. Go To Ball
9. Score Goal
10. At Ball
11. Look For Ball



Snappy in competition



Are there other methods of
decision making?



Types of Decision Making

- Deliberative (Planner-based) Control
 - “Think hard, act later.”
- Reactive Control
 - “Don’t think, (re)act.”
- Hybrid Control
 - “Think and act separately & concurrently.”
- Behavior-Based Control
 - “Think the way you act.”



Next lecture: Inverse Kinematics

